Sequential Decision-Making for Inline Text Autocomplete

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Abstract

Autocomplete suggestions are fundamental to modern text entry systems, with applications in domains such as messaging and email composition. Typically, autocomplete suggestions are generated from a language model with a confidence threshold. However, this threshold does not directly take into account the cognitive load imposed on the user by surfacing suggestions, such as the effort to switch contexts from typing to reading the suggestion, and the time to decide whether to accept the suggestion. In this paper, we study the problem of improving inline autocomplete suggestions in text entry systems via a sequential decision-making formulation, and use reinforcement learning to learn suggestion policies through repeated interactions with a target user over time. This formulation allows us to factor cognitive load into the objective of training an autocomplete model, through a reward function based on text entry speed. We acquired theoretical and experimental evidence that, under certain objectives, the sequential decision-making formulation of the autocomplete problem provides a better suggestion policy than myopic single-step reasoning. However, aligning these objectives with real users requires further exploration. In particular, we hypothesize that the objectives under which sequential decision-making can improve autocomplete systems are not tailored solely to text entry speed, but more broadly to metrics such as user satisfaction and convenience.

1 Introduction

The ability to enter text is essential in today's world, spanning technology such as keyboards, phone/tablet screens, and smart watches. Autocomplete suggestions are fundamental to modern text entry systems, with applications in domains such as messaging and email composition. Autocomplete provides a mechanism for users to transmit more information without needing to enter too many more characters. For example, the user may simply enter "`how a`", upon which the autocomplete system suggests "`how are you?`", which can be accepted by the user in one additional stroke.

Among many possible instantiations, we choose to focus on *inline* autocomplete systems, which may provide the user with up to a single suggestion at each timestep, displayed inline, e.g., "`how are you?`". Such systems have been shown to be more effective at encouraging users to enter text than other approaches, such as displaying multiple suggestions in a different on-screen location (Azzopardi & Zuccon, 2016). An inline autocomplete system must decide not only *what* to suggest to the user, but also *when* to make a suggestion to avoid interrupting users' focus (Quinn & Zhai, 2016).

Existing autocomplete systems generally follow a two-stage process: 1) generate a ranked list of candidate completions of the current text entered by the user, 2) decide which, if any, to surface to the user based on a pre-defined fixed confidence threshold (Cai et al., 2016; Mitra & Craswell, 2015; Quinn & Zhai, 2016; Fowler et al., 2015). The downside of these systems is that they do not directly consider the cognitive load that surfacing autocomplete suggestions will impose on the user. This may come from several aspects of the autocomplete process, such as switching contexts from typing

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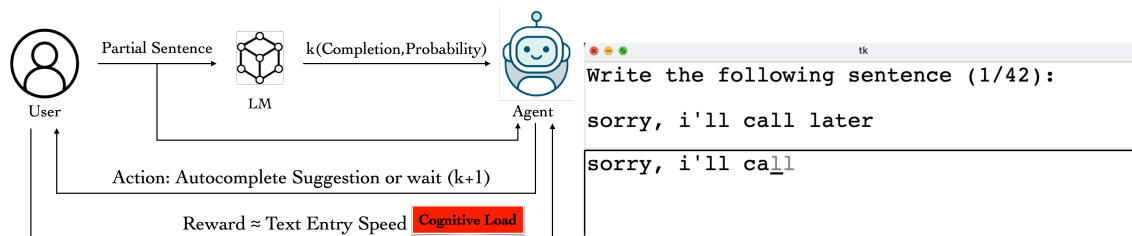
Figure 1: *Left:* An overview of the workflow of our RL agent for inline text autocomplete. A language model (LM) generates k candidate completions of the current text. The RL agent decides which, if any, to give the user as an inline suggestion. The agent is rewarded based on the user's text entry speed, which takes into account the cognitive load of showing suggestions. *Right:* The interface for our user study (Section 6.3). In this example, the user was asked to type the sentence "sorry, i'll call later" on a keyboard. Currently, they have typed "sorry, i'll ca", and a suggestion was made that completes the last word as "call", which the user can accept by pressing the `tab` key.

to reading a suggestion, mentally processing the suggestion, and deciding whether to accept it. Too many suggestions, even if usually accurate, can therefore lead to bad user experience.

We tackle the problem of generating inline autocomplete suggestions while minimizing the user's cognitive load by formulating text autocomplete as a sequential decision-making problem, and apply reinforcement learning (RL) methods (Kaelbling et al., 1996; Sutton & Barto, 2018) to train the autocomplete model. RL solves the problem of learning an optimal sequential decision-making policy through environment interaction, without assuming the differentiability of the objective/reward function *w.r.t.* the model parameters. RL methods have demonstrated impressive success in domains such as Atari (Mnih et al., 2013) and Go (Silver et al., 2016). Using RL methods to train an autocomplete model on top of a language model (LM) allows us to learn suggestion policies through repeated interactions with a target user, and define a reward function based on text entry speed that captures the cognitive load of surfacing suggestions (Figure 1). We note that RL is suitable here since the cognitive load takes an unknown functional form *w.r.t.* the autocomplete model.

This paper's contributions are as follows:

- We formulated the inline text autocomplete problem as sequential decision-making.
- We performed theoretical analysis on when this formulation can improve over myopic reasoning.
- We ran simulated experiments on how an RL autocomplete agent performs on an idealized user.
- We performed a user study to understand the gaps between an idealized user and a real one.

Our key findings are as follows:

(1) We acquired theoretical and experimental evidence that, when optimizing certain objective functions, RL can provide a better suggestion policy than myopic reasoning, but aligning these objectives with real-world users requires further exploration. We believe these objectives are not tailored solely to text entry speed, but more broadly to metrics like user satisfaction and convenience, which aligns with earlier findings in the text entry literature (Quinn & Zhai, 2016).

(2) Given an idealized user that always accepts correct suggestions and inputs each character without typos, we could not find any evidence with a real dataset and language model that RL-trained models improve text entry speed over the classical threshold-based approach with a fixed threshold value.

(3) Our user study ($N = 9$) reveals that for keyboard typing, the cognitive load of looking at a suggestion is independent of its length, but is dependent on whether the suggestion matches what the user is trying to type (10ms if it matches, 50ms if it does not). Also, we could not find any evidence that suggestion acceptance rate is affected by the number of past surfaced suggestions.

Recommendation. Based on these findings, we recommend that further research into sequential decision-making for inline text autocomplete should *not* pursue the goal of solely increasing text

entry speed for idealized users. Instead, more realistic scenarios (stochastic user behavior, typos in their input, etc.), with a focus on user experience, may provide better opportunities for RL methods.

2 Related Work

Autocomplete has a rich history, especially in the domain of search queries (Cai et al., 2016), where methods that rely on neural language models have become increasingly popular (Wang et al., 2020; Park & Chiba, 2017; Wang et al., 2018). For example, Wang et al. (2020) demonstrate how to make use of context in both the generation and ranking phases to improve end-to-end performance. These methods can also be used to obtain personalized models by embedding user IDs (Fiorini & Lu, 2018; Jiang et al., 2018). Like these works, we also use a neural language model in this paper for candidate suggestion generation, but for selection, we use a policy trained using deep reinforcement learning.

A separate line of work has investigated the empirical performance of existing autocomplete systems (Fowler et al., 2015; Quinn & Zhai, 2016; Azzopardi & Zuccon, 2016). Fowler et al. (2015) found that the text entry enhancements found in modern touchscreen phones greatly reduce word error rate. Quinn & Zhai (2016) discovered, surprisingly, that even though autocomplete suggestions can impair text entry speed, users often prefer them subjectively because they lowered cognitive and physical burden. Azzopardi & Zuccon (2016) studied the cost-benefit tradeoffs that users make when conducting searches, concluding that inline autocomplete systems are an effective way to increase the amount of text entered. This entire line of work complements our paper, providing rationale for why inline autocompletion is a useful problem to study, and why cognitive load is important.

Reinforcement learning methods have demonstrated impressive success in domains such as Atari (Mnih et al., 2013), Go (Silver et al., 2016), and control tasks (Brockman et al., 2016), but it is not commonly applied to text autocomplete systems. The two closest works to ours are Wang et al. (2017) and Lee et al. (2019). The former studies query autocomplete as opposed to inline autocomplete; the authors formulated the problem as a multi-armed bandit (Katehakis & Veinott, 1987), a stateless simplification of the Markov decision process framework we adopt. The latter studied autocomplete as a two-agent communication game solved via unsupervised learning and optimized with policy gradients (Sutton et al., 1999). However, they assumed the user only enters keywords drawn from the target phrase, while we allow the user to input any English characters.

3 Background: Reinforcement Learning

In this section, we give background for sequential decision-making and reinforcement learning in the Markov decision process (MDP) framework (Puterman, 2014). An MDP is given by $\langle \mathcal{S}, \mathcal{A}, T, R, \gamma \rangle$, with state space $\mathcal{S}$; action space $\mathcal{A}$; transition model $T(s_t, a_t, s_{t+1}) = P(S_{t+1} = s_{t+1} \mid S_t = s_t, A_t = a_t)$, where t is the time-step, $s_t, s_{t+1} \in \mathcal{S}$, $a_t \in \mathcal{A}$, and S_t, A_t, S_{t+1} are random variables; reward function $R(s_t, a_t, s_{t+1}) = r_t \in \mathbb{R}$; and discount factor $\gamma \in [0, 1]$. The optimal solution to an MDP is a policy $\pi^* : \mathcal{S} \to \mathcal{A}$, a mapping from states to actions, such that acting under π^* maximizes *return*, the expected sum of discounted rewards: $\pi^* = \text{argmax}_\pi \mathbb{E} \left[\sum_{t=0}^{H} \gamma^t R(s_t, \pi(s_t), s_{t+1}) \right]$. Here, H is the horizon of an episode, a sequence of state-action-rewards from an initial to a terminal state. The optimal Q-value of a state-action pair, $Q^*(s_t, a_t)$, is the expected return of taking action a_t from state s_t, and acting optimally afterward: $Q^*(s_t, a_t) = \mathbb{E}_{s_{t+1} \sim T(s_t, a_t, \cdot)} [R(s_t, a_t, s_{t+1}) + \gamma V^*(s_{t+1})]$. The optimal value of a state, $V^*(s_t)$, is the maximum Q-value over actions: $V^*(s_t) = \max_a Q^*(s_t, a)$.

In reinforcement learning, an agent interacts with an MDP where T and R are unknown, and attempts to discover π^* through these interactions. There are many families of algorithms for RL (Kaelbling et al., 1996; Arulkumaran et al., 2017; Sutton & Barto, 2018), but some of the most popular are policy gradient methods and value-based methods. The former optimize a policy directly (Sutton et al., 1999; Schulman et al., 2017; 2015), while the latter learn the value of each state-action pair and use that to infer the policy (Mnih et al., 2013; Watkins & Dayan, 1992). Another

recently popularized direction is offline RL (Levine et al., 2020), in which the agent does not get to interact with the environment, but rather must learn from a static dataset of prior interactions.

4 Problem Formulation: Autocomplete as Sequential Decision-Making

In this section, we describe how to formulate inline text autocomplete as an MDP, which can then be solved via RL. As shown in Figure 1, we assume access to a language model (LM) that can generate k candidate completions of a partial sentence, along with their probabilities. We build the MDP on top of this LM. A state in the MDP is the current *context* and the k candidates from the LM (with their probabilities). The context is all characters entered so far in the sentence, which includes the full previous words and the prefix of the current word. The action space has size $k+1$: surfacing one of the k candidates to the user, or a special `wait` action that does not surface anything. Note that in this formulation, the word corresponding to each action $a \in \{1, \ldots, k\}$ (except for `wait`) changes on each step based on the LM output. While the agent should do better with higher k since it has more candidates to choose from, increasing k would also increase the problem complexity.

The transition model is defined by the user and LM. On each timestep, after the RL agent acts, the user enters a character. The character can be a special acceptance key (e.g., `tab`), or the next English character the user wants to enter. After that, the LM generates k new candidates from the updated context. In our computational experiments (Section 6.2), we will consider an *idealized user* who behaves as follows. They sample a target sentence at the start of each episode, unknown to the RL agent. On each timestep, the idealized user accepts the suggestion if and only if it matches any prefix of the remaining sentence. In case of no suggestion or a mismatched suggestion, the idealized user enters the next English character of the current word without making any typos.[1] An episode ends when all characters of the target sentence have been entered.

Finally, the reward function is proportional to the time saved/lost due to the suggestions:

$$
R = \begin{cases} 0 & \text{no suggestion made by agent} \\ (1 - \alpha) \cdot \text{len(suggestion)} - \beta & \text{suggestion accepted by user} \\ -\alpha \cdot \text{len(suggestion)} - \beta & \text{suggestion ignored by user} \end{cases}.
$$

Here, $\alpha, \beta \in [0, 1]$ are parameters controlling the degree of penalty on the agent when it makes a suggestion, due to the user's cognitive load. α is the cognitive load proportional to suggestion length, while β is a constant cognitive load incurred for moving the gaze. Refer to Appendix A for the derivation of the reward function. By default, we use $\alpha = 40/521$ (character reading time / character writing time) and $\beta = 60/521$ (2× saccade time / character writing time). If the user is idealized, then under this reward function, `wait` actions give zero reward, correct suggestions accepted by the user give positive reward, and incorrect suggestions ignored by the user give negative reward. The choice of γ can heavily influence the optimal solution; our experiments will explore this further.

5 Theoretical Analysis

We begin with a theoretical study of a simple setting where a user may be entering one of two words with equal probability. Our goal is to answer: *Do there exist conditions such that the sequential decision-making formulation of text autocomplete is beneficial over myopic reasoning?* To answer this question, we study a restricted setup and derive conditions on the reward function under which the optimal policy in the MDP with $\gamma = 1$ obtains higher return at a particular timestep than the optimal (myopic) policy in the MDP with $\gamma = 0$, holding all other components fixed. In particular, we aim to show that the farsighted agent *waits* for more information in certain cases where the myopic agent would make an incorrect suggestion, which gives the farsighted agent higher return.

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[1]This transition model is stochastic from the perspective of the RL agent because it does not know the target sentence. We could alternatively model this using a partially observable MDP (Kaelbling et al., 1998), but we stick with the fully observable formulation due to its simplicity and popularity in the RL field.

5.1 Analysis Setup

We focus on an idealized user (Section 4) and $k = 1$, meaning there are two actions to choose from at each timestep: *show* the top LM candidate suggestion (S) or *wait* (W). To keep the analysis simple, we consider two arbitrary words u and v of length n. Both words share the first m letters, e.g., for words "this" and "they" we have $n = 4$, $m = 2$. The user picks the target word uniformly at random across both at the start of each episode. We aim to find α, β in our reward function such that the optimal policy for $\gamma = 1$ waits while the optimal policy for $\gamma = 0$ shows, at the last common letter (position m). Note that this is sufficient to answer our central question stated above, because the Q-value of the $\gamma = 1$ policy is precisely the sum of future rewards, our evaluation criteria. Due to greedy action selection, the $\gamma = 1$ policy will find a better action than the $\gamma = 0$ policy, should they behave differently.

We consider a specific form of the LM that outputs the non-target word as the candidate when $\leq m$ letters are entered, and the target word after that. Let u_t be the state of the tth step consisting of the first t letters of u, and similarly for v_t, for any $t \leq n$. For notational simplicity, we use "$Q(u_t, \cdot)$" to refer to the optimal Q-value of the state u_t (similarly with v_t) and action either S or W. Note that this notation hides the LM candidates portion of the state.

5.2 Derivation for $\gamma = 0$

We begin by deriving conditions on α and β under which the optimal policy for $\gamma = 0$ would prefer to suggest (S) at $t = m$. The base case is $Q(u_n, W) = Q(u_n, S) = Q(v_n, W) = Q(v_n, S) = 0$. Then:

Case 1: $m < t \leq n$
$Q(u_t, W) = Q(v_t, W) = 0$
$Q(u_t, S) = Q(v_t, S) = (n - t)(1 - \alpha) - \beta$
Case 2: $t \leq m$
$Q(u_t, W) = Q(v_t, W) = 0$
$Q(u_t, S) = Q(v_t, S) = 0.5[(n - t)(1 - \alpha) - \beta] + 0.5[-(n - t)\alpha - \beta]$
$= (n - t)(0.5 - \alpha) - \beta$

The condition for preferring suggesting (S) at $t = m$ under $\gamma = 0$ is $Q(u_m, S) > Q(u_m, W)$, which implies that $(n - m)(0.5 - \alpha) - \beta > 0$.

5.3 Derivation for $\gamma = 1$

Now, we derive conditions on α and β under which the optimal policy for $\gamma = 1$ would prefer to wait (W) at $t = m$. This derivation is more involved as the Q-value expressions are recursive, due to lookahead. Again, the base case is $Q(u_n, W) = Q(u_n, S) = Q(v_n, W) = Q(v_n, S) = 0$. Now:

Case 1: $m < t \leq n$
$Q(u_t, W) = \max(Q(u_{t+1}, W), Q(u_{t+1}, S))$
$Q(v_t, W) = \max(Q(v_{t+1}, W), Q(v_{t+1}, S))$
$Q(u_t, S) = Q(v_t, S) = (n - t)(1 - \alpha) - \beta$
Case 2: $t \leq m$
$Q(u_t, W) = Q(v_t, W) = 0.5 \max(Q(u_{t+1}, W), Q(u_{t+1}, S)) + 0.5 \max(Q(v_{t+1}, W), Q(v_{t+1}, S))$
$Q(u_t, S) = Q(v_t, S) = 0.5[(n - t)(1 - \alpha) - \beta] + 0.5[-(n - t)\alpha - \beta + \max(Q(v_{t+1}, W), Q(v_{t+1}, S))]$

With some algebra, we can solve the recursion for the $t = m$ case that we care about:

$$Q(u_m, W) = (n - m - 1)(1 - \alpha) - \beta$$
$$Q(u_m, S) = (n - m)(1 - 1.5\alpha) - 0.5(1 - \alpha) - 1.5\beta$$

The condition for preferring wait (W) at $t = m$ under $\gamma = 1$ is $Q(u_m, S) < Q(u_m, W)$, which implies that $(n - m + 1)\alpha + \beta > 1$.

5.4 Final Constraints on α and β

Putting together the work in Section 5.2 and Section 5.3, we finally obtain the following constraint on α and β which would lead to different optimal policies for $\gamma = 0$ and $\gamma = 1$ at at position m:

$$\boxed{\frac{1 - \beta}{n - m + 1} < \alpha < \frac{0.5(n - m) - \beta}{n - m}}.$$

With a fixed value of β, an α value close to 0.5 can satisfy the above. To go beyond the two-word setup empirically, we obtained the most likely 500 words from our LM (described in Section 6.1), calculated the optimal policy using backward dynamic programming for $\gamma = 0$ and $\gamma = 1$ (other MDP components are the same), and measured the number of states for which the two policies differed. Figure 2 below depicts this difference for various α. We set β to the default value $60/521$.

We can see that the gap is largest when α is between 0.3 and 0.4. Hence, for these values of α, we should see more benefit to solving the autocomplete problem via the sequential decision-making formulation; however, the disagreement (y-axis) only corresponds to $\sim 2\%$ of the state space. Another intuition for using larger α values is to more strongly penalize long but incorrect suggestions, which incentivizes an RL agent to wait for additional input from the user before being informed enough to make a suggestion. Notice that as α gets closer to 1, both policies become very conservative due to the high potential penalty of making wrong suggestions, and hence the number of disagreements reduces drastically.
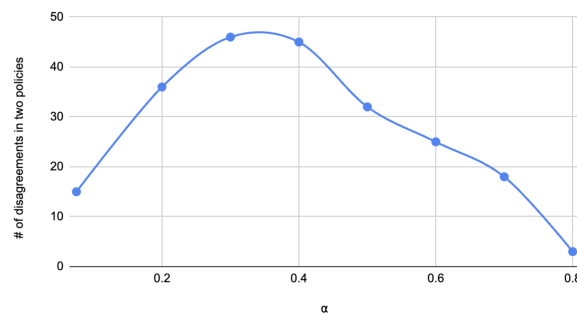

Figure 2: Number of states where the optimal farsighted policy ($\gamma = 1$) and the optimal myopic policy ($\gamma = 0$) disagree, for various values of α.

5.5 Limitations of our Analysis

Although we derived constraints under which text autocomplete benefits from sequential reasoning, these constraints may not reflect the goal of text entry speed improvement. In our user study (Section 6.3), we will see that the ideal values of α and β for faster text entry are near zero, which violates the constraints we derived. Additionally, our analysis depends on a simple form of LM which is unlikely to reflect those used in practice. The degree to which the sequential decision-making formulation can benefit our problem depends on the user's goal and what LM we use to implement the MDP.

6 Experiments

6.1 Experimental Setup

We sampled target sentences for the user from two open-source datasets, SMS Spam Collection ("ham" labels only) (Almeida et al., 2011) and Reddit Webis-TLDR-17 (Volske et al., 2017). Applying the following filters led to ~500 and ~300,000 sentences in each dataset respectively:

- Use only sentences with length ≤ 10 words to save compute.
- Use only sentences with no profanity and whose perplexity is under 150 as computed by GPT2-Large (Radford et al., 2019), to ensure language quality (e.g., no misspellings or slang).
- Remove sentences with characters not in the set "a-z,.'?! " to satisfy the LM input requirements.

For our language model (LM), we trained a small (~25MB) transformer (Vaswani et al., 2017) on the Wikipedia[2] and Reddit Webis-TLDR-17 corpora. This transformer outputs a probability distribution over the English vocabulary. To reduce down to the k candidates fed into our RL agent, we take the top k outputs and renormalize their probabilities. Unless otherwise specified, our experiments only consider single-word autocompletion (as opposed to multi-word).

For all simulations, we assume the user is the idealized one described in Section 4.

6.2 Computational Experiments

We explored three RL algorithms: PPO, an online policy gradient method (Schulman et al., 2017); DQN, an online value-based method (Mnih et al., 2013); and IQL, an offline method (Kostrikov et al., 2021). We benchmark these algorithms against three baseline agents: oracle, uniform random, and threshold-based. The oracle agent has privileged access to the target sentence and always surfaces correct suggestions when given by the LM; it thus establishes an upper bound on performance. The threshold-based agent surfaces the top suggestion if and only if its probability is above a fixed threshold. Optimization on the validation set led us to use threshold=0.3. For PPO and DQN, we used DistilBERT (Sanh et al., 2019) as the policy architecture and initialization, while IQL used a multi-layer perceptron (MLP) trained from scratch. See Appendix B for more details.

The IQL policy received the suggestion probabilities from the LM as part of its input, while PPO/DQN policies did not. This design choice was made because probabilities from the LM are floating-point numbers and it is not useful to tokenize them as strings to feed into transformers. Future work may consider learning or constructing an input representation for these probabilities, e.g., using an embedding layer (Chen et al., 2021) or predefined activation (Gorishniy et al., 2022).

All RL algorithms were trained for 250K gradient steps with $\gamma = 0.99$. Since IQL is an offline RL algorithm, we trained it on a static dataset of 5,000 trajectories collected by a policy that follows the threshold-based baseline but with a 5% chance of taking a random exploratory action each step.

First, we considered the $k = 1$ setting, where the LM generates one candidate and the action space is $\{suggest, wait\}$. We used the default reward function parameters $\alpha = 40/521$, $\beta = 60/521$. Figure 3 shows the average return and number of saved characters in our two domains. In both cases, IQL performed best among RL techniques (9.37 ± 0.17 average return), but could not improve significantly over the threshold-based agent (9.27 ± 0.18). Interestingly, PPO was overly aggressive: it saved the user the most characters, yet it obtained a lower return due to more incorrect suggestions.

These observations made us question whether our autocomplete problem benefits from sequential decision-making, or if a contextual bandit suffices. To answer this, we reran the RL agents under the same MDP but with $\gamma = 0$. Results are shown in Figure 4 (left two plots). Theoretically, $\gamma = 0.99$ renders the problem harder, yet the solution asymptotically should be better or the same as when $\gamma = 0$. For IQL, the results with both γ values were on par. However, for PPO, we observed better results with $\gamma = 0$, though as we increased the number of training steps to 1M, the difference

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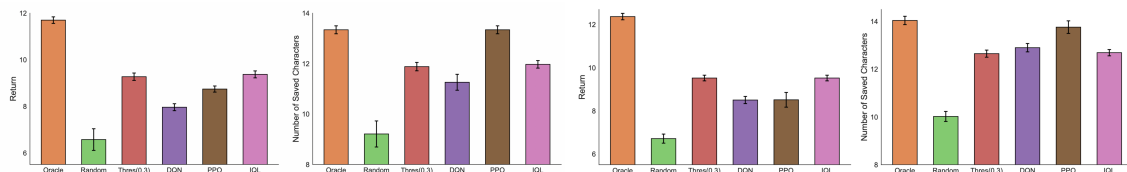[2] https://huggingface.co/datasets/wikipedia

Figure 3: Average return and number of characters saved, over 5 independent runs (including training, for RL agents). Error bars depict 95% confidence interval. *Left two:* SMS dataset, 50 sentences in evaluation set. *Right two:* Reddit Webis-TLDR-17 dataset, 400 sentences in evaluation set.
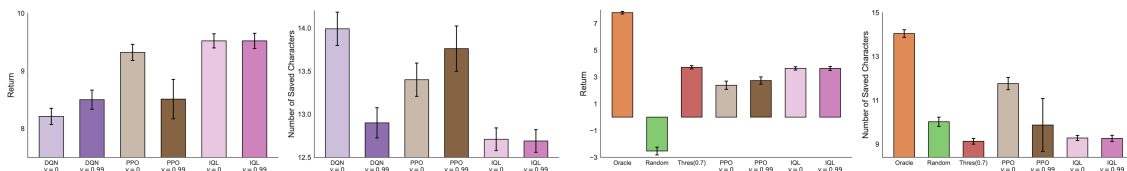

Figure 4: *Left two plots:* Analysis of how varying γ affects RL agents. *Right two plots:* Results of rerunning experiments with $\alpha = 0.4$, as suggested by our theory (Section 5). All plots use the Reddit Webis-TLDR-17 dataset and show the same metrics (y-axis) as in Figure 3. In the right two plots, DQN results are omitted because they were significantly worse than PPO and IQL, and we changed the threshold-based agent to use threshold 0.7 based on re-tuning with the updated α.

disappeared (not shown in plots). Our observations support the hypothesis that with our current setup, sequential decision-making may not be helpful.

Next, we incorporated our theoretical takeaways from Section 5 and set $\alpha = 0.4$ to see if this provides better opportunity for RL. Results are shown in Figure 4 (right two plots). Indeed, our theoretical analysis transferred to PPO: we see that the PPO agent trained under $\gamma = 0.99$ performs better than $\gamma = 0$. Because this difference was not significant after 250K steps, we extended the learning to 1M steps and confirmed the returns differed significantly (not shown in plots): (3.14 ± 0.27) for $\gamma = 0.99$ vs. (2.65 ± 0.16) for $\gamma = 0$. However, like in Figure 3, PPO could not reach the average return of IQL and the threshold-based agent. We believe this gap in performance is due to the fact that the PPO policy does not receive suggestion probabilities from the LM as part of its input.

Our final computational experiment revolved around *multi-word suggestions*, drawing on the intuition that longer suggestions have more opportunity to improve text entry speed. We increased our candidate pool to $k = 5$ and allowed LM candidates to be 1 or 2 words. Since the joint likelihood of suggesting two words is always lower than the likelihood of suggesting just the first, we normalized the joint probability of 2-word suggestions, similar to Murray & Chiang (2018). See Appendix C for details. Unfortunately, our initial experiments indicated that allowing multi-word suggestions degraded the return for both oracle and threshold-based agents. Surprisingly, it also reduced the oracle agent's number of saved characters. The reason is that 2-word candidates can take up the slot of the correct 1-word candidate, preventing it from being seen by the agent. See Appendix D for details. Given these findings, we didn't train RL agents (which are GPU-intensive) in this setting.

6.3 User Study

In addition to our computational experiments, we ran a user study to understand how well our reward function aligns with real user behavior. Our goals were to 1) estimate real values for the reward function parameters, α and β, that capture the cognitive load of the user, and 2) explore the possibility of "accumulated fatigue" (Paas et al., 2003) for the users, meaning that as the number of surfaced suggestions increases, the user is less likely to accept suggestions. To address these goals, we ran a study where we asked $N = 9$ users to enter 42 sentences on a keyboard, both with and
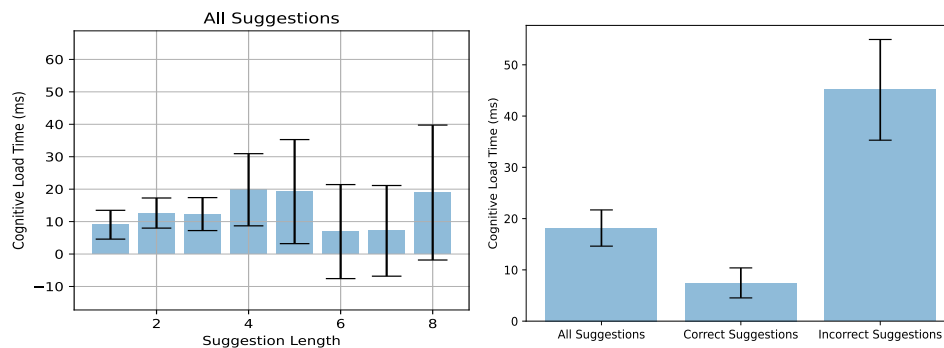
Figure 5: User study results (Section 6.3). Error bars depict 95% confidence interval. *Left:* Average cognitive load versus suggestion length. The cognitive load did not grow significantly with suggestion length. *Right:* Average cognitive load versus suggestion correctness. There is a significant difference between the user's cognitive load when considering correct versus incorrect suggestions.

without autocomplete suggestions. Figure 1 (right) shows an example of the study interface. All $N = 9$ users work with computers as a regular part of their profession.

We obtained 3968 instances where a user entered the same key given the same context (letters typed so far) both with and without autocomplete suggestions. To measure the cognitive load due to the suggestions, we looked at the time difference between how long it took the user to enter the next key in both cases. Figure 5 (left) shows this cognitive load measure as a function of suggestion length. Contrary to our initial estimate of $\alpha = 40/521$, the time users spend on suggestions did not grow with suggestion length, implying that α should be set to 0. The average cognitive load for users was 21.29 ± 3.61ms, which falls within the 20-30ms of a single saccade time for reading (Rayner & Clifton, 2009). This observation suggests that the user only has to saccade once, not twice, after reading a suggestion. This is likely because initially, their eyes are already focused where the suggestion appears, which can in return explain the widespread adoption of inline suggestions.

Furthermore, Figure 5 (right) shows that the cognitive load of looking at a suggestion is highly dependent on suggestion correctness. Specifically, users experienced cognitive loads of 9.18 ± 3.05ms and 50.49 ± 9.67ms for correct and incorrect suggestions respectively. This observation suggests that β is dependent on suggestion correctness, as opposed to our initial fixed estimate of $\beta = 60/521$.

Finally, we probed the presence of "accumulated fatigue", as defined earlier. See Figure 7 in Appendix E for results. The data did not show any evidence of declined acceptance rate based on the cumulative number of past suggestions, or the cumulative number of past incorrect suggestion.

Based on these findings, we re-ran our experiments on the Reddit Webis-TLDR-17 dataset with $\alpha = 0$, and $\beta = 10/521$ if the suggestion is correct and $50/521$ if it is wrong. With these changes, we found that the optimal threshold for the threshold-based agent was 0: always surface the top LM candidate, regardless of its probability. This is because by reducing α and β, we reduced the penalty for incorrect suggestions. This result implies that the sequential decision-making formulation does *not* improve text entry speed of an idealized user when α, β are chosen based on real user behavior. Yet in reality, users do not prefer always-on suggestions, meaning that there is something more than text entry speed that is important to the user (Quinn & Zhai, 2016).

7 Conclusion and Future Work

In this paper, we studied the problem of generating inline autocomplete suggestions via sequential decision-making. This formulation allowed us to apply RL methods to solve the problem, and define a reward function that captures user cognitive load through text entry speed. Our experimental findings suggest that sequential decision-making and RL do *not* improve text entry speed for an

idealized user. Therefore, we recommend that further research into sequential decision-making for inline text autocomplete should *not* pursue the goal of solely increasing text entry speed, but rather aim to make real users enjoy the text entry experience.

There are several important directions for future work, to address some of the limitations of this paper. (1) It would be interesting to perform our theoretical analysis on the outputs of a real language model, to connect better with practice. (2) On the computational side, we hope to experiment with feeding the LM probability values as part of the input into the PPO and DQN agents. (3) Our user study only considered prompted writing tasks, where our software told users what sentences to write. The results may be different if users were asked to do freeform writing. (4) Most importantly, we believe that introducing more realistic conditions into our simulations would provide greater scope for RL-based agents to improve over threshold-based methods. Examples include stochasticity in the user suggestion acceptance behavior, typos in their text input, or deciding suggestion acceptance based on semantic matching with the target sentence rather than hard matching. This research would align well with other work that has found users to prefer autocomplete suggestions due to lower cognitive and physical burden, even when text entry speed is impaired (Quinn & Zhai, 2016).

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A   Reward Derivation

Our objective is to minimize the total time it takes for the user to enter the input. Hence, the instantaneous reward will be proportional to the *saved time* due to a correct suggestion that the user accepted minus the *lost time* due to cognitive load imposed on the user. For simplicity, we assume all characters take the same amount of time to write ($\Delta t_{char-write}$) and to be read ($\Delta t_{char-read}$). We also associate an additional fixed time loss for every suggestion, where the user has to pause and move their gaze ($\Delta t_{distraction}$). Hence we will have:

$$r \propto \text{Saved Time} - \text{Lost Time} \tag{1}$$

$$\propto len(a) \times \text{accepted} \times \Delta t_{char-write} - len(a) \times \Delta t_{char-read} - \Delta t_{distraction} \times (len(a) \neq 0) \tag{2}$$

$$\propto len(a) \left(\text{accepted} - \frac{\Delta t_{char-read}}{\Delta t_{char-write}} \right) - \frac{\Delta t_{distraction}}{\Delta t_{char-write}} \times (len(a) \neq 0) \tag{3}$$

$$\propto len(a)(\text{accepted} - \alpha) - \beta \times (len(a) \neq 0), \tag{4}$$

where a is the suggestion made by the agent (an empty string if no suggestion was made), and "accepted" is a binary indicator for whether the user accepted the suggestion. We estimate $\Delta t_{distraction}$ by two saccada times for the task of natural reading (Rayner & Clifton, 2009), which amounts to $\Delta t_{distraction} = 2 \times 30$ ms $= 60$ms. We estimated the per-character writing time and reading time to be 521ms and 40ms respectively, based on an internal dataset in our target use case of EMG handwriting (CTRL-labs at Reality Labs et al., 2024). This leads to $\alpha = \frac{40}{521}, \beta = \frac{60}{521}$.

B   Further Details on Computational Experiments

Our PPO and DQN agents are built off the CleanRL implementations (Huang et al., 2022), while our IQL agent is built off the CORL implementation (Tarasov et al., 2022). For PPO and DQN, we use a per-action Q-network architecture that takes as input the state and a single candidate suggestion (or `wait`), and produces the corresponding Q-value (and similarly the action probability for the PPO policy). To obtain the best action, we simply choose the candidate suggestion or `wait` with highest Q-value (or with highest action probability for PPO); note that this requires running $k + 1$ forward passes through the model, one per k candidate suggestions plus one for `wait`. Both PPO and DQN used the `distilbert-base-uncased` pre-trained model from HuggingFace[3], where the Q-function and the PPO policy network are implemented as one-layer projection MLPs on top of the distilbert transformer. We did *not* freeze any layers of the transformer; initial experiments found that only training the projection layer of the Q-function network and using distilbert as a frozen feature extractor worsened DQN's performance. IQL used a multi-layer perceptron (MLP) with two hidden layers of size 256 each, and $k + 1$ output nodes, one for each of the k candidates and `wait`. To obtain the best action, we take the action corresponding to the output node with maximum value. All RL agents were trained for 250K steps.

The default hyperparameters for the RL agents are as follows.

PPO: learning rate 10^{-6}, number of steps per iteration 20, number of optimization epochs 1, discount factor 0.99. All other hyperparameters were unchanged from the CleanRL defaults.

DQN: learning rate $3 \cdot 10^{-7}$, target network update interval 10000, learning start iteration 25000, discount factor 0.99, model update frequency 10, batch size 32, exploration ϵ linearly decaying from 1.0 to 0.05 over the first half of training. All other hyperparameters were unchanged from the CleanRL defaults.

IQL: learning rate $3 \cdot 10^{-4}$, batch size 256, discount factor 0.99, $\tau = 0.7$. All other hyperparameters were unchanged from the CORL defaults.

C   Multi-Word Suggestion Length Normalization

In our multi-word suggestions experiment, we generated multiple LM candidates via beam search. Since the joint likelihood of suggesting two words is always lower than the likelihood of suggesting just the first, i.e., $P(\text{second word} \mid \text{first word}) \times P(\text{first word}) < P(\text{first word})$, we normalized the joint probability of each 2-word suggestion by taking the square root to counteract this effect, similar to Murray & Chiang (2018). We note that in the multi-word suggestions experiment, we considered both 1-word and 2-word suggestions, not just the 2-word ones. Hence, for all suggestions, we universally replace the raw probability from the LM, denoted as P, by the normalized probability, denoted as P'. Concretely, the normalized probability P' for a general m-word suggestion $w_{1:m}$ after the entered partial sentence w_{prev} is

$$P'(w_{1:m} \mid w_{\text{prev}}) = \left(\prod_{i=1}^{m} P\left(w_i \mid w_{1:i-1}, w_{\text{prev}} \right) \right)^{\frac{1}{m}}.$$

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[3] https://huggingface.co/distilbert/distilbert-base-uncased

Here, w_i refers to the ith word. We can see that when $m = 1$, we simply have $P'(w_1 \mid w_{\text{prev}}) = P(w_1 \mid w_{\text{prev}})$, and hence no length normalization is applied.

Here is a real example from our LM in the multi-word suggestions experiment. For the context `finally, we have a third val`, the LM generated three candidate completions: `entine's day`, `ue`, and `entine's`. After length normalization, the normalized probabilities were {`entine's day`: 33%, `ue`: 32%, `entine's`: 17%}. This would be impossible without length normalization, as the joint probability of `entine's day` could never exceed the probability of `entine's`, but it is clear that `entine's day` is a better completion for the stated context.

D Why Does Incorporating 2-Word Suggestions Harm the Oracle?

In our initial experiments, we were surprised to find that incorporating 2-word suggestions *harms* the performance of even the oracle agent. Recall that the oracle agent has privileged access to the target sentence the user is trying to write, and therefore will never make a wrong suggestion that gets ignored by the user. Upon probing further, we discovered that this is due to several situations where 2-word candidates take up the slot of the correct 1-word candidate, preventing it from being one of the k candidates seen by the agent. Here, we provide a real example from our experiments.

Recall that our 2-word suggestions experiment used $k = 5$, i.e., the agent picks from the top-5 candidate completions from the LM with the highest probabilities (together with `wait`). For the context `i am gr`, where the user's target sentence is `i am great, how are you?`, the five candidate completions from our LM, in order of descending probability, are: `ateful`, `ateful for`, `ateful to`, `eat for`, and `eat with`. None of these matches the remaining target sentence, so the oracle agent does not surface any suggestion to the user, and instead chooses to `wait` with a reward of 0. However, the LM's sixth completion turned out to be `eat`, which matches the remaining target sentence. Hence, if we were still in the 1-word suggestion scenario, the unmatched 2-word suggestions (`ateful for`, `ateful to`, `eat for`, and `eat with`) would not be present, and the oracle agent would have received `eat` as one of its $k = 5$ options. The oracle then would have surfaced this suggestion to the user and received positive reward.

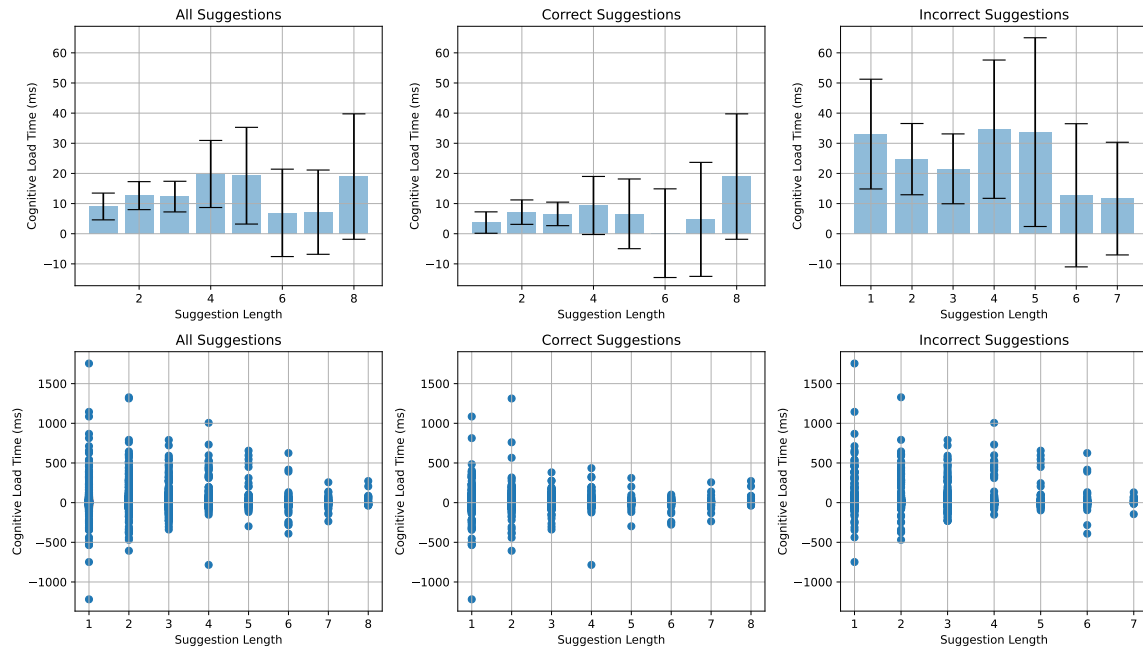## E Cognitive Load User Study - Extended Results

Figure 6: Detailed results of the cognitive load user study based on $N = 9$ subjects. The top row shows the average and 95% confidence intervals, while the bottom row shows all the actual datapoints. The three columns from left to right represent the average cognitive load across: 1) all suggestions, 2) correct suggestions only, and 3) incorrect suggestions only.
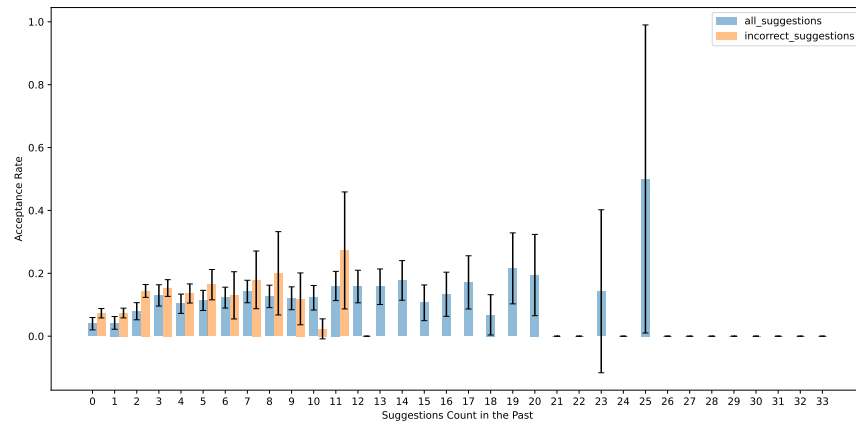

Figure 7: User acceptance rate as a function of the total number of past a) suggestions (blue) and b) incorrect suggestions (orange). The data did not show any evidence of declined suggestion acceptance rate based on the cumulative number of past suggestions, or the cumulative number of past incorrect suggestion. Therefore, we did not find evidence for the accumulated fatigue hypothesis. Error bars depict 95% confidence interval.