

Sparsity	Safe-Fair	Safe-Truthful	Fair-Truthful
$L_0=21$	0.1232	0.0759	0.0978
$L_0=29$	0.1727	0.0929	0.1304
$L_0=77$	0.2418	0.1534	0.1963
$L_0=166$	0.2988	0.2226	0.2581
$L_0=395$	0.3997	0.3496	0.3504

TABLE 7: Conflict between the two semantic steering directions within each SAE of varying sparsity levels. For example, *Safe-Fair* denotes the conflict degree between the safety and fairness steering vectors.

0.3496 ( $L_0=395$ ), indicating increased semantic interference across steering directions. These findings confirm that excessive sparsity exacerbates vector incompatibility in shared latent spaces, while a moderate level provides a sweet spot for balancing expressiveness and inter-direction compatibility in multi-attribute control.

## 5. Limitations and Future Directions

### 5.1. Limitations

Despite its effectiveness, SRS has several limitations. First, SRS requires access to the model’s internal activations and the ability to inject steering vectors into intermediate layers, making it inapplicable to black-box settings. Second, the method relies on a pretrained SAE tailored to the model. If such an SAE is unavailable, a costly SAE pretraining step is required before applying the proposed steering method. Moreover, SRS increases inference-time computation due to sparse encoding and control vector injection, it significantly reduces overall adaptation cost by avoiding fine-tuning.

### 5.2. Future Directions

**Hierarchical Multi-Attribute Composition.** Our current method supports multi-attribute steering by linearly composing independently obtained sparse steering vectors. While this design benefits from the natural disentanglement property of sparse representations, where different attributes activate mostly non-overlapping dimensions, our empirical results suggest that naive composition, such as LW, PCA, or Orthogonal Projection (OP), still falls short of fully capturing the complex relationships among alignment goals.

Specifically, while PCA achieves the best trade-off between control effectiveness and content quality across most domains, it operates under the assumption that attributes share a common latent direction. Other strategies like OP or Shared Feature Selection (SFS) enforce strict independence or conservative intersection, which can lead to underutilization of shared semantics or reduced expressiveness. These limitations highlight a fundamental challenge, i.e., real-world alignment tasks often involve nuanced dependencies and potential conflicts between attributes (e.g., truthfulness may contradict safety when prompts are dangerous or

sensitive), which cannot be fully resolved by global vector-level operations.

A promising future direction is to move beyond global vector composition and explore layer-wise or component-wise multi-attribute steering. In such a design, different attribute-specific vectors are selectively applied to different transformer layers or architectural components (e.g., residual stream, MLP, attention). For instance, a safety vector could be injected into mid-layer residual streams to suppress harmful intent, while a fairness vector operates on earlier MLP activations to mitigate lexical bias. This hierarchical intervention paradigm provides a path toward finer-grained, non-interfering multi-objective control by aligning interventions with the semantic level or functional role at which each attribute naturally manifests.

**Context-Aware and Personalized Steering.** SRS applies a unified steering vector to all prompts within a given attribute domain, ignoring contextual nuances such as topic, intent, or user profile. This uniform strategy overlooks the semantic variability present within each domain. For instance, prompts related to safety may span vastly different contexts, e.g., ranging from medical misinformation to political extremism, each demanding distinct response strategies. A promising future direction is therefore prompt-aware steering, where steering vectors are dynamically tailored based on the semantic content of each input.

Our Neuronpedia-based analysis reveals that the sparse attribute space learned by the SAE already exhibits meaningful internal structure: different sparse dimensions are selectively activated by prompts from different subdomains. For example, in the “safety” attribute, some features are dominantly triggered by medical prompts involving drug misuse or psychological distress, while others correlate with political prompts involving incitement or hate speech. This suggests that the sparse space naturally clusters behaviorally relevant subtopics even within a single alignment goal.

Building on this insight, we envision a personalized steering mechanism that integrates semantic classification with sparse feature routing. Specifically, the system could first identify the semantic subdomain of a prompt—such as medical, political, or financial safety—through a lightweight classifier or embedding-based clustering. Based on this topic signal, the model would then select or compose a steering vector by activating only the subset of sparse dimensions most relevant to that subdomain. In this way, the model’s behavioral adjustment becomes both context-sensitive and interpretable, as each activated sparse feature corresponds to a semantically grounded behavioral component.

## 6. Conclusion

In this work, we proposed SRS, a sparse encoding-based representation engineering method to enable precise steering of LLM while maintaining the response quality. By locating and adjusting task-specific sparse feature dimensions, SRS provides fine-grained control over content generation

while preserving quality and enhancing interpretability, thus serving as a more reliable guardrail for LLMs. Experimental evaluation on various tasks, i.e., safety, fairness and truthfulness, demonstrates that SRS achieves superior control compared to existing methods while mitigating unintended side effects.

## 7. Ethics Considerations

This study aims to advance the safety and controllability of LLMs by systematically analyzing and mitigating unsafe behaviors via sparse representation steering method. The research setup was carefully designed to minimize any potential negative impact. All experiments were conducted in a controlled setting with the sole intention of improving model alignment and transparency. No real-world deployment or malicious exploitation was performed. All derived insights are intended to support safer, more interpretable, and more robust LLM development.

## 8. LLM Usage Considerations

**Originality:** LLMs were used for editorial purposes in this manuscript, and all outputs were inspected by the authors to ensure accuracy and originality.

**Transparency:** All models and datasets used in this study are publicly available. Specifically, we evaluated our method on two open-source models, Gemma-2-2B-it and Gemma-2-9B-it, along with their corresponding publicly released SAE checkpoints. We conduct evaluations on three open-source datasets, i.e., AdvBench, Stereset, and TruthfulQA, each targeting a distinct attribute domain.

**Responsibility:** All experiments were conducted using two NVIDIA A6000 GPUs in a controlled research environment. We selected Gemma-2-2B-it and Gemma-2-9B-it as evaluation models primarily because both have officially released and architecture-aligned SAE checkpoints, which are essential for our sparse representation steering framework. Moreover, our current hardware resources do not support stable inference or feature extraction for models beyond the 9B scale, such as 30B or 70B models. Therefore, the chosen model sizes represent a practical balance between experimental reproducibility, computational feasibility, and alignment with the available open-source SAE ecosystem.

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## Appendix

### 1. Impact Score of Sparse Representations

We visualized the impact scores of each sparse feature dimension on different domains, computed from the positive and negative data in Eq. 5 in the sparse space. The results for the safety domain are shown in Fig. 5, for the fairness domain in Fig. 6, and for the truthfulness domain in Fig. 7.

### 2. Impact of Hyper-parameter $\alpha$

We evaluate the steering effect under different  $\alpha$ . Score represents the attribute score, measuring how well the model output aligns with the targeted property (see Sec. 4.1.2 for details). Coherence quantifies the semantic consistency between the steered output and the user input, since excessively large steering strength  $\alpha$  may distort the generated content. To jointly capture both aspects, we further considered the product of Score and Coherence, which balances property alignment and semantic preservation under different  $\alpha$  values.

The results are demonstrated in Fig. 8. As  $\alpha$  increases, the attribute Score steadily improves. For instance, in the safety domain, the Score rises from approximately 0.94 at  $\alpha = 10$  to about 0.96 at  $\alpha = 80$ , indicating enhanced