

1) 2 Dices

Probability Assignment

<u>D1</u>	<u>D2</u>				
<u>(1,1)</u>	<u>(1,2)</u>	<u>(1,3)</u>	<u>(1,4)</u>	<u>(1,5)</u>	<u>(1,6)</u>
<u>(2,1)</u>	<u>(2,2)</u>	<u>(2,3)</u>	<u>(2,4)</u>	<u>(2,5)</u>	<u>(2,6)</u>
<u>(3,1)</u>	<u>(3,2)</u>	<u>(3,3)</u>	<u>(3,4)</u>	<u>(3,5)</u>	<u>(3,6)</u>
<u>(4,1)</u>	<u>(4,2)</u>	<u>(4,3)</u>	<u>(4,4)</u>	<u>(4,5)</u>	<u>(4,6)</u>
<u>(5,1)</u>	<u>(5,2)</u>	<u>(5,3)</u>	<u>(5,4)</u>	<u>(5,5)</u>	<u>(5,6)</u>
<u>(6,1)</u>	<u>(6,2)</u>	<u>(6,3)</u>	<u>(6,4)</u>	<u>(6,5)</u>	<u>(6,6)</u>

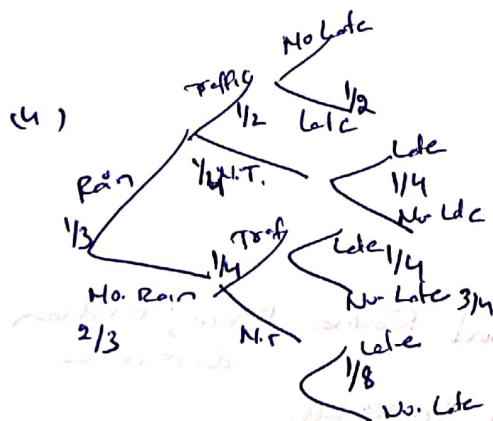
Sum of No. being even and one die shows 6
 Total outcomes = 36
 Even + Atleast one 6 = 5 $\Rightarrow 5/36$

(2) Sum of No. less than 7
 = 15/36

(3) Coin - 3 times = (H, H, H), (H, T, H), (H, T, T), (T, H, H), (T, T, H), (T, T, T), (T, H, T), (H, H, T)
 Atleast one head = $1 - \frac{1}{8} = 7/8$

Atleast two heads = $4/8$

$$P(\text{Atleast one head}) = \frac{4/8}{7/8} = 4/7$$



(a) Not Rain + heavy traffic + No Late

$$\Rightarrow \frac{2}{3} \times \frac{1}{4} \times \frac{3}{4} = \frac{1}{8}$$

(b) Greatly Late

$$\begin{aligned} \Rightarrow & \frac{1}{3} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{3} \times \frac{1}{2} \times \frac{1}{4} + \frac{2}{3} \times \frac{1}{4} \times \frac{1}{4} \\ & + \frac{2}{3} \times \frac{3}{4} \times \frac{1}{8} \\ = & \frac{1}{12} + \frac{1}{24} + \frac{1}{24} + \frac{1}{16} = \frac{4+2+2+3}{48} = \frac{11}{48} \end{aligned}$$

(17) Late if it rained

$$\Rightarrow \text{Late} = 1/48 \text{ (from b)}$$

$$\begin{aligned} \text{Rain \& Late} &= \frac{1}{3} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{3} \times \frac{1}{2} \times \frac{1}{4} \\ &= \frac{1}{12} + \frac{1}{24} = \frac{2+1}{24} = \frac{3}{24} = \frac{1}{8} \end{aligned}$$

2	12, 24
2	6, 12
3	3, 6
2	1, 2
1	1

(15) 3 Coins

2 Good + 1 Fake \Rightarrow

(a) Always head =

Coin 1 = $1/2$, Coin 2 = $1/2$, Coin 3 = 1 (only head)

$$\begin{aligned} P(H) &= \frac{1}{2} \times (1 - 1/3) + 1 \times \frac{1}{3} \\ &= \frac{1}{2} \times \frac{2}{3} + \frac{1}{3} = \frac{2}{3} \end{aligned}$$

only two are valid tosses
So remove 1 from 3
tosses = $2/3$ is
valid.

$$\begin{aligned} \text{(b) } P(H/\text{coin 2}) &= \frac{1 \times \frac{1}{3}}{\frac{1}{2} \times \frac{2}{3} + \frac{1}{2} \times \frac{2}{3}} = \frac{\frac{1}{3}}{\frac{1}{3} + \frac{1}{3}} = \frac{\frac{1}{3}}{\frac{2}{3}} \\ &= \frac{1}{2} \end{aligned}$$

$$\text{(6) } \text{Coffee} = \frac{70}{100} = 0.7$$

$$\text{Cake} = \frac{40}{100} = 0.4$$

$$\text{Both} = \frac{20}{100} = 0.2$$

$$P(\text{Coffee}) = \frac{\text{Both}}{\text{Cake}} = \frac{0.2}{0.4} = \frac{1}{2}$$

(7), (8), (9), (10) \rightarrow Need to check and Review mean, median & mode
Need to verify.

11) 8 black, 1 white
Total 9 balls

$$P(b) = \frac{8}{9}, P(w) = \frac{1}{9}$$

$$P(T) = \frac{5}{6}$$

$$P(\text{Truth} / \text{not white}) = 1 - \frac{5}{6} = \frac{1}{6}$$

$$P(\text{White} \& \text{Truth}) = \frac{\frac{5}{6} \times \frac{1}{9}}{\frac{5}{6} \times \frac{1}{9} + \frac{1}{6} \times \frac{8}{9}} \\ = \frac{5}{13}$$

$$(12) P(T) = \frac{4}{5}$$

$$P(6) = \frac{1}{6}$$

$$P(T / \text{Not } 6) = \frac{1}{5}$$

$$P(6/T) = \frac{\frac{1}{6} \times \frac{4}{5}}{\frac{1}{6} \times \frac{4}{5} + \frac{5}{6} \times \frac{1}{5}} \\ = \frac{4}{9}$$