

Merge Sort

Mergesort needs to be implemented using recursion. First, divide the N-sized array in half. Then, two N/2 arrays are created when the original array is divided once. The next split produces four N/4 arrays. And it goes on like this when array size increases. This means that the segmentation process is reduced by half each time, so we have to repeat $\log N$ to divide into a one-size array.

In our case, merging left = $T(N/2)$ and merging right = $T(N/2)$. And, merge them together $O(N)$. Basically, we split the array in half continuously with variables such as start, mid, and end. Using a while loop, we compare the values of the array of each position to swap using $a[i] > a[j]$, and increase the value of the i and j according to the conditions. So, it is converted to

$$\begin{aligned} T(n) &= 2 \times T(n/2) + O(n) = 2(2T(n/4) + O(n/2)) + O(n) = 4T(n/4) + 2O(n) = \dots \\ &= n \times T(1) + \log n \times O(n) = n \times O(1) + O(n \log n) = O(n) + O(n \log n) = O(n \log n) \end{aligned}$$

Therefore, it has a time complexity of $O(N \log N)$.

Quicksort

We implemented quicksort recursively with partitioning. First, we first pick an element as pivot $O(1)$ and classify small, equal, and large values compare with pivot value $O(n)$. Then, quicksort each case.

If a left variable is smaller than the pivot value, then increase its index (i). If the right variable is larger than the pivot value, then decrease its index (j).

If $left \leq right$, swap them using while loop. Then, increase the left variable and decrease the right variable. Repeat this process until sorting complete.

Hence, $T(n) = T(left) + T(right) + O(n)$.

// left = number of elements less than or equal to the pivot

// right = number of elements larger than or equal to the pivot.

Suppose the pivot divides the number of elements in half. If so, it shows that $T(n) = 2T(n/2) + O(n)$. Consequently, the average time complexity is converted to $T(n) = O(n \log n)$ and the worst is $O(n^2)$.

Gold's Poresort

First, we compare all even-indexed cells to their next neighbor cell, and then compare all odd-indexed cells to their next neighbor cell. We implemented this algorithm using variable "status" to distinguish whether it is checking even-indexed cells or odd-indexed cells. When it's swapping even-indexed cells, the status is equal to 0 $O(1)$. When it's over, the status changes to 1 $O(1)$. Then, it starts to swap odd-indexed slots. And, when it's over, the status changes to 0 again. Repeat this process until sorting is complete. We have for loop that increases the $i=0$ to array length N $O(N)$. And, there are two for loops that comparing even-indexed cells or odd-indexed cells increasing by two.

Therefore, there are $(N/2)$ passes, so $T(N) = N * (N/2) = N^2$. Consequently, the time complexity is converted to $O(N^2)$.