TAD Graph

Graph = (V, A)

\forall (u, v, w) \in A: (u \in V) \land (v \in V) \land (w \gt 0)

	Primitive Opera	ations	
Operation	Input	Input	Туре
addNode	Node	Void	Modifier
addEdge	Edge	void	Modifier
getNodes	_	List	Observer
getEdgesFrom	Node	List	Observer
getNeighbors	Node	List	Observer
getEdgeWeight	Node s, Node d	double	Observer

⟨addNode(Graph, Node)⟩

⟨Adds a new node to the graph⟩

Precondition: ⟨node ≠ null ∧ node ∉ V⟩

Postcondition: $\langle node \in V \land adjacencyList[node] = [] \rangle$

⟨addEdge(Graph, Edge)⟩

⟨Adds an edge between two nodes⟩

Precondition: $\langle edge \neq null \land edge.source \in V \land edge.destination \in V \land edge.weight > 0 \rangle$

Postcondition: $\langle edge \in A \land edge \in adjacencyList[edge.source] \rangle$

⟨addEdge(Grafo, T, T, int)⟩

〈Adds a new edge with weight between two vertices〉

{pre: $\langle u \in V \land v \in V \land w > 0 \rangle$ }

{post: $\langle \text{isDirected} \Rightarrow (u, v, w) \in A \ V \neg \text{isDirected} \Rightarrow (u, v, w) \in A \land (v, u, w) \in A \rangle$ }

⟨getNodes(Graph)⟩

 \langle Returns all nodes in the graph \rangle

Precondition: —

Postcondition: returns V>

⟨getEdgesFrom(Graph, Node)⟩

⟨Returns all edges starting from the given node⟩

Precondition: $\langle node \in V \rangle$

Postcondition: $\langle \text{returns A'} \subseteq A \text{ where } \forall e \in A' : e.source = node \rangle$

⟨getNeighbors(Graph, Node)⟩

⟨Returns all neighbors (adjacent nodes) of a given node⟩

Precondition: $\langle node \in V \rangle$

Postcondition: $\langle \text{returns list of nodes such that } \exists \text{ edge} \in A : \text{edge.source} = \text{node } \land \text{ edge.destination} \in \text{list} \rangle$

⟨getEdgeWeight(Graph, Node, Node)⟩

⟨Returns the weight of the edge from source to destination⟩

Precondition: $\langle \exists \text{ edge} \in A : \text{edge.source} = \text{source} \land \text{edge.destination} = \text{destination} \rangle$

Postcondition: ⟨returns edge.weight if found, otherwise ∞⟩

TAD AdjacencyMatrix

AdjacencyMatrix = (V, A, M)

 $\forall \ i,j \in [0,\mathsf{SIZE}): (i=j \Rightarrow \mathsf{M}[i][j] = 0) \ \land \ (i \neq j \Rightarrow \ (\exists \ \mathsf{w} \in \mathbb{N}^+ : \mathsf{edge}(i,j,\mathsf{w}) \in \mathsf{A} \Rightarrow \mathsf{M}[i][j] = \mathsf{w}) \ \lor \ (\neg \exists \ \mathsf{edge}(i,j,\mathsf{w}) \in \mathsf{A} \Rightarrow \mathsf{M}[i][j] = \infty))$

Primitive Operations

Operation	Input	Input	Туре
addNode	Node	Void	Modifier
addEdge	Edge	void	Modifier
getNodes	_	List	Observer
clear	_	void	Modifier
getNeighbors	Node	List	Observer
getEdgeWeight	Node s, Node d	double	Observer
getNodeIndex	Node	int	Observer

⟨addNode(AdjacencyMatrix, Node)⟩

Adds a new node to the graph if it doesn't already exist and there is space

Precondition: node \neq null \land node \notin V \land |V| < SIZE

Postcondition: node ∈ V

⟨addEdge(AdjacencyMatrix, Edge)⟩

Adds a new edge between two registered nodes, with direction or bidirection depending on the edge

Precondition: edge \neq null \land edge.source \in V \land edge.destination \in V \land edge.weight > 0

Postcondition: $M[i][j] \leftarrow w \land \neg edge.isDirected() \Rightarrow M[j][i] \leftarrow w$

⟨getNodes(AdjacencyMatrix)⟩

Returns the list of all registered nodes

Precondition: —

Postcondition: returns V

⟨getNeighbors(AdjacencyMatrix, Node)⟩

Returns the list of adjacent nodes of the given node

Precondition: node $\in V$

Postcondition: returns L = { nodes[j] \in V | M[i][j] $\neq \infty \land$ M[i][j] $\neq 0$ }

⟨getEdgeWeight(AdjacencyMatrix, Node u, Node v)⟩

Returns the weight of the edge between two nodes

Precondition: $u \in V \land v \in V$

Postcondition: $(M[i][j] \neq \infty \Rightarrow \text{returns } M[i][j]) \land (M[i][j] = \infty \Rightarrow \text{returns } \infty)$

$$\label{eq:clear} \begin{split} & \langle \mathsf{clear}(\mathsf{AdjacencyMatrix}) \rangle \\ & \qquad \qquad \mathsf{Clears} \; \mathsf{all} \; \mathsf{nodes} \; \mathsf{and} \; \mathsf{resets} \; \mathsf{the} \; \mathsf{matrix} \\ & \qquad \qquad \mathsf{Precondition:} \; - \\ & \qquad \qquad \mathsf{Postcondition:} \; \mathsf{V} = \emptyset \; \land \; \forall \; \mathsf{i}, \mathsf{j} \in [\mathsf{0}, \; \mathsf{SIZE}) \text{:} \; (\mathsf{i} = \mathsf{j} \Rightarrow \mathsf{M}[\mathsf{i}][\mathsf{j}] = \mathsf{0}) \; \land \; (\mathsf{i} \neq \mathsf{j} \Rightarrow \mathsf{M}[\mathsf{i}][\mathsf{j}] = \infty) \end{split}$$

TAD Edge

Edge = (source, destination, weight, isDirected)

source ≠ null ∧ destination ≠ null ∧ weight > 0

	Primitive (Operations	
Operation	Input	Input	Туре
getSource	_	Node	Observer
getDestination	_	Node	Observer
getWeight	_	int	Observer
isDirected	_	boolean	Observer

〈getSource(Edge)〉
Returns the source node of the edge
Precondition: —
Postcondition: returns source ∈ Node

\(\square\text{getDestination(Edge)}\) Returns the destination node of the edge Precondition: — Postcondition: returns destination ∈ Node

\(\lambda \text{isDirected(Edge)} \) Returns the list of adjacent nodes of the given node Precondition: node ∈ V Postcondition: returns true \(\Lambda \) the edge is directed (source \(\rightarrow \) destination)

TAD Node

Node = (id, x, y, isWalkable, isHacked)

id≠null∧x∈R∧y∈R∧isWalkable∈B∧isHacked∈B

Opreaciones Primitivas: Operación Salida **Entrada** Tipo getId String Observer getX double Observer getY double Observer isWalkable boolean Observer isHacked boolean Observer setHacked void Modifier boolean equals Object boolean Observer hashCode int Observer

〈getId(Node)〉	
Returns the identifier of the node	
Precondition: —	
Postcondition: returns id ∈ String ∧ id ≠ null	

〈getX(Node)〉	
Returns the x-coordinate	
Precondition: —	
Postcondition: returns $x \in \mathbb{R}$	

〈getY(Node)〉
Returns the y-coordinate
.Precondition: —
Postcondition: returns $y \in \mathbb{R}$

⟨isWalkable(Node)⟩
Returns whether the node is walkable
Precondition: —
Postcondition: returns isWalkable $\in \mathbb{B}$

〈isHacked(Node)〉
Returns whether the node has been hacked
.Precondition: —
Postcondition: returns is Hacked $\in \mathbb{B}$

〈setHacked(Node, boolean)〉
Sets the hacked status of the node
Precondition: hacked $\in \mathbb{B}$
Postcondition: isHacked = hacked

⟨equals(Node, Object)⟩
Compares two nodes by id
.Precondition: o ≠ null
Postcondition: returns true ⇔ this.id = o.id

〈hashCode(Node)〉
Returns a hash code based on id
Precondition: —
Postcondition: returns hash(id)

TAD PathFinder

PathFinder = (dijkstraPath, bfsPath, reconstructPath)

∀ method ∈ {dijkstraPath, bfsPath}: startNode ≠ null ∧ endNode ≠ null ∧ startNode ∈ V ∧ endNode ∈ V

Opreaciones Primitivas:

Operación	Entrada	Salida	Tipo
	Graph, Node start, Node		
dijkstraPath	end	List	Analizadora
	Graph, Node start, Node		
bfsPath	end	List	Analizadora
	Map <node, node="">, Node</node,>		
reconstructPath	end	List	Auxiliar

⟨dijkstraPath(PathFinder, Graph, Node start, Node end)⟩

Finds the shortest path from start to end using Dijkstra's algorithm

Precondition: start \neq null \land end \neq null \land start \in V \land end \in V

Postcondition:(path ≠ Ø ∧ path[0] = start ∧ path[|path|-1] = end ∧ ∀ alternativePath: validPath(start, end) ⇒ totalWeight(path) ≤totalWeight(alternativePath)) ∨ (path = Ø ∧ no path exists from start to end)

\langle bfsPath(PathFinder, Graph, Node start, Node end) \rangle Finds a path from start to end using Breadth-First Search Precondition: start \neq null \wedge end \neq null \wedge start \in V \wedge end \in V

Postcondition:(path ≠ Ø ∧ path[0] = start ∧ path[|path|-1] = end ∧ path contains the minimal number of edges between start and end)V (path = Ø ∧ no path exists from start to end)

⟨reconstructPath(PathFinder, Map<Node, Node> cameFrom, Node end)⟩

Reconstructs a path from the end node by following the cameFrom map

Precondition: end ∈ domain(cameFrom) ∨ end = null

Postcondition: $\forall i \in [1, |path|-1]$: cameFrom(path[i]) = path[i-1] \land path[|path|-1] = end