

assign7_1_prob_classification

May 31, 2019

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In [1]: import numpy as np
        np.random.seed(1)

        import matplotlib.pyplot as plt
        %matplotlib inline

In [2]: def generate_data(sample_size=90, n_class=3):
        x = (np.random.normal(size=(sample_size // n_class, n_class))
              + np.linspace(-3., 3., n_class)).flatten()
        y = np.broadcast_to(np.arange(n_class),
                              (sample_size // n_class, n_class)).flatten()

        return x, y

        x, y = generate_data()

In [3]: # 各クラスのサンプル、サンプル数
        n = len(x)
        cs = np.unique(y)
        n_class = len(cs)

        indices_cs = [np.where(y==c) for c in cs]
        x_cs = [x[indices_c] for indices_c in indices_cs]
        n_cs = [len(x_c) for x_c in x_cs]

In [4]: # 各クラスの計画行列
        def calc_design_matrix(x, c, h=1):
            return np.exp(-(x[None] - c[:, None]) ** 2 / (2 * h ** 2))

        ks = [calc_design_matrix(x_c, x) for x_c in x_cs]

In [5]: # 各クラスの one_hot ベクター
        def one_hot(indices_c):
            zeros = np.zeros(n, dtype=np.float32)
            zeros[indices_c] = 1
            return zeros

        pis = [one_hot(indices_c) for indices_c in indices_cs]

In [6]: # 最小二乗法によるパラメータ推定
        l = 0.01
        thetas = [np.linalg.inv(k.T.dot(k) + l * np.eye(n_c)).dot(k.T).dot(pi) for k, n_c, pi in zip(ks, n_cs, pis)]

In [7]: # 確率分布可視化用サンプル
        x_vis = np.linspace(start=-5, stop=5, num=1000)
        ks_vis = [calc_design_matrix(x_c, x_vis) for x_c in x_cs]
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In [8]: # 各クラスの確率分布
ls_vis = np.maximum([k_vis.dot(theta) for k_vis, theta in zip(ks_vis, thetas)], 0)
ps_vis = ls_vis / np.sum(ls_vis, 0)
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In [9]: # 可視化
plt.scatter(x_cs[0], np.zeros(n_cs[0]))
plt.scatter(x_cs[1], np.zeros(n_cs[1]))
plt.scatter(x_cs[2], np.zeros(n_cs[2]))
plt.plot(x_vis, ps_vis[0])
plt.plot(x_vis, ps_vis[1])
plt.plot(x_vis, ps_vis[2])
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Out[9]: [<matplotlib.lines.Line2D at 0x7f0e4817e550>]
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