

# Cambridge International A Level

---

**MATHEMATICS****9709/32**

Paper 3 Pure Mathematics 3

**February/March 2025****MARK SCHEME**

Maximum Mark: 75

---

**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the February/March 2025 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

---

This document consists of **23** printed pages.

**PUBLISHED**  
**Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

**GENERIC MARKING PRINCIPLE 1:**

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

**GENERIC MARKING PRINCIPLE 2:**

Marks awarded are always **whole marks** (not half marks, or other fractions).

**GENERIC MARKING PRINCIPLE 3:**

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

**GENERIC MARKING PRINCIPLE 4:**

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

**GENERIC MARKING PRINCIPLE 5:**

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

**GENERIC MARKING PRINCIPLE 6:**

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

**Mathematics Specific Marking Principles**

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

**Annotations guidance for centres**

Examiners use a system of annotations as a shorthand for communicating their marking decisions to one another. Examiners are trained during the standardisation process on how and when to use annotations. The purpose of annotations is to inform the standardisation and monitoring processes and guide the supervising examiners when they are checking the work of examiners within their team. The meaning of annotations and how they are used is specific to each component and is understood by all examiners who mark the component.

We publish annotations in our mark schemes to help centres understand the annotations they may see on copies of scripts. Note that there may not be a direct correlation between the number of annotations on a script and the mark awarded. Similarly, the use of an annotation may not be an indication of the quality of the response.

The annotations listed below were available to examiners marking this component in this series.

**Annotations**

<b>Annotation</b>	<b>Meaning</b>
	More information required
	Accuracy mark awarded zero
	Accuracy mark awarded one
	Independent accuracy mark awarded zero
	Independent accuracy mark awarded one
	Independent accuracy mark awarded two
	Benefit of the doubt
	Blank Page
	Incorrect point
Dep	Used to indicate DM0 or DM1

<b>Annotation</b>	<b>Meaning</b>
DM1	Dependent on the previous M1 mark(s)
FT	Follow through
wavy	Indicate working that is right or wrong
Highlighter	Highlight a key point in the working
ISW	Ignore subsequent work
J	Judgement
JU	Judgement
M0	Method mark awarded zero
M1	Method mark awarded one
M2	Method mark awarded two
MR	Misread
O	Omission or Other solution
Off-page comment	Allows comments to be entered at the bottom of the RM marking window and then displayed when the associated question item is navigated to.
On-page comment	Allows comments to be entered in speech bubbles on the candidate response.
PE	Judgment made by the PE
Pre	Premature approximation
SC	Special case

Annotation	Meaning
<b>SEEN</b>	Indicates that work/page has been seen
<b>SF</b>	Error in number of significant figures
	Correct point
<b>TE</b>	Transcription error
<b>XP</b>	Correct answer from incorrect working

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

### Types of mark

- M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B** Mark for a correct result or statement independent of method marks.
- DM or DB** When a part of a question has two or more ‘method’ steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
  - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
  - The total number of marks available for each question is shown at the bottom of the Marks column.
  - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
  - Square brackets [ ] around text or numbers show extra information not needed for the mark to be awarded.

**Abbreviations**

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

Question	Answer	Marks	Guidance
1	State that $1 - e^{-2x} = e^{-3}$	B1	OE, with ln removed.
	Use correct method to solve an equation of the form $e^{\pm 2x} = a$ , where $a > 0$ , and a reasonable attempt at the B1, for $\pm 2x \ln e$ or $\pm x \ln e$	M1	E.g. $[e^{-2x} = 1 - e^{-3}]$ $-2x = \ln(1 - e^{-3}) \dots$ OE. Can be numerical $\ln(1 - 0.049787) = \ln 0.9502$ . Evidence of method must be seen.
	Obtain answer 0.0255	A1	CAO Must be 4 decimal places. No working seen scores 0.
<b>Alternative Method for Question 1</b>			
	State that $1 - e^{-2x} = e^{-3}$	B1	OE, without ln.
	Rearrange to obtain an expression for $e^x$ <b>and</b> solve an equation of the form $e^{\pm x} = a$ , where $a > 0$ , and a reasonable attempt at the B1, for $x$	M1	E.g. $\left[ e^x = \sqrt{\frac{1}{1-e^{-3}}}, e^x = \sqrt{\frac{e^3}{e^3-1}} \right]$ , $x = \ln \sqrt{\frac{1}{1-e^{-3}}}$ Can be numerical. Evidence of method must be seen.
	Obtain answer 0.0255	A1	CAO Must be 4 decimal places. No working seen scores 0.
		3	

<b>Question</b>	<b>Answer</b>	<b>Marks</b>	<b>Guidance</b>
2	State or imply $\frac{1+2\frac{dy}{dx}}{x+2y}$ as the derivative of $\ln(x+2y)$	<b>B1</b>	
	State derivative of $xy^2$ is $x2y \frac{dy}{dx} + y^2$	<b>B1</b>	$x^2y \frac{dy}{dx} + y^2$
	Obtain $y^2 + 2xy \frac{dy}{dx} + \frac{1+2\frac{dy}{dx}}{x+2y} = 0$	<b>B1</b>	OE May be implied by correct final answer.
	Obtain $y = \frac{1}{2}e$ when $x = 0$	<b>B1</b>	OE Allow $\frac{1}{2} \times 2.718$ or 1.36 or better e.g. 1.359... May be implied by correct final answer.
	Obtain $\frac{dy}{dx} = -\frac{1}{8}(e^3 + 4)$	<b>B1</b>	OE Accept AWRT –3.01. ISW.
		<b>5</b>	

Question	Answer	Marks	Guidance
3(a)	Obtain $\text{Im}(z) \leq -1$	B1	Condone strict inequalities throughout (a).
	Obtain answer of the form $ z - a  \leq b$	M1	Accept equation or any inequality sign. $a = \pm 2 \pm i$ and $b = 3$ , e.g. $ z + 2 - i  = 3$ or $ z + 2 - i  > 3$ .
	Obtain answer $ z + 2 - i  \leq 3$	A1	Accept $ z - (-2 + i)  \leq 3$ as final answer. Do not ISW.
		3	
3(b)	Identify the coordinates of correct point	M1*	$(-2 - \sqrt{5}, -1)$ , if correct. From solving $(x \pm 2)^2 + (y \pm 1)^2 = 3^2$ (or = 9) with $y = -1$ , or attempt to get $2 + \sqrt{5}$ using a right-angled triangle.
	Carry out a correct method for finding the greatest value of $ z $	DM1	
	Obtain answer 4.35 or $\sqrt{10 + 4\sqrt{5}}$	A1	AWRT 4.35, e.g. 4.3525...
		3	

Question	Answer	Marks	Guidance
4	State $\frac{\tan x - \sqrt{3}}{1 + \sqrt{3} \tan x}$	B1	OE Allow decimals throughout.
	2 cot $x$ replaced by $\frac{2}{\tan x}$	B1	SOI
	Reduce the equation to $\tan^2 x - 3\sqrt{3} \tan x - 2 = 0$ , or three-term equivalent	B1	May be implied by further work.
	Solve a three-term quadratic in $\tan x$ , for $x$	M1	FT <i>their</i> 3-term quadratic. Allow $\tan^{-1}(..)$ .
	Obtain answer, e.g. $79.8^\circ$	A1	AWRT $79.8$ .
	Obtain the second answer, e.g. $160.2^\circ$ and no other in the interval	A1	Allow $160$ , or AWRT $160.2$ . Treat answers in radians as a misread. Ignore answers outside the given interval.
		6	

<b>Question</b>	<b>Answer</b>	<b>Marks</b>	<b>Guidance</b>
5	Square $x + iy$ and equate real and imaginary parts to $-4$ and $6\sqrt{5}$ respectively	M1	
	Obtain equations $x^2 - y^2 = -4$ and $2xy = 6\sqrt{5}$ or $\sqrt{x^2 + y^2} = \sqrt{(-4)^2 + (6\sqrt{5})^2}$	A1	Or $x^2 + y^2 = 14$ .
	Eliminate one variable and find a horizontal equation in the other	M1	Allow slips in e.g. signs, powers etc.
	Obtain $x^4 + 4x^2 - 45 = 0$ or $y^4 - 4y^2 - 45 = 0$ or three-term equivalents, or $2x^2 = 10$ or $2y^2 = 18$	A1	May be implied by further work.
	Obtain answers $\pm(\sqrt{5} + 3i)$	A1	Accept e.g. $x = \sqrt{5}$ , $y = 3$ and $x = -\sqrt{5}$ , $y = -3$ or $\pm(\sqrt{5}, 3)$ , but must be clearly paired. Can be implied by (e.g.) column working.
		5	

Question	Answer	Marks	Guidance
6	Use correct double angle formula to express $\sin^2 2\theta$ in terms of $\cos 4\theta$	<b>B1</b>	$\sin^2 2\theta = \frac{1}{2} (1 - \cos 4\theta)$
	Separate variables correctly and reasonable attempt at integration of at least one side	<b>M1</b>	Position of $(x + 5)$ or $(\frac{1}{5}x + 1)$ and $\sin^2 2\theta$ sufficient for correct separation.
	Obtain term $5\ln\left(\frac{1}{5}x+1\right)$	<b>B1</b>	OE May see $5\ln(x+5)$ .
	Obtain term $\frac{1}{2}(\theta - \frac{1}{4}\sin 4\theta)$	<b>B1 FT</b>	Allow $\frac{1}{2}(\pm\theta \pm \frac{1}{4}\sin 4\theta)$ from $= \frac{1}{2}(\pm 1 \pm \cos 4\theta)$ .
	Use $x = 5$ when $\theta = 0$ to evaluate a constant or as limits in a solution containing terms of the form $\ln\left(\frac{1}{5}x+1\right)$ , $\theta$ and $\sin 4\theta$	<b>M1</b>	OE
	Obtain correct answer in any form	<b>A1</b>	E.g. $5\ln(x+5) = \frac{1}{2}(\theta - \frac{1}{4}\sin 4\theta) + 5\ln 10$
	Obtain final answer $x = 10\exp\left[\frac{1}{10}\left(\theta - \frac{1}{4}\sin 4\theta\right)\right] - 5$ or equivalent with ln removed	<b>A1 FT</b>	$x = 10\exp\left[\frac{1}{2}\left(\pm\theta \pm \frac{1}{4}\sin 4\theta\right)\right] - 5$ Must remove ln from $\ln(x+5) = \frac{1}{2}(\pm\theta \pm \frac{1}{4}\sin 4\theta) + \alpha \ln 10$ .
		7	

Question	Answer	Marks	Guidance
7(a)	Use correct product rule	M1	$3x^2 \cos(2x) + x^3 \left( \frac{d}{dx}(\cos 2x) \right)$ OE
	Obtain derivative $3x^2 \cos(2x) - 2x^3 \sin(2x)$	A1	OE
	Equate correct derivative to zero and obtain $p = \frac{1}{2} \tan^{-1}\left(\frac{3}{2p}\right)$ after full and correct working	A1	AG Must reach $\tan 2p = \dots$ or $\tan 2x = \dots$ before given answer.
		3	
7(b)	Calculate the values of a relevant expression or pair of expressions at $x = 0.5$ and $x = 0.7$ Must have at least 1 of 2 values correct or 3 of 4 values correct	M1	$f(p) = p - \frac{1}{2} \tan^{-1}\left(\frac{3}{2p}\right)$ $f(0.5) = -0.124\dots < 0, f(0.7) = 0.132\dots > 0$ or comparing $p$ and $\frac{1}{2} \tan^{-1}\left(\frac{3}{2p}\right)$ . $0.5 \quad \frac{1}{2} \tan^{-1}\left(\frac{3}{2p}\right) = 0.624\dots \quad 0.5 < 0.624\dots$ $0.7 \quad \frac{1}{2} \tan^{-1}\left(\frac{3}{2p}\right) = 0.567\dots \quad 0.7 > 0.567$
	Complete the argument correctly with correct calculated values	A1	
		2	

<b>Question</b>	<b>Answer</b>	<b>Marks</b>	<b>Guidance</b>
7(c)	Use the iterative formula correctly at least twice	<b>M1</b>	
	Obtain final answer 0.596	<b>A1</b>	
	Show sufficient iterations to at least 5 decimal places to justify 0.596 to 3 decimal places or show there is a sign change in the interval (0.5955, 0.5965)	<b>A1</b>	E.g. 0.5, 0.62452, 0.58814, 0.59856, 0.59556, 0.59642 0.6, 0.59514, 0.59654, 0.59614, 0.59626 0.7, 0.56708, 0.60467, 0.59380, 0.59693, 0.59603, 0.59629 Can recover from wrong values.
		<b>3</b>	

Question	Answer	Marks	Guidance
8(a)	Express general point of a line in component form, e.g. $(-1 + 2\lambda, 3 + 3\lambda, -4 - \lambda)$ or $(2 - \mu, -3 - 2\mu, -1 + \mu)$	B1	
	Equate at least two pairs of components and solve for $\lambda$ or for $\mu$	M1	
	Obtain correct answer for $\lambda$ or for $\mu$	A1	Possible answers are 6, 12, 0 for $\lambda$ and -9, -21, -3 for $\mu$ .
	Verify that one component equation is not satisfied Can show by correctly obtaining 2 values of $\lambda$ or 2 values of $\mu$	A1	E.g. show $21 \neq 15$ for $(11, 21, -10)$ and $(11, 15, -10)$ , or show $-16 \neq -22$ for $(23, 39, -16)$ and $(23, 39, -22)$ , or show $-1 \neq 5$ for $(-1, 3, -4)$ and $(5, 3, -4)$ .
	Show that the lines are not parallel	B1	E.g. $\begin{pmatrix} 2 \\ 3 \\ -1 \end{pmatrix} \neq k \begin{pmatrix} -1 \\ -2 \\ 1 \end{pmatrix}$ at least 2 components required.  Just a statement that direction vectors are not scalar multiple of each other insufficient, if direction vectors have not been clearly identified. Also, told answer is skew.
		5	

Question	Answer	Marks	Guidance
8(b)	Carry out correct process for evaluating the scalar product of $\begin{pmatrix} 2 \\ 3 \\ -1 \end{pmatrix}$ and $\begin{pmatrix} -1 \\ -2 \\ 1 \end{pmatrix}$	<b>M1</b>	E.g. $(2 \times -1) + (3 \times -2) + (-1 \times 1)$ or $-2 - 6 - 1$ or $-9$ .
	Using the correct process for the moduli, divide the scalar product by the product of the moduli and evaluate the inverse cosine of the result	<b>M1</b>	Allow for any pair of vectors here but must be consistent between scalar product and magnitudes.
	Obtain answer AWRT $169.1^\circ$ or $2.95^c$	<b>A1</b>	Allow $169^\circ$ .
		<b>3</b>	

Question	Answer	Marks	Guidance
9(a)	Substitute $x = 3$ or $-3$ into $p(x)$ and equate to 0 or into $p'(x)$ and equate to 72	<b>M1*</b>	
	Obtain $162 + 9a + 3b + 9 = 0$	<b>A1</b>	OE
	Obtain $162 + 6a + b = 72$	<b>A1</b>	OE
	Solve simultaneous equations to obtain either $a$ or $b$ after using $p(\pm 3) = 0$ and $p'(\pm 3) = 72$	<b>DM1</b>	
	Obtain $a = -11$ and $b = -24$	<b>A1</b>	
		<b>5</b>	

Question	Answer	Marks	Guidance
9(b)	Equate $(x - 3)(6x^2 + Ax + B)$ to $6x^3 - 11x^2 - 24x + 9$ and obtain equations to solve for $A$ and $B$  or divide $6x^3 - 11x^2 - 24x + 9$ by $x - 3$ and reach $6x^2 \pm 7x$	M1	Using <i>their a</i> and <i>their b</i> . $A - 18 = a = -11$ , $B - 3A = -b = -24$ , $-3B = 9$ . $A = 7$ and $B = -3$ .  Or reach $6x^2 \pm (\text{their } a + 18)x$ .
	$(x - 3)(6x^2 + 7x - 3)$	A1	SOI
	Obtain $(x - 3)(2x + 3)(3x - 1)$	A1	
			Special Case: If only $(x - 3)(x + \frac{3}{2})(x - \frac{1}{3})$ or $(x - 3)(2x + 3)(3x - 1)$ seen, SC B1 only (but can gain two marks in (c)).
		3	
9(c)	Obtain one correct region $x < -\frac{3}{2}$ or $\frac{1}{3} < x < 3$	B1 FT	Must be final answer not in working. FT is on the last two brackets (not $(x - 3)$ ).
	Obtain both regions $x < -\frac{3}{2}$ , $\frac{1}{3} < x < 3$	B1 FT	Allow $x < -\frac{3}{2}$ and $\frac{1}{3} < x < 3$ . SC B1 for $x \leq -\frac{3}{2}$ , $\frac{1}{3} \leq x \leq 3$ . FT is on the last two brackets (not $(x - 3)$ ). If incorrect factor or factors in (b) but correct regions here, allow SC B1 only.
		2	

<b>Question</b>	<b>Answer</b>	<b>Marks</b>	<b>Guidance</b>
10(a)	State or imply the form $\frac{A}{(1+x)} + \frac{Bx+C}{(4+x^2)}$	<b>B1</b>	
	Use a correct method for finding a constant Even with incorrect PF denominators	<b>M1</b>	$A(4+x^2) + (Bx+C)(1+x) = -7x^2 + 2x - 6$
	Obtain one of $A = -3$ , $B = -4$ and $C = 6$	<b>A1</b>	
	Obtain a second value	<b>A1</b>	
	Obtain a third value	<b>A1</b>	
			<b>Special Case 1:</b> $\frac{A}{(1+x)} + \frac{C}{(4+x^2)} +$ Find $A$ , <b>M1 A1.</b> Max 2/5. <b>Special Case 2:</b> $\frac{A}{(1+x)} + \frac{Bx}{(4+x^2)} +$ Find $A$ , <b>M1 A1.</b> Max 2/5.
		<b>5</b>	

Question	Answer	Marks	Guidance
10(b)	Obtain term $-3\ln(1+x)$	<b>B1 FT</b>	OE FT $A \ln(1+x)$
	Obtain term $-2\ln(4+x^2)$	<b>B1 FT</b>	OE FT $\frac{B}{2} \ln(4+x^2)$
	Obtain integral of the form $c \tan^{-1} dx$ with $d \neq 1$ following separation into two expressions	<b>M1</b>	$d = \frac{1}{2}$ or 2 only.
	Obtain $3\tan^{-1}\frac{x}{2}$	<b>A1 FT</b>	FT $\frac{C}{2} \tan^{-1}\frac{x}{2}$
	Substitute correct limits correctly in an expression (obtained correctly) of the form $a \ln(1+x)$ , $b \ln(4+x^2)$ , and $c \tan^{-1}\left(\frac{1}{2}x\right)$ , where $a, b, c \neq 0$ .	<b>M1</b>	$a \ln(3) + b \ln(8) - b \ln(4) + c\left(\frac{1}{4}\pi\right)$ , where $a, b, c \neq 0$ . Do not allow slips, and must get to $c\left(\frac{1}{4}\pi\right)$ .
	Obtain answer $\frac{3}{4}\pi - \ln 108$	<b>A1</b>	Must be in the form $a\pi - \ln b$ .
		<b>6</b>	

Question	Answer	Marks	Guidance
11	Commence integration by parts and reach $Ax^2 \sin \frac{1}{3}x \pm \int Bx \sin \frac{1}{3}x dx$	*M1	OE BOD on $\pm$ otherwise scores 0/6.
	Obtain $3x^2 \sin \frac{1}{3}x - \int 6x \sin \frac{1}{3}x dx$	A1	OE Allow $3 \times 2$ for 6.
	Complete integration by parts and reach $Ax^2 \sin \frac{1}{3}x + Bx \cos \frac{1}{3}x + C \sin \frac{1}{3}x$	*DM1	OE
	Obtain $3x^2 \sin \frac{1}{3}x + 18x \cos \frac{1}{3}x - 54 \sin \frac{1}{3}x$ oe	A1	Allow $6 \times 3$ for 18, $9 \times 6$ for 54 OE.
	Substitute limits correctly in an expression of the form $Ax^2 \sin \frac{1}{3}x + Bx \cos \frac{1}{3}x + C \sin \frac{1}{3}x$ , where $ABC \neq 0$	DM1	Dependent on both previous M1 marks. Need to use $\sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}$ , and $\cos \frac{\pi}{3} = \frac{1}{2}$ to obtain $A\pi^2 \frac{\sqrt{3}}{2} + \frac{B\pi}{2} + \frac{C\sqrt{3}}{2}$ .
	Obtain answer $\frac{3\sqrt{3}}{2}\pi^2 + 9\pi - 27\sqrt{3}$ or exact equivalent ISW	A1	Allow $\frac{\sqrt{27}}{2}$ for $\frac{3\sqrt{3}}{2}$ , $\frac{18}{2}$ for 9, $\frac{54}{2}$ for 27, $\sqrt{2187}$ for $27\sqrt{3}$ etc.
	<b>Alternative Method for first 4 marks:</b>		
	Commence integration by parts and reach $Ax^2 \sin \frac{1}{3}x + Bx \cos \frac{1}{3}x$	*M1	
	Obtain $3x^2 \sin \frac{1}{3}x + 18x \cos \frac{1}{3}x$	A1	OE Allow $6 \times 3$ for 18.
	Complete integration by parts and reach $Ax^2 \sin \frac{1}{3}x + Bx \cos \frac{1}{3}x + C \sin \frac{1}{3}x$	*DM1	

Question	Answer	Marks	Guidance
11	Obtain $3x^2 \sin \frac{1}{3}x + 18x \cos \frac{1}{3}x - 54 \sin \frac{1}{3}x$	A1	OE Allow $6 \times 3$ for 18, $9 \times 6$ for 54, OE.
		6	