

알고리즘 2주차

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문제 1.

선택 정렬 최선의 경우 : $(n-1) + (n-2) + \dots + 1 = \sum_{i=1}^{n-1} (n-i) = \frac{n(n-1)}{2} = \Omega(n^2)$

삽입 정렬 최선의 경우 : $1 + 1 + 1 + \dots + 1 = \sum_{i=1}^n 1 = (n-1) = \Omega(n)$

퀵 정렬 최선의 경우 : 비교연산 n , 재귀 호출 횟수 $\log n = \Omega(n \log n)$

삽입정렬의 슈도코드

```
void insertion_sort(A[], n) {  
  
  for i <- 1; i < n; i++ {  
  
    value <- A[i]  
  
    j <- i  
  
    while (A[j - 1] > value and j > 0) {  
  
      A[j] <- A[j - 1]  
  
      j <- j - 1  
  
    }  
  
    A[j] <- value  
  
  }  
  
}
```

삽입정렬의 경우 정렬되어있는 배열에 대해서 최선의 시간 복잡도를 가진다. 모든 원소별로 한번씩만 비교를 하면 되므로 $O(n)$ 의 시간복잡도를 가지게된다.

$$\sum_{i=1}^n 1 = n$$

```

insertion_sort.py > insertion_sort
1  import random as r
2
3  def insertion_sort(arr, n):
4      for i in range(1, n):
5          value = arr[i]          #삽입하고자 하는 원소를 지정
6          j = i
7          while(arr[j - 1] > value and j > 0):    #해당 원소보다 앞에 있는 값들과 비교
8              arr[j] = arr[j - 1]              #해당 원소보다 클 경우 뒤로 밀어냄
9              j -= 1
10         arr[j] = value                    #맞는 자리에 해당 원소 삽입
11         print(arr)                      #한 턴 진행 후 출력
12     return arr
13
14 arr = [r.randint(1, 100) for i in range(30)]
15 print("초기 배열 :",arr)
16 print("정렬된 배열 :",insertion_sort(arr, len(arr)))

```

```

taewoo@eomtaeuui-MacBookPro week2 % python3 insertion_sort.py
초기 배열 : [73, 20, 89, 19, 38, 21, 30, 3, 93, 64, 96, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[73, 20, 89, 19, 38, 21, 30, 3, 93, 64, 96, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[89, 73, 20, 19, 38, 21, 30, 3, 93, 64, 96, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[89, 73, 20, 19, 38, 21, 30, 3, 93, 64, 96, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[89, 73, 38, 20, 19, 21, 30, 3, 93, 64, 96, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[89, 73, 38, 21, 20, 19, 30, 3, 93, 64, 96, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[89, 73, 38, 30, 21, 20, 19, 3, 93, 64, 96, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[89, 73, 38, 30, 21, 20, 19, 3, 93, 64, 96, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[93, 89, 73, 38, 30, 21, 20, 19, 3, 64, 96, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[93, 89, 73, 64, 38, 30, 21, 20, 19, 3, 96, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[96, 93, 89, 73, 64, 38, 30, 21, 20, 19, 3, 98, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 73, 64, 38, 30, 21, 20, 19, 3, 75, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 64, 38, 30, 21, 20, 19, 3, 73, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 64, 38, 30, 21, 20, 19, 3, 65, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 38, 30, 21, 20, 19, 3, 55, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 55, 38, 30, 21, 20, 19, 3, 9, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 55, 38, 30, 21, 20, 19, 9, 3, 55, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 55, 55, 38, 30, 21, 20, 19, 9, 3, 43, 16, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 55, 55, 43, 38, 30, 21, 20, 19, 16, 9, 3, 43, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 55, 55, 43, 43, 38, 30, 21, 20, 19, 16, 9, 3, 30, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 55, 55, 43, 43, 38, 30, 21, 20, 19, 16, 9, 3, 18, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 55, 55, 43, 43, 38, 30, 21, 20, 19, 18, 16, 9, 3, 44, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 55, 55, 44, 43, 43, 38, 30, 30, 21, 20, 19, 18, 16, 9, 3, 60, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 60, 55, 55, 44, 43, 43, 38, 30, 30, 21, 20, 19, 18, 16, 9, 3, 36, 95, 76, 88, 16]
[98, 96, 93, 89, 75, 73, 73, 65, 64, 60, 55, 55, 44, 43, 43, 38, 36, 30, 30, 21, 20, 19, 18, 16, 9, 3, 95, 76, 88, 16]
[98, 96, 95, 93, 89, 75, 73, 73, 65, 64, 60, 55, 55, 44, 43, 43, 38, 36, 30, 30, 21, 20, 19, 18, 16, 9, 3, 76, 88, 16]
[98, 96, 95, 93, 89, 76, 75, 73, 73, 65, 64, 60, 55, 55, 44, 43, 43, 38, 36, 30, 30, 21, 20, 19, 18, 16, 9, 3, 88, 16]
[98, 96, 95, 93, 89, 88, 76, 75, 73, 73, 65, 64, 60, 55, 55, 44, 43, 43, 38, 36, 30, 30, 21, 20, 19, 18, 16, 9, 3, 16]
[98, 96, 95, 93, 89, 88, 76, 75, 73, 73, 65, 64, 60, 55, 55, 44, 43, 43, 38, 36, 30, 30, 21, 20, 19, 18, 16, 16, 9, 3]
정렬된 배열 : [98, 96, 95, 93, 89, 88, 76, 75, 73, 73, 65, 64, 60, 55, 55, 44, 43, 43, 38, 36, 30, 30, 21, 20, 19, 18, 16, 16, 9, 3]
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```

문제2.

1. 비순환적 선택 정렬

슈도코드:

```
function selection_sort(array arr, integer n)
```

```
for(int i = 0; i < n; i++)
```

```
    min <- i
```

```
    for (int j = i; j < n; j++)
```

```
        min <- j
```

```
    Swap arr[min],arr[i]
```

```
    print(arr)
```

```
return arr
```

```
selection_sort.py > ...
1  def selection_sort(arr, n):
2      for i in range(0, n):
3          min = i
4          for j in range(i, n):
5              if(arr[min] > arr[j]):
6                  min = j
7          arr[min], arr[i] = arr[i], arr[min]
8          print(arr)
9      return arr
10
11
12 arr = [30, 20, 40, 10, 5, 10, 30, 15]
13 print(arr)
14 print(selection_sort(arr, len(arr)))
```

문제 출력 디버그 콘솔 터미널 포트 + v zsh

```
taewoo@eomtaeuui-MacBookPro week2 % python3 selection_sort.py
[30, 20, 40, 10, 5, 10, 30, 15]
[5, 20, 40, 10, 30, 10, 30, 15]
[5, 10, 40, 20, 30, 10, 30, 15]
[5, 10, 10, 20, 30, 40, 30, 15]
[5, 10, 10, 15, 30, 40, 30, 20]
[5, 10, 10, 15, 20, 40, 30, 30]
[5, 10, 10, 15, 20, 30, 40, 30]
[5, 10, 10, 15, 20, 30, 30, 40]
[5, 10, 10, 15, 20, 30, 30, 40]
[5, 10, 10, 15, 20, 30, 30, 40]
taewoo@eomtaeuui-MacBookPro week2 %
```

2. 순환적 선택 정렬

슈도코드 :

Function recursive_sel_sort(array arr, integer n, integer m)

 If n == m

 Return arr

min <- n

 for(int i = n + 1; i < m, i++)

 If arr[min] > arr[i]

 min <- i

Swap arr[n], arr[min]

print arr

recursive_sel_sort(arr, n+1, m)

```
selection_sort.py > ...
1  import random as r
2
3  def recursive_sel_sort(arr, n, m):
4      if(n == m):
5          return arr
6      min = n
7      for i in range(n+1,m):
8          if (arr[min] > arr[i]):
9              min = i
10         arr[n], arr[min] = arr[min], arr[n]
11         print(arr)
12         return recursive_sel_sort(arr, n+1, m)
13
14 arr = [30, 20, 40, 10, 5, 10, 30, 15]
15 print(arr)
16 print(recursive_sel_sort(arr, 0, len(arr)))
```

문제 출력 디버그 콘솔 터미널 포트 + ~ zsh □ 🗑

```
taewoo@eomtaeuui-MacBookPro week2 % python3 selection_sort.py
[30, 20, 40, 10, 5, 10, 30, 15]
[5, 20, 40, 10, 30, 10, 30, 15]
[5, 10, 40, 20, 30, 10, 30, 15]
[5, 10, 10, 20, 30, 40, 30, 15]
[5, 10, 10, 15, 30, 40, 30, 20]
[5, 10, 10, 15, 20, 40, 30, 30]
[5, 10, 10, 15, 20, 30, 40, 30]
[5, 10, 10, 15, 20, 30, 30, 40]
[5, 10, 10, 15, 20, 30, 30, 40]
[5, 10, 10, 15, 20, 30, 30, 40]
taewoo@eomtaeuui-MacBookPro week2 %
```