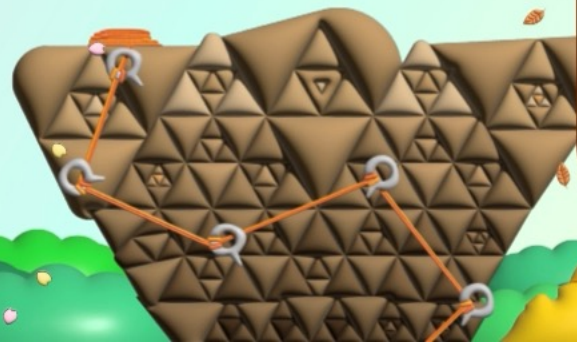


# 파이썬으로 배우는 데이터 구조



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# 학습 목표

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제자리(In-Place) 연산이 가능하게 하는  
메소드를 정의할 수 있다

# Data Structures in Python

## Chapter 1 - 2

- Object-Oriented Programming
- OOP in Python
- OOP - Fraction Example
- OOP - Classes
- **OOP - In-Place Operators**
- Exceptions
- Exception Clauses

# Agenda

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- Classes
  - Overloading Operators
  - `__add__`, `__sub__`, `__eq__`
  - GCD
  - `__lt__`
- In-Place Operations
  - `__mul__`, `__rmul__`, `__imul__`
- References:
  - [Problem Solving with Algorithms and Data Structures using Python](#)
    - Chapter 1.13 Object-Oriented Programming in Python
    - [Chapter 2.2 A Proper Class](#)

## Forward, Reverse and In-Place

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- Every arithmetic operator is transformed into a method call. By defining **the numeric special methods**, your class will work with the built-in arithmetic operators.
  - First, there are as many as **three** variant methods required to implement each operation.
    - For example, `*` is implemented by `__mul__`, `__rmul__` and `__imul__`
    - There are forward and reverse special methods so that you can assure that your operator is properly commutative.
    - You don't need to implement all three versions.
    - The reverse name is used for special situations that involve objects of multiple classes.

## mul vs. rmul

- Locating an appropriate method for an operator
  - First, it tries a class based on the left operand using the "forward" name. If no suitable special method is found, it tries the right-hand operand, using the "reverse" name.
- **Sample Run and Version 1:**

```
x = Fraction(2,3)
```

```
y = Fraction(1,3)
```

```
p = x * y
```

```
print(p)
```

Invoke x.\_\_mul\_\_(y)

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```
p = x * 2
```

```
print(p)
```

AttributeError:  
'int' object has  
no attribute 'num'

```
class Fraction:
```

```
...
```

```
    def __mul__(self, other):
```

```
        num = self.num * other.num
```

```
        den = self.den * other.den
```

```
        return Fraction(num, den)
```

## mul vs. rmul

- Locating an appropriate method for an operator
  - First, it tries a class based on the left operand using the "forward" name. If no suitable special method is found, it tries the right-hand operand, using the "reverse" name.
- **Sample Run and Version 2:**

```
x = Fraction(2,3)
```

```
y = Fraction(1,3)
```

```
p = x * y
```

```
print(p)
```

Invoke x.\_\_mul\_\_(y)

2/9

```
p = x * 2
```

```
print(p)
```

Invoke x.\_\_mul\_\_(y)

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Version 2 checks the type of the right operand:

```
class Fraction:
```

```
...
```

```
    def __mul__(self, other):
```

```
        if isinstance(other, Fraction):
```

```
            num = self.num * other.num
```

```
            den = self.den * other.den
```

```
            return Fraction(num, den)
```

```
        else:
```

```
            num = self.num * other
```

```
            return Fraction(num, self.den)
```

If the right operand is not a Fraction

## mul vs. rmul

- Locating an appropriate method for an operator
  - First, it tries a class based on the left operand using the "forward" name. If no suitable special method is found, it tries the right-hand operand, using the "reverse" name.
- **Sample Run and Version 2:**

```
x = Fraction(2,3)
y = Fraction(1,3)
p = x * y
print(p)
```

Invoke x.\_\_mul\_\_(y)

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```
p = x * 2
print(p)
```

Invoke x.\_\_mul\_\_(y)

4/3

```
p = 2 * x
print(p)
```

TypeError: unsupported operand type(s) for \*: 'int' and 'Fraction'

Version 2 checks the type of the right operand:

```
class Fraction:
...
    def __mul__(self, other):
        if isinstance(other, Fraction):
            num = self.num * other.num
            den = self.den * other.den
            return Fraction(num, den)
        else:
            num = self.num * other
            return Fraction(num, self.den)
```

If the right operand is not a Fraction



## mul vs. rmul

- Locating an appropriate method for an operator
  - First, it tries a class based on the left operand using the "forward" name. If no suitable special method is found, it tries the right-hand operand, using the "reverse" name.
- **Sample Run and Version 3:**

```
x = Fraction(2,3)
```

```
y = Fraction(1,3)
```

```
p = x * y
```

```
print(p)
```

Invoke x.\_\_mul\_\_(y)

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```
p = x * 2
```

```
print(p)
```

Invoke x.\_\_mul\_\_(y)

4/3

```
p = 2 * x
```

```
print(p)
```

TypeError: unsupported operand type(s) for \*: 'int' and 'Fraction'

If the left operand of \* is a primitive type and the right operand is a Fraction, Python invokes **\_\_rmul\_\_**

```
class Fraction:
```

```
...
```

```
def __mul__(self, other):
```

```
    if isinstance(other, Fraction):
```

```
        num = self.num * other.num
```

```
        den = self.den * other.den
```

```
        return Fraction(num, den)
```

```
    else:
```

```
        num = self.num * other
```

```
        return Fraction(num, self.den)
```

## mul vs. rmul

- Locating an appropriate method for an operator
  - First, it tries a class based on the left operand using the "forward" name. If no suitable special method is found, it tries the right-hand operand, using the "reverse" name.
- **Sample Run and Version 3:**

<code>x = Fraction(2,3)</code>	
<code>y = Fraction(1,3)</code>	
<code>p = x * y</code>	Invoke x.__mul__(y)
<code>print(p)</code>	2/9
<code>p = x * 2</code>	Invoke x.__mul__(y)
<code>print(p)</code>	4/3
<code>p = 2 * x</code>	Invoke x.__rmul__(2)
<code>print(p)</code>	4/3

If the left operand of \* is a primitive type and the right operand is a Fraction, Python invokes **\_\_rmul\_\_**

```
class Fraction:
...
    def __mul__(self, other):
        if isinstance(other, Fraction):
            num = self.num * other.num
            den = self.den * other.den
            return Fraction(num, den)
        else:
            num = self.num * other
            return Fraction(num, self.den)

    def __rmul__(self, other):
        num = self.num * other
        return Fraction(num, self.den)
```

# In-Place Operators

- `+=`, `-=`, `*=`, `/=` etc
- Sample Run:

```
x = Fraction(2,3)
y = Fraction(1,3)
print(id(x))
x += y
print(id(x))
print(x)
```

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Invoke `x.__iadd__(y)`

- Code:

```
class Fraction:
    ...
    def __iadd__(self, other):
        num = self.num * other.den + self.den * other.num
        den = self.den * other.den
        gcd = Fraction.gcd(num, den)
        self.num = num // gcd
        self.den = den // gcd
        return self
```

Do the calculation in-place

## Exercise 4

- Overload the following operators in the `Point` class:
  - `+`: returns a new `Point` that contains the sum of x's and the sum of y's, respectively.
  - `*`: computes the **dot product** of the two points, defined according to the rules of linear algebra.
- Sample Run:

```
p1 = Point(3, 4)
p2 = Point(5, 7)
p3 = p1 + p2
print(p3)

print(p1 * p2)
```

Point(8, 11)

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$= 3*5 + 4*7 = 15 + 28$

## Exercise 5

- If the left operand of `*` or `+` is a primitive type and the right operand is a `Point`, Python invokes `__rmul__` and `__radd__`.
- Let them perform scalar multiplication and addition, respectively in your code.
- Sample Run:

```
p1 = Point(3, 4)
p2 = Point(5, 7)
p5 = 2 * p1
print(p5)           Point(6, 8)

p6 = p2 * 2
print(p6)           Point(10, 14)

print(2 + p1)        Point(5, 6)
print(p1 + 2)        Point(7, 9)
```

## Exercise 6

- Overload the following operators in the `Circle` class:
  - `+`: returns a new `Circle` that contains the sum of two radii.
  - `*`: computes a new `Circle` that contains the multiplication of two radii.
  - If the left operand of `*` or `+` is a primitive type and the right operand is a `Circle`, Python invokes `__rmul__` and `__radd__`. Let them perform scalar multiplication and addition, respectively in your code.
- Sample Run:

```
c1 = Circle(2)
c2 = Circle(3)
print(c1 + c2)
print(c1 * c2)

print(c1 * 2)
print(2 * c2)

print(3 + c1)
print(c2 + 3)
```

Circle(5)
Circle(6)

Circle(4)
Circle(6)

Circle(5)
Circle(6)

## Summary

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- We can **override(재정의)** the **default methods** in a class definition.

# 학습 정리

- 1) `__rmul__()`, `__radd__()` 같은 특별한 메소드는 피연산자의 타입이 서로 맞지 않을 때 순서를 바꾸어 계산할 수 있도록 돕는다
- 2) 제자리(In-Place) 연산자는 객체의 reference가 바뀌지 않으므로 `self`를 반환해야 한다



# 파이썬으로 배우는 데이터 구조

수고했습니다  
곧 다음 시간에  
다시 뵙겠습니다

