

Limitations

For the API-based models used in RECONCILE, we note that we lack complete knowledge of the data that these models have been exposed to, and their scales in terms of parameters. Moreover, due to the API access, we do not possess complete control over their behavior. Depending on API-based models also necessitates the need to prompt these models to estimate their confidence. While this approach proves effective as evidenced by our results, we note that these estimates remain post-hoc in nature. Nevertheless, it is worth highlighting that these limitations could potentially be mitigated in the future should more open-sourced models emerge and demonstrate robust capabilities in adhering to long instructions.

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