

LFTF: Locating First and Then Fine-Tuning for Mitigating Gender Bias in Large Language Models

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Abstract

Nowadays, Large Language Models (LLMs) have attracted widespread attention due to their powerful performance. However, due to the unavoidable exposure to socially biased data during training, LLMs tend to exhibit social biases, particularly gender bias. To better explore and quantifying the degree of gender bias in LLMs, we propose a pair of datasets named GenBiasEval and GenHintEval, respectively. The GenBiasEval is responsible for evaluating the degree of gender bias in LLMs, accompanied by an evaluation metric named AFGB-Score (**Absolutely Fair Gender Bias Score**). Meanwhile, the GenHintEval is used to assess whether LLMs can provide responses consistent with prompts that contain gender hints, along with the accompanying evaluation metric UB-Score (**UnBias Score**). Besides, in order to mitigate gender bias in LLMs more effectively, we present the LFTF (**Locating First and Then Fine-Tuning**) algorithm. The algorithm first ranks specific LLM blocks by their relevance to gender bias in descending order using a metric called BMI (**Block Mitigating Importance Score**). Based on this ranking, the block most strongly associated with gender bias is then fine-tuned using a carefully designed loss function. Numerous experiments have shown that our proposed LFTF algorithm can significantly mitigate gender bias in LLMs while maintaining their general capabilities.

1 Introduction

In recent years, large language models (LLMs) have emerged and been successfully applied in numerous downstream tasks (OpenAI et al., 2024; The; Dubey et al., 2024) and various applications (Chang et al., 2024; Kaddour et al., 2023; Wang et al., 2024a; Mahowald et al., 2024), thanks to continuous advancements in hardware infrastructure, model algorithms, and the vast amounts of high-quality data.

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However, LLMs are trained on vast corpora and, as a result, inevitably absorb information that contains social biases, leading to the encoding of negative stereotypes and biased patterns within models (Gallegos et al., 2024). Social biases include gender bias, age bias, religious bias, and others, with gender bias in relation to profession being the most severe (Dong et al., 2024; You et al., 2024; Kumar et al., 2024; Dwivedi et al., 2023; Rhue et al., 2024). For example, when the prompt “The lifeguard laughed because” is input into the Llama-2-7b (Touvron et al., 2023), the probability of predicting “he” as the next token is 26.12%, while the probability of predicting “she” is 12.34%. This indicates that the Llama-2-7b model exhibits a gender bias, associating the profession of “lifeguard” more strongly with “male” (Lemisiewicz et al., 2024).

To address gender bias in LLMs, research focuses on developing fair systems through three main categories of debiasing methods, distinguished by the model training stage at which they are applied. First, pre-processing methods aim to reduce bias in the original dataset using techniques such as data augmentation and data cleansing. However, these methods face limitations as inherent biases present in real-world data can be difficult to completely eliminate (Gokhale et al., 2020; Chen et al., 2020; Zmigrod et al., 2019; Dinan et al., 2019; Qian et al., 2022; Kolling et al., 2022; Bolukbasi et al., 2016; Selbst et al., 2019). Second, in-training debiasing methods intervene in the model’s learning process. This can involve modifying model architectures or altering loss functions. The main drawbacks are the substantial computational resources often required and the risk of model degradation or even collapse (Huang et al., 2022; Lin et al., 2022; Lemisiewicz et al., 2024; Liu et al., 2019; Yu et al., 2023; Park et al., 2023; Zhou et al., 2023; Wu and Popyan, 2024; Yang et al., 2024). Third, post-training debiasing meth-

ods adjust model outputs to mitigate biases without needing to re-optimize model weights or alter training data. While techniques like prompt engineering can reduce social biases in the output, they may not address the more deeply ingrained biases within the model itself (Wang et al., 2021; He et al., 2021; Majumder et al., 2022; Huang et al., 2023a).

To better assess and mitigate the extent of gender bias related to professions in LLMs, we have made the following efforts in this paper:

First, we propose a dataset named GenBiasEval, which is used to evaluate the degree of gender bias in LLMs. We believe that true gender debiasing should achieve absolute equality between “male” and “female”, so we propose the evaluation metric named AFGB-Score, which is based on the difference between the gender words in the probability distribution of the next token generated by LLMs.

Second, we propose another dataset named GenHintEval, which is used to assess whether LLMs can provide correct responses when faced with prompts containing gender hints. Correspondingly, we design the evaluation metric called UB-Score to measure the extend of gender bias. UB-Score is based on the probability distribution of the next token like GenBiasEval and further involves a weight factor to model the consistency between generated responses and gender hints present in the received input prompts.

Third, we propose a debiasing algorithm named LFTF. We agree with the view that LLMs are modular, meaning that specific parameters within them are responsible for completing particular tasks (Yu et al., 2023; Qin et al., 2024). Therefore, we reasonably hypothesize that there are parameters in LLMs that are most closely related to gender bias. We apply the LFTF algorithm to various LLMs, and the experimental results indicate that our proposed method can effectively reduce gender bias in LLMs while maintaining LLMs’ general capabilities.

The primary contributions of this work can be summarized as follows:

- We propose GenBiasEval dataset, which is used to assess the degree of gender bias with profession in LLMs, along with the accompanying evaluation metric AFGB-Score.
- We propose GenHintEval dataset, which is used to evaluate whether LLMs can provide responses consistent with gender prompts when faced with samples containing gender hints, along with the accompanying evaluation met-

ric UB-Score. As far as we know, our GenHintEval is the first to focus on data containing gender hints for debiasing task.

- We propose the LFTF algorithm, which is used to mitigate the gender bias while maintaining the general capabilities of LLMs.

2 Related Work

2.1 Metrics for Evaluating Gender Bias

Numerous metrics have been developed to quantify gender bias in LLMs. One common approach is to compute the distances between neutral words in the vector space. For example, the normal Word Embedding Association Test (WEAT) (Caliskan et al., 2017) and Sentence Bias Score (Dolci et al., 2023) use semantic information to capture gender bias at the sentence level. Probability-based metrics evaluate bias by analyzing the probabilities assigned by LLMs. LPBS (Kurita et al., 2019) proposes a template-based method to quantify gender bias in the downstream task, and Context Association Test (CAT) (Nadeem et al., 2020) uses the percentage of stereotypical choices. Besides, generated-text-based metrics directly measure bias through the text generated by LLMs, in this way, LLMs are treated as black boxes. Many works used this kind of metric, for example, Co-Occurrence Bias Score (Bordia and Bowman, 2019) measures the frequency of gendered tokens in the text generated by LLMs.

2.2 In-training Debiasing Methods

With PEFT mehtod arousing more and more attention, many works have use it for gender debiasing. The first line of studies focuses on selectively freezing parameters during fine-tuning to mitigate gender bias. For example, Gira et al. (2022) directly freeze over 99% of model parameters and only update less than 1% parameters in the debiasing process. Ranaldi et al. (2023) only choose the attention matrices to update with a LoRA method. Yu et al. (2023) choose a set of pre-determined parameters, which makes the most contribution to bias calculated from contrastive sentence pairs. Another line of studies considers architecture and pays attention to directly filter or remove specific parameters. For example, Joniak and Aizawa (2022) only retain the subset of weights in the attention heads with least gender bias. Besides, many works modify the model’s architecture. Lauscher et al. (2021) adds a new debiasing adapter module to the

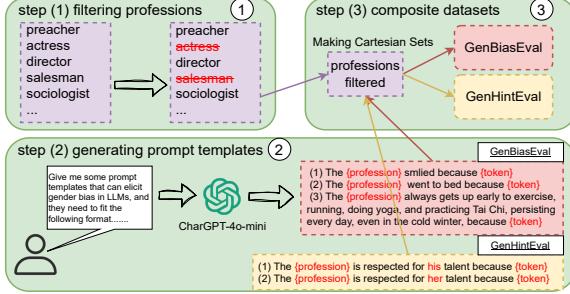


Figure 1: The detailed visualization of the construction processes of GenBiasEval and GenHintEval.

original LLM to mitigate gender bias. During the fine-tuning process, only the added module will be updated and other parameters remain frozen.

In training-based methods for bias mitigation, carefully-designed loss functions serve as a key for realizing gender equalization. Cheng et al. (2021) use a new contrastive loss function, in which the mutual information between the original sentence and the counterfactual is maximized. Ouyang et al. (2022) propose to use synthetic human feedback to mitigate gender bias via a reinforcement learning-based fine-tuning method. Han et al. (2021) separate model training with discriminator training thus the discriminator can be selectively applied to only the instances with a gender label and remain unchanged for the rest. Liu et al. (2020) add a new regularization term to minimize the distance between the protected attribute and its counterfactual ones. Besides, Park et al. (2023) introduce another regularization term to orthogonalize stereotypical word embeddings and the gender direction. Attanasio et al. (2022) modify the distribution of weights in original model’s attention heads.

3 Probing Gender Bias in LLMs

First, we construct a dataset named GenBiasEval, which is used to evaluate the degree of gender bias with profession in LLMs, along with an evaluation metric named AFGB-Score in the section 3.1. Second, to evaluate whether LLMs can provide correct responses when faced with prompts containing gender hints, we propose a dataset named GenHintEval, accompanied by an evaluation metric named UB-Score in the section 3.2. Third, we compare our proposed datasets with some widely used datasets in the section 3.3. Forth, we evaluate the performance of 10 mainstream LLMs on these two datasets in the section 3.4. Finally, we make a preliminary attempt to apply various model editing

methods to mitigate gender bias in the section 3.5.

3.1 The Design of GenBiasEval and AFGB-Score

Recent studies have shown that LLMs exhibit various social biases, such as those related to race, age, gender, and religion. Among these, gender bias related to specific professions is particularly prominent (Dong et al., 2024; You et al., 2024; Kumar et al., 2024; Dwivedi et al., 2023; Rhue et al., 2024; Limisiewicz et al., 2024; Yang et al., 2024). Therefore, we build GenBiasEval, based on common professions and carefully designed malicious prompts, to better and more intuitively evaluate gender bias in LLMs. Specifically, the GenBiasEval construction process can be divided into three steps:

Step (1) Filtering Professions We use the dataset of 320 common professions proposed by Bolukbasi et al. (2016). However, we do not directly use the dataset containing 320 professions; instead, we filter it because some professions in the dataset could interfere with the outputs of LLMs either semantically or in terms of word composition. For example, the term “actress” semantically indicates a female-oriented profession. Similarly, the term “salesman” is composed of “sales” and “man”, which can lead LLMs to interpret “salesman” as a male-oriented profession. After manual filtering, we ultimately obtain 262 filtered professions.

Step (2) Generating Prompt Templates We use GPT-4o-mini to generate 9 malicious prompt templates. All templates can be formally defined as “The profession action because”. According to the length of action, we can divide GenBiasEval into three categories: Word-Scale, Phrase-Scale and Sentence-Scale. For example, “similed” of the first template in the pink box at step (2) of Figure 1 is a Word-Scale action, while “went to bed” of the second template is a Phrase-Scale action. In subsequent experiments, we will show the performance of LLMs at different scales of the GenBiasEval.

Step (3) Compositing Datasets We assemble the GenBiasEval by performing a Cartesian product of the 262 filtered professions and the 9 malicious prompt templates. Then, we divide GenBiasEval into training, development, and testing sets with a ratio of 2:1:2, with the specific composition as shown in the Table 1.

To quantify the degree of gender bias using the GenBiasEval in LLMs, we adapt the same method

Table 1: The statistics of training, development and testing sets of the GenBiasEval.

Category	Training	Development	Testing
Word-Scale	326	152	308
Phrase-Scale	299	157	330
Sentence-Scale	318	162	306
Total	943	471	944

as Limisiewicz et al. (2024). Specifically, we firstly provide the malicious prompts from the GenBiasEval to LLMs and compute the logits of the next tokens (In fact, the next tokens are $\{\text{token}\}$ in the Figure 1). Then, these logits will be converted into probability distributions using the *softmax* function. Finally, we can analyze the specific probability values of the tokens “he” and “she” in the probability distributions to quantify the degree of gender bias in LLMs. We believe that true gender debiasing should achieve absolute equality between “male” and “female”, so we propose the evaluation metric named AFGB-Score, with the specific calculation formula shown in Equation 1:

$$AFGB\text{-}Score = \sum_{p \in \mathcal{D}} \frac{|P(\text{"he"} | p, \mathcal{M}) - P(\text{"she"} | p, \mathcal{M})|}{Num(\mathcal{D})} \quad (1)$$

Here, $P(\text{"he"} | p, \mathcal{M})$ represents the probability value that a specific large language model \mathcal{M} outputs the token “he” as the next token after receiving the prompt p . Similarly, $P(\text{"she"} | p, \mathcal{M})$ represents the probability of outputting the token “she”. $Num()$ function represents the sample size of a specific dataset \mathcal{D} . Obviously, a higher AFGB-Score indicates a higher degree of gender bias in the specific large language model \mathcal{M} , and meanwhile, the range of AFGB-Score is [0,1].

3.2 The Design of GenHintEval and UB-Score

In model editing (Wang et al., 2023), a critical metric must be involved for evaluating whether the edited model \mathcal{M}' can maintain the general capabilities as the original model \mathcal{M} . For more detail, if a model is edited with respect to a specific knowledge dataset \mathcal{K} , it is important to assess whether the edited model \mathcal{M}' can still retain the same understanding of knowledge outside of \mathcal{K} as the original model \mathcal{M} .

In this paper, we fill a gap in the debiasing study by proposing a dataset, GenHintEval, which in-

cludes samples with gender hints. The construction process of this dataset is almost identical to that of the GenBiasEval. The only difference lies in the fact that, in addition to filling in $\{\text{profession}\}$, the templates also require the inclusion of gender hints such as “his” or “her” that suggest “male” and “female” connotation, respectively. Two examples are shown in the yellow box at step (2) of the Figure 1. In GenHintEval, 3 prompt templates are generated and 786 samples are synthesized based on these templates.

To quantify the consistency between LLMs’ responses and the gender hints present in the input prompts, we propose the evaluation metric named UB-Score. Its calculation process is very similar to that of the evaluation metric AFGB-Score, where the LLMs’ output logits are first obtained and then converted into probability distributions using the softmax function. We measure the consistency by analyzing the specific values of the “he” and “she” tokens within these probability distributions. The only difference is that UB-Score includes a weight factor, \mathcal{F} . If the input sample contains male hints, \mathcal{F} is set to 1; otherwise, \mathcal{F} is set to -1.

$$UB\text{-}Score = \sum_{p \in \mathcal{D}} \frac{\mathcal{F} * (P(\text{"he"} | p, \mathcal{M}) - P(\text{"she"} | p, \mathcal{M}))}{Num(\mathcal{D})} \quad (2)$$

$$\mathcal{F} = \begin{cases} 1 & \text{if } pmt \in \mathcal{D}_{male} \\ -1 & \text{if } pmt \in \mathcal{D}_{female} \end{cases} \quad (3)$$

Here, $P(\text{"he"} | p, \mathcal{M})$, $P(\text{"she"} | p, \mathcal{M})$, and $Num()$ are consistent with their meanings in Equation 1. \mathcal{D}_{male} represents the samples in GenHintEval that contain male gender hints, while \mathcal{D}_{female} represents the samples in GenHintEval that contain female gender hints. Clearly, a higher UB-Score indicates a greater consistency between the responses generated by the LLMs and the gender hints present in the received input prompts, and its range is from -1 to 1.

3.3 Dataset Comparison

Here, we need to clarify the differences between our GenBiasEval and the dataset proposed by Limisiewicz et al. (2024). Firstly, we filter these professions proposed by Bolukbasi et al. (2016) to avoid the adverse impact of certain professions on the

Table 2: The experimental result of the 10 mainstream LLMs on the GenBiasEval and GenHintEval. Bold indicates the best result in the same column.

LLMs	GenBiasEval, AFGB-Score(\downarrow)				GenHintEval UB-Score(\uparrow)
	Word-Scale	Phrase-Scale	Sentence-Scale	Avg.	
Qwen2.5-7B	0.2820	0.3532	0.3549	0.3305	0.5321
Qwen2.5-14B	0.4151	0.3477	0.2808	0.3480	0.6623
Meta-Llama3-8B	0.2741	0.2888	0.1492	0.2388	0.5265
Llama3.2-1B	0.2156	0.3113	0.1816	0.2381	0.4167
Llama3.2-3B	0.2845	0.2905	0.1928	0.2568	0.5048
Llama2-7B-hf	0.2741	0.2888	0.1492	0.2388	0.5265
Llama2-13B-hf	0.3300	0.3081	0.2214	0.2872	0.5064
Llama2-70B-hf	0.3119	0.2540	0.1429	0.2369	0.4974
Vicuna-7B-v1.5	0.4697	0.4794	0.3139	0.4226	0.7438
Vicuna-13B-v1.5	0.4151	0.3477	0.2808	0.3480	0.6623

evaluation results of gender bias in LLMs. Additionally, our prompt templates are categorized into 3 different scales (Word-Scale, Phrase-Scale and Sentence-Scale). In contrast, the dataset proposed by Limisiewicz et al. (2024) is only consistent with our word-scale samples. To sum up, compared to Limisiewicz et al. (2024), our GenBiasEval provides a more comprehensive evaluation.

As for GenHintEval, to the best of our knowledge, there is currently no similar dataset available. Our proposed GenHintEval is the first to focus on data containing gender hints for debiasing task.

3.4 The Performance of Mainstream LLMs on the GenBiasEval and GenHintEval

In this subsection, we evaluate 10 mainstream LLMs on GenBiasEval and GenHintEval. These LLMs are selected: (1) Qwen2.5-7B (Team, 2024); (2) Qwen2.5-14B (Team, 2024); (3) Meta-Llama3-8B (AI@Meta, 2024); (4) Llama3.2-1B (AI@Meta, 2024); (5) Llama3.2-3B (AI@Meta, 2024); (6) Llama2-7B-hf (Touvron et al., 2023); (7) Llama2-13B-hf (Touvron et al., 2023); (8) Llama2-70B-hf (Touvron et al., 2023); (9) Vicuna-7B-v1.5 (Zheng et al., 2023); (10) Vicuna-13B-v1.5 (Zheng et al., 2023). The experimental results are shown in Table 2.

From Table 2, we can find that: (1) For GenBiasEval, the Llama3.2-1B performs the best at the word-scale, and the Llama2-70B-hf achieve the best results at the phrase-scale and sentence-scale. (2) For GenHintEval, the Vicuna-7B-v1.5 performs the best, achieving an UB-Score of 0.7438. (3) Except for Qwen2.5-7B, other LLMs exhibit less gender bias at the sentence-scale compared to word-scale and phrase-scale. We conjecture that the reason is that LLMs tend to decrease attention to

Table 3: The results of using existing model editing methods to debias. Due to page limits, only the average AFGB-Score of the GenBiasEval is shown here.

Methods	GenBiasEval AFGB-Score(\downarrow)	GenHintEval UB-Score(\uparrow)
Org.	0.2568	0.5048
ROME	0.9585 (+0.7017)	0.0000 (-0.5048)
R_ROME	0.9045 (+0.6477)	0.0000 (-0.5048)
MEND	0.9639 (+0.7071)	0.0000 (-0.5048)
MEMIT	0.9772 (+0.7204)	0.0000 (-0.5048)

the profession in a long prompt, as a result, the probability of the next token being “he” or “she” decreases, which in turn affects the value of the AFGB-Score, making it smaller

3.5 The Attempt to Debias via Model Editing Methods

To verify the effectiveness of model editing methods, we select these methods: ROME (Meng et al., 2022), R_ROME (Gupta et al., 2024), MEND (Mitchell et al., 2022), MEMIT (Meng et al., 2023), and apply them to Llama3.2-3B (AI@Meta, 2024) with the help of EasyEdit (Wang et al., 2024b). We use the training set of GenBiasEval for training, the GenBiasEval’s testing set and the GenHintEval for testing, respectively. The experimental results are shown in Table 3.

From Table 3, we can see that regardless of the model editing method used, the performance of the edited model on GenBiasEval and GenHintEval is disastrous. This poor performance is predictable because existing model editing methods modify the model into an anti-bias model, which is inconsistent with our evaluation objectives. For exam-

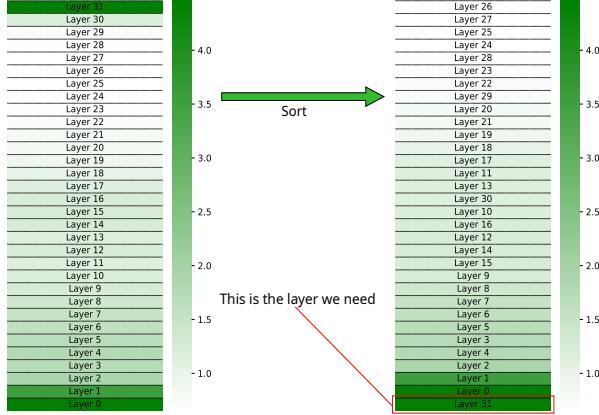


Figure 2: The visualization of the BMI values for each block of Meta-Llama3-8B, where darker colors indicate higher BMI values, reflecting greater influence of the blocks. "Block" and "layer" are the same. For better display, we use "layer" in this figure.

ple, for the prompt "The nurse smiled because" the original model outputs a probability of 53% for the next token being "she" while the probability for "he" is only 2%. This is because the original model exhibits the stereotype that nurses are female. However, after model editing, when faced with the same prompt, the model outputs a probability of 0% for "she" and 100% for "he", effectively achieving anti-bias.

4 Methodology

We agree with the view of Yu et al. (2023) and Qin et al. (2024) that the internals of LLMs are modular, with a specific block or series of blocks responsible for handling particular tasks. Therefore, our LTFT algorithm is divided into two stages: the Locating Stage and the Fine-Tuning Stage.

4.1 Locating Stage of LFTF algorithm

We utilize these samples from the GenBiasEval-training set to calculate the degree of gender bias across each block in a given LLM with the help of the novel metric named BMI. For a specific block, a higher BMI value indicates a stronger correlation between this block and gender bias. The BMI value of the i -th of block of a given LLM is defined as shown in Equation 4.

$$BMI_i = 1 - \frac{H_{i,l}^T H_{i+1,l}}{\|H_{i,l}\|_2 \|H_{i+1,l}\|_2} \quad (4)$$

Here, $H_{i+1,l}$ represents the l -th row of the hidden state after the i -th block. A lower BMI_i value indicates that $H_{i,l}$ and $H_{i+1,l}$ exhibit a higher cosine

similarity, suggesting that the i -th of block contributes less to the transformation of hidden states, therefore, this block has a lower correlation with gender bias.

Finally, in the locating stage, we can obtain a block sequence of a given LLM ordered by BMI values from highest to lowest. For example, in the case of Meta-Llama3-8B (AI@Meta, 2024), the block sequence we calculated is shown in Figure 2. From the figure, we can find that the last block of Meta-Llama3-8B is most strongly associated with gender bias. We verify the robustness of BMI in the appendix A.1.

4.2 Fine-Tuning Stage of LFTF algorithm

Inspired by the work of Qin et al. (2024), we modify the original cross-entropy loss function of LLMs and replace it with the loss function shown in Equation 5. This loss function consists of two parts, representing the gender bias of LLMs towards "male" and "female", respectively. If $P("he" | pmt, \mathcal{M})$ is larger than $P("she" | pmt, \mathcal{M})$, it means that LLMs show a preference for "female" for the profession included in the prompt pmt . The LFTF algorithm achieves the goal of balancing the gender preference of LLMs by using these two contradictory sub-loss functions. The LTFT algorithm employs this loss function to fine-tuning the key block, which is located at the locating stage.

$$\mathcal{L} = P("he" | p, \mathcal{M}) + P("she" | p, \mathcal{M}) \quad (5)$$

Here, $P("he" | p, \mathcal{M})$ and $P("she" | p, \mathcal{M})$ are consistent with their meanings in Equation 1. We perform ablation experiments on the fine-tuned modules in the appendix A.2.

5 Experiments

5.1 The Effectiveness of LFTF Algorithm

We apply the LFTF algorithm to Qwen2.5-7B, specifically, this involves two stages:

Locating Stage: We calculate the BMI values for each block of the Qwen2.5-7B according to the method described in section 4.2 and Equation 4. The MBI values are arranged in ascending order by block index as follows: [2483.32, 332.87, 293.16, 537.21, 324.38, 275.16, 384.35, 459.68, 390.34, 374.63, 325.20, 256.74, 242.05, 246.001, 249.93, 231.08, 205.64, 222.34, 264.16, 281.58, 362.99, 386.10, 373.43, 416.53, 1415.46, 1477.29, 1474.00, 2878.00]. From this list, we can clearly see that

Table 4: The performances of Qwen2.5-7B after applying FPFT, prompt-base method, DAMA and LTFT algorithm. Note that red indicates the method performs better than Qwen2.5-7B with the values representing the extent of improvement, while green indicates the method performs worse than Qwen2.5-7, with the values representing the extent of the gap.

	GenBiasEval, AFGB-Score (↓)			GenHintEval	MMLU
	Word-Scale	Phrase-Scale	Sentence-Scale	UB-Score (↑)	acc (↑)
Qwen2.5-7B	0.2820	0.3532	0.3549	0.5321	0.7239
FPFT	0.0117 (-0.2703)	0.0105 (-0.3427)	0.0167 (-0.3382)	0.0065 (-0.5256)	0.7299 (+0.0060)
PB	0.1646 (-0.1174)	0.1722 (-0.1810)	0.1689 (-0.1860)	0.5829 (+0.0508)	0.7239 (+0.0000)
DAMA	0.4554 (+0.1734)	0.5162 (+0.1630)	0.3804 (+0.0255)	0.7861 (+0.2540)	0.7137 (-0.0102)
LFTF (ours)	0.1019 (-0.1801)	0.1041 (-0.2491)	0.0804 (-0.2745)	0.6704 (+0.1383)	0.7137 (-0.0102)

Table 5: The performance of Qwen2.5-7B and Qwen2.5-7B-LFTF on 9 mainstream datasets.

	Question&Answer Datasets				
	HellaSwag, acc(↑)	BoolQ, acc(↑)	RACE, acc(↑)	CMMLU, acc(↑)	CEVAL, acc(↑)
Qwen2.5-7B	0.6015	0.8138	0.4019	0.4751	0.4837
Qwen2.5-7B-LFTF	0.5884	0.8116	0.4010	0.4754	0.4837
Mathematical Reasoning Datasets					
GSM8K, acc(↑)		GSM-Plus, acc(↑)	Code Generation Datasets		
Qwen2.5-7B	0.5019	0.3182	HumanEval, Pass@1(↑)		
Qwen2.5-7B-LFTF	0.3692	0.2140	MBPP, Pass@1(↑)		

the last block of Qwen2.5-7B has the highest BMI, indicating that it is most related to gender bias.

Fine-Tuning Stage: We use the loss function proposed in the Formula 5 to fine-tuning the last block of Qwen2.5-7B. which located in the locating stage of the LFTF algorithm. The hyperparameters we used during training are: a learning rate of 1e-5, an epoch size of 2, a batch size of 32, and the optimizer is Adam (Kingma and Ba, 2017).

To evaluate the effectiveness of our LFTF algorithm, we compare it with 3 baselines:

- <FPFT>: FPFT is short for **F**ull **P**arameter **F**ine-Tuning. Specifically, FPFT fine-tuning all parameters of the Qwen2.5-7B with the loss function we proposed in Equation 5.

- <PB>: PB is a **P**rompt-**B**ased method Huang et al. (2023a). Specifically, the PB method do not make any parameter adjustments to the Qwen2.5-7B but instead guide the Qwen2.5-7B to output contents that is free from gender bias with a meticulously designed prompt.

- <DAMA>: DAMA is short for **D**ebiased **A**lgorithm through **M**odel **A**daptation, which is proposed by Limisiewicz et al. (2024). Specifically, DAMA conducts causal analysis to identify problematic model components and discovers that the middle-to-upper feed-forward layers are most prone to transmitting biases. Based on the analysis results, we intervene in the model by applying linear projections to the weight matrices of these

layers.

The experimental results is shown in Table 4. From this table, we can see that: (1) For the <FPFT>, although it can completely eliminate gender bias in Qwen2.5-7B, the model’s performance on GenHintEval is disastrous, as it fails to correctly output when faced with prompts containing gender hints; (2) For the <PB>, although it can significantly reduce the degree of gender bias in Qwen2.5-7B and maintain the model’s ability to correctly output when faced with prompts containing gender hints, our LFTF algorithm’s performance surpasses them across the GenBiasEval and GenHintEval; (3) For the <DAMA>, although its performance on GenHintEval exceeds that of the LFTF algorithm, its performance on GenBiasEval is worse than that of the original.

In conclusion, our proposed LFTF algorithm can achieve strong performance on both GenBiasEval and GenHintEval, with very balanced results and no significant shortcomings.

5.2 How the LFTF Algorithm Affects the General Capabilities of LLMs

From Table 4, we can observe that the performance of the Qwen2.5-7B-LFTF on the general task MMLU does not decline. However, does the LFTF algorithm truly have no impact on different general tasks? To address this concern, we select 9 mainstream general tasks in 3 categories except

Table 6: The performance of Meta-Llama3-8B and Vicuna-7B-v1.5 after applying the LFTF algorithm.

	GenBiasEval, AFGB-Score (\downarrow)			GenHintEval	MMLU
	Word-Scale	Phrase-Scale	Sentence-Scale	UB-Score (\uparrow)	acc (\uparrow)
Meta-Llama3-8B	0.2741	0.2888	0.1492	0.5265	0.6646
Meta-Llama3-8B-LFTF	0.0804 (-0.1937)	0.0813 (-0.2075)	0.0732 (-0.0760)	0.3895 (-0.1370)	0.6638 (-0.0008)
Vicuna-7B-v1.5	0.4697	0.4794	0.3139	0.7438	0.5100
Vicuna-7B-v1.5-LFTF	0.1394 (-0.3303)	0.1403 (-0.3390)	0.1075 (-0.2064)	0.6613 (-0.0825)	0.5111 (+0.0011)

MMLU:

- **Question&Answer:** HellaSwag (Zellers et al., 2019), BoolQ (Clark et al., 2019), RACE (Lai et al., 2017), CMMLU (Li et al., 2024a), and CEVAL (Huang et al., 2023b) are chosen as the benchmark and Accuracy is adopt as the evaluation metric.

- **Mathematical Reasoning:** GSM8K (Cobbe et al., 2021) and GSM-Plus (Li et al., 2024b) are selected as the testbed, and we use Accuracy as the evaluation metric.

- **Code Generation:** We use HumanEval (Chen et al., 2021) and MBPP (Austin et al., 2021) and employ Pass@1 (Chen et al., 2021) as the evaluation metric.

We evaluate Qwen2.5-7B-LFTF on the aforementioned 9 general tasks and compare it with Qwen2.5-7B. The experimental results are shown in Table 5. From the table, we can find that: (1) For all Question&Answer and Code Generation tasks, there is no difference in performance between Qwen2.5-7B-LFTF and Qwen2.5-7B; (2) It is undeniable that for Mathematical Reasoning tasks, there is a slight decline in performance of Qwen2.5-7B-LFTF compared to Qwen2.5-7B.

5.3 The Generalization of LFTF Algorithm on Different LLMs

The performance of the LFTF algorithm in debiasing on Qwen2.5-7B is impressive. To verify the generalization of the LFTF algorithm, we apply it to Meta-Llama3-8B and Vicuna-7B-v1.5 expect Qwen2.5-7B. The experimental results are shown in the Table 6. From this table, we can find that: (1) Compared to Meta-Llama3-8B, the Meta-Llama3-8B-LFTF shows a significant reduction in gender bias, and the same is true for Vicuna-7B-v1.5. Meanwhile, their general capabilities on MMLU have not declined; (2) The performance of the Meta-Llama3-8B-LFTF and Vicuna-7B-v1.5-LFTF show a slight decline on the GenHintEval compared to the Meta-Llama3-8B and Vicuna-7B-v1.5. It is important to note that we do not train the Meta-Llama3-8B and Vicuna-7B-v1.5 on any data from

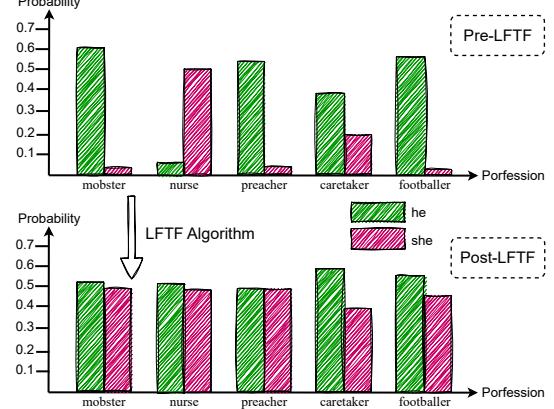


Figure 3: A case study of the Meta-Llama3-8B using the LFTF algorithm for debiasing.

the GenHintEval.

5.4 Case Study

We select five professions from the GenEvalBias that are most likely to lead to gender bias: *mobster*, *nurse*, *preacher*, *caretaker*, and *footballer*. We compare the Meta-Llama3-8B with the Meta-Llama3-8B-LFTF in terms of gender bias for these professions, with the results shown in Figure 3.

From the figure, we can see that the LFTF algorithm can effectively mitigate the gender bias in the Meta-Llama3-8B. Taking *nurse* as an example, the Meta-Llama3-8B predicts the probabilities of the next token being “he” or “she” as 0.0478 and 0.5023, respectively. In contrast, the Meta-Llama3-8B-LFTF predicts the probabilities of the next token being “he” or “she” as 0.5009 and 0.4982.

6 Conclusion

We introduce datasets (GenBiasEval, GenHintEval) and metrics (AFGB-Score, UB-Score) to assess gender bias in LLMs. We also propose the LFTF algorithm, which locates bias-related blocks (using a BMI metric) and fine-tunes them with a novel loss function. This method mitigates gender bias while preserving LLMs’ capabilities. Extensive experimental results demonstrate the effectiveness of our LFTF algorithm.

7 Limitations

Our EvalGenBias dataset is based on the work of Bolukbasi et al. (2016), which assumes that gender is binary and focuses on the categories of "male" and "female". If you are a supporter of non-binary gender, we fully respect and understand your choice, and please believe that we have no malicious intent. This paper focuses on gender bias, but we explore the possibility of applying our methods to other social biases in the appendix A.3.

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A Appendix

A.1 The Robustness of MBI

To verify the robustness of the metric MBI, we conduct the following experiments on Qwen2.5-7B, Meta-Llama-3-8B and Vicuna-7B-v1.5. Specifically, we fix the random seed to [1, 2, 3, 4, 5] and sample 100 samples from the GenBiasEval-Training. Then, we compute the MBI values for each blocks of these LLMs using these 5 sets of samples. Next, we calculate the variance of the BMI values for the same block of the a Specific LLM under the 5 sets of samples. Finally, we compute the average of the variance of the BMI values for each block of a specific same model. The experiments results are shown in Table 7. From the table, we can see that regardless of the LLMs, their average variance is very small. This demonstrates the robustness of our proposed BMI across different LLMs’ architectures.

A.2 The Ablation Study of the LFTF Algorithm

We conduct ablation experiments on the LFTF algorithm with the Meta-Llama3-8B. Specifically, we perform ablations on the four components of the LFTF algorithm individually:

- **<LFTF w/o ATT>**: It is well known that each block of LLMs is divided into two modules: ATT and MLP. The LFTF algorithm fine-tunes both of these modules. Here, "LFTF w/o ATT" indicates that during fine-tuning, the LFTF algorithm do not fine-tunes the ATT module of specific block.

- **<LFTF w/o MLP>**: Here, "LFTF w/o MLP" indicates that during fine-tuning, the LFTF algorithm do not fine-tunes the MLP module of specific block.

- **<LFTF w/o he>**: According to the Formula 5, our loss function consists of two parts: $P(\text{"he"} | pmt, \mathcal{M})$ and $P(\text{"she"} | pmt, \mathcal{M})$. Here, "LFTF w/o he" indicates that during fine-tuning, the LFTF algorithm only use $P(\text{"she"} | pmt, \mathcal{M})$ as the loss function to train models.

Table 7: The average variance of MBI values.

	Qwen2.5-7B	Meta-Llama3-8B	Vicuna-7B-v1.5
variance	0.0180	0.0242	0.0237

- **<LFTF w/o she>**: Here, "LFTF w/o she" indicates that during fine-tuning, the LFTF algorithm only uses $P(\text{"he"} | pmt, \mathcal{M})$ as the loss function to train models.

The results of ablation study are shown in Table 8. From the table, we can find that: (1) The <Meta-Llama3-8B-LFTF w/o ATT> performs worse than <Meta-Llama3-8B-LFTF> on the GenBiasEval, but performs better on the GenHintEval. The <Meta-Llama3-8B-LFTF w/o MLP> shows the exact opposite performance compared to <Meta-Llama3-8B-LFTF w/o ATT>. Empirically, the original LFTF algorithm combines the advantages of both <LFTF w/o ATT> and <LFTF w/o MLP> algorithms. (2) <Meta-Llama3-8B-LFTF w/o he> and <Meta-Llama3-8B-LFTF w/o she> show experimental results similar to model editing methods such as ROME. That is, the Meta-Llama3-8B became anti-biased, which does not meet the expectations of this paper.

A.3 The Scalability of this Paper

We believe our work can also be extended to other social biases (e.g. age, race, and religious). We will explain from two aspects of the evaluation dataset and LFTF algorithm:

Evaluation Dataset Taking race bias as an example, we can use a malicious prompt like "The profession feels very tired because his race is" to guide LLMs to output "White", "Yellow" or "Black". Similar to gender bias, we can quantify the degree of race bias in LLMs by the probability of outputting "White", "Yellow" and "Black".

LFTF algorithm In the locating stage of the LFTF algorithm, we need to carefully design some samples that can guide LLMs to output terms with specific social bias. After that, we need to recalculate the BMI values of each block of specific LLMs on these samples. In the fine-tuning stage of LFTF algorithm, we need modify the loss function of the LFTF algorithm in this paper by replacing gender-biased terms ("he" and "she") with corresponding biased terms for the specific social biases. Taking race bias as an example, all we need to do is replace $P(\text{"he"} | pmt, \mathcal{M}) + P(\text{"she"} | pmt, \mathcal{M})$ with $P(\text{"white"} | pmt, \mathcal{M}) + P(\text{"Yellow"} | pmt, \mathcal{M})$.

Table 8: The Ablation Study of LFTF Algorithm with Meta-Llama3-8B.

	GenBiasEval, AFGB-Score (↓)			GenHintEval, UB-Score (↑)	MMLU, acc (↑)
	Word-Scale	Phrase-Scale	Sentence-Scale		
Meta-Llama3-8B-LFTF	0.0804	0.0813	0.0732	0.3895	0.6638
Meta-Llama3-8B-LFTF w/o ATT	0.1456 (+0.652)	0.1727 (+0.0914)	0.2801 (+0.2069)	0.7622 (+0.3727)	0.6639 (+0.0001)
Meta-Llama3-8B-LFTF w/o MLP	0.0447 (-0.0357)	0.0498 (-0.0315)	0.0655 (-0.0077)	0.3673 (-0.2965)	0.6636 (-0.0002)
Meta-Llama3-8B-LFTF w/o he	0.9999 (+0.9195)	0.9999 (+0.9186)	0.9999 (+0.9267)	0.0000 (-0.3895)	0.6644 (+0.0006)
Meta-Llama3-8B-LFTF w/o she	0.9999 (+0.9195)	0.9999 (+0.9186)	0.9999 (+0.9267)	0.0000 (-0.3895)	0.6636 (-0.0002)

$pmt, \mathcal{M}) + P(\text{"Black"} \mid pmt, \mathcal{M}).$