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### Exercise 1: Mutable string .....

Create a data type that supports the following operations on a string: **get(int i)**, **insert(int i, char c)**, and **delete(int i)**, where **get** returns the  $i$ th character of the string, **insert** inserts the character **c** and makes it the  $i$ th character, and **delete** deletes the  $i$ th character. Use a binary search tree.

Hint: Use a BST (with key = real number between 0 and 1, value = character) so that the inorder traversal of the tree yields the characters in the appropriate order. Use **select()** to find the  $i$ th element. When inserting a character at position  $i$ , choose the real number to be the average of the keys currently at positions  $i - 1$  and  $i$ .

Use the Red-Black tree implementation from the lectures (**red-black-bst.hpp** attached).

### Exercise 2: Graph Operations .....

In this problem, you are working with an undirected graph represented using an adjacency list. Your task is to implement a series of functions to perform different operations on the graph.

#### Operations to Implement

1. **Find the Vertex with Maximum Degree:** Write a function that finds and returns the vertex with the maximum degree in the graph. The degree of a vertex is the number of edges connected to it.
2. **Find the Degree of a Vertex:** Write a function that takes a vertex as input and returns the degree (the number of edges) of that vertex.
3. **Find the Vertex with Minimum Degree:** Write a function that finds and returns the vertex with the minimum degree in the graph.

#### Input:

- An integer  $n$ , representing the number of vertices.
- A list of edges, where each edge is a pair of integers  $[u, v]$  representing an undirected edge between vertices  $u$  and  $v$ .
- A list of vertices to check for degree queries.

#### Output:

- Output the vertex with the highest degree.
- Output the vertex with the lowest degree.
- Output the degree of the specified vertices.

**Example:****Input:**

`n = 6`

`edges = [[0, 1], [0, 2], [3, 4], [4, 5], [2, 4]]`

`verticesToCheck = [0, 1, 2, 3]`

**Output:**

Vertex with maximum degree: 4

Vertex with minimum degree: 1

Degree of vertices:

Vertex 0: Degree 2

Vertex 1: Degree 1

Vertex 2: Degree 2

Vertex 3: Degree 1