#### Al and Deep Learning

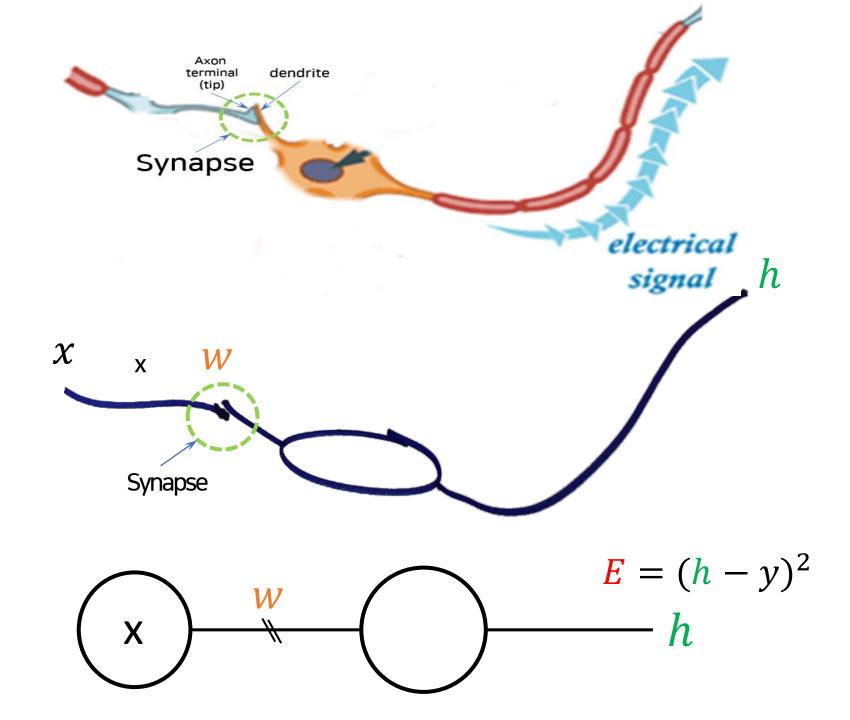
## Logistic Regression (1)

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# Agenda

- Artificial Intelligence
- Brain, Neurons
- Learning
- Regression
- Deep Neural Networks
- · CNN





# Logistic Regression

The shape of regression is not linear but logistic.

What does that mean?

# W desmos

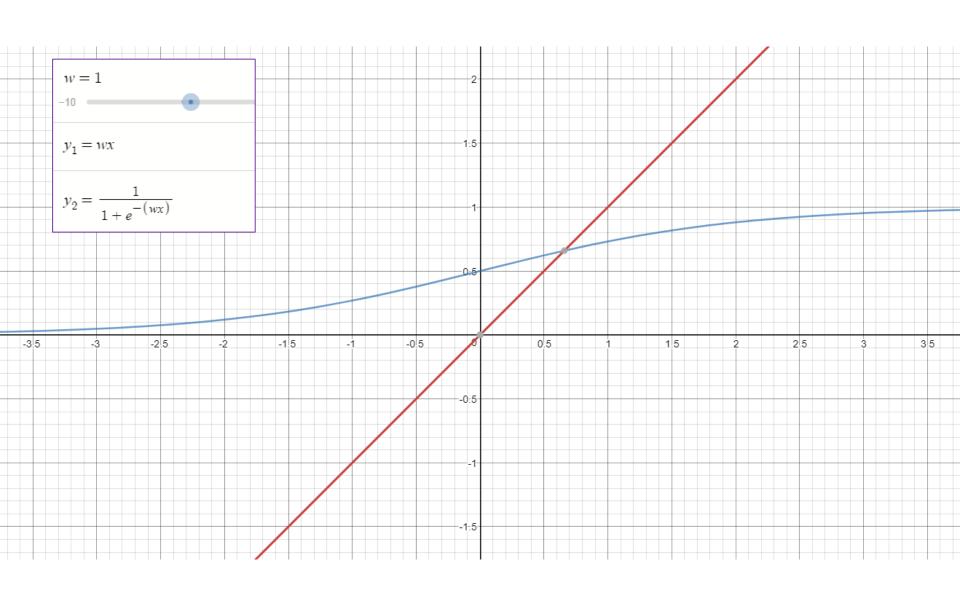
점 (-3, 0), (-2, 0), (-1, 0), (1, 1), (2, 1), (3, 1) 표시

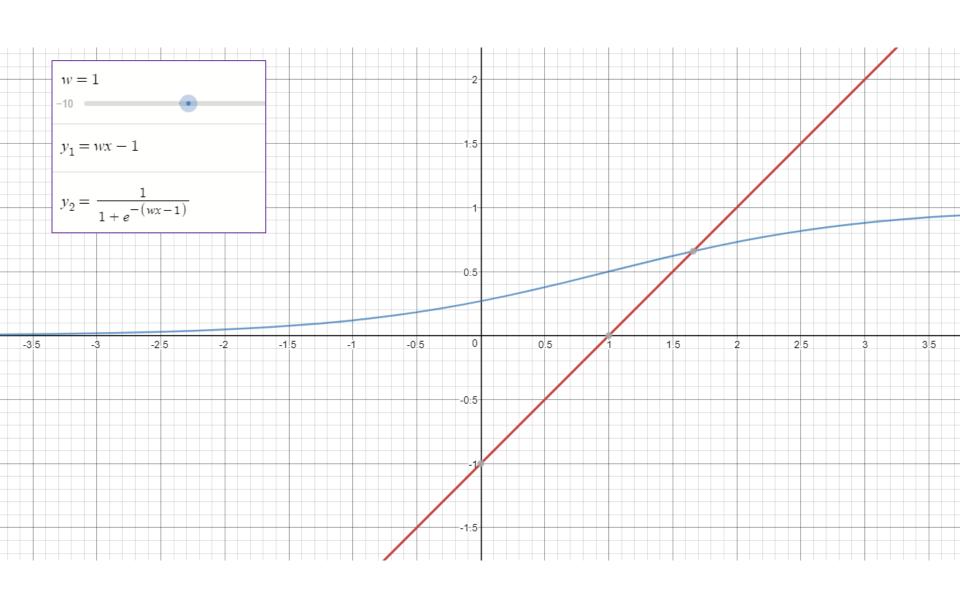
$$y = wx$$
$$y = \frac{1}{1 + e^{-wx}}$$

x	<b>⊕</b> y
-2	0
-1	0
1	1
2	1

х	Sy.
-2	0
-1	0
Н	1
2	н

## 0, 1을 결정(decision)하는 경계(boundary)



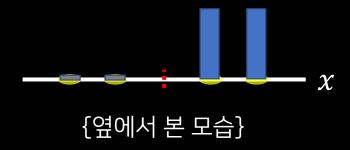


## 결정 경계

$$h = \frac{1}{1 + e^{-(wx)}}$$
 ਰੁਕ ਬੰਸ  
 $or$ ,  
 $h = \text{sigmoid } (wx)$ 

## 결정 경계

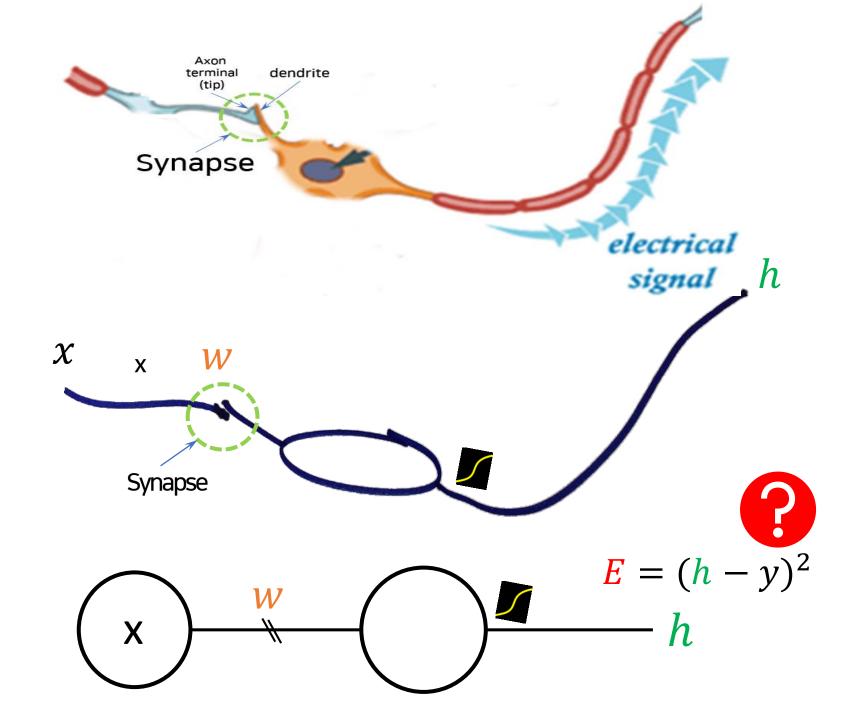
$$wx = 0$$
$$x = 0$$



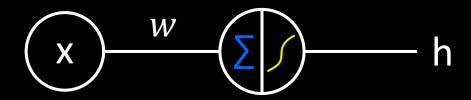
$$wx + b = 0$$
$$x + 1 = 0$$

$$\sim$$
  $\sim$   $\sim$   $\sim$   $\sim$   $\sim$   $\sim$   $\sim$ 

{위에서 본 모습}



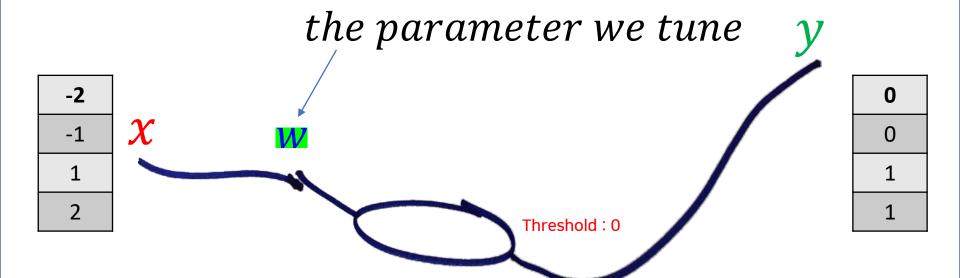
## 신경 세포 기능



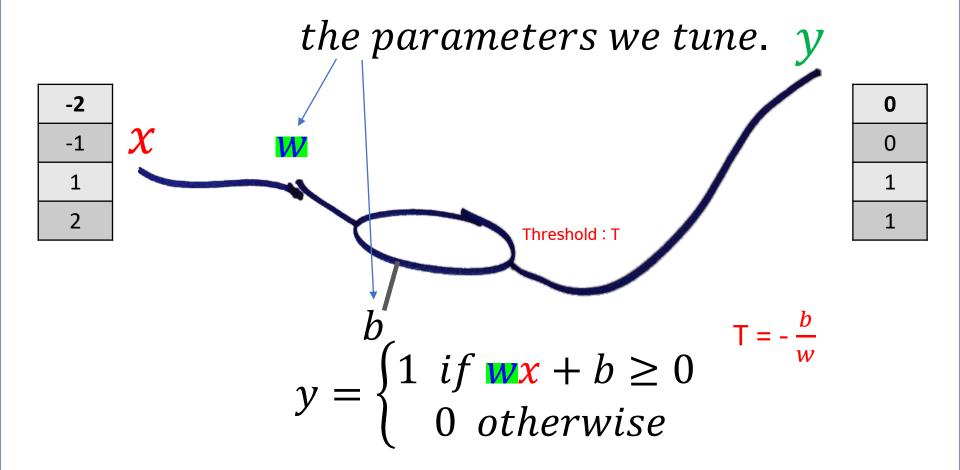
- 신경세포 1개가 할 수 있는 것은?
- 한 개의 입력 x에 따라 0, 혹은 1을 출력(h)함. 예를 들어, 입력이 -1이면 0을, 3이면 1을 출력함.

#### Classification

- Pass(1) or Fail(0)
- Spam(1) or Ham(0)
- Scam(fraud, 1) or not(0)
- Safe(1) or Dangerous(0)
- Intrusion/virus(1) or not(0)
- Cancer(1) or not(0)
- Binary classification -> Multiple classification



$$y = \begin{cases} 1 & if \mathbf{w} \mathbf{x} \ge 0 \\ 0 & otherwise \end{cases}$$



# 가설

$$H(X) = \frac{1}{1 + e^{-WX}}$$

### 오류 함수

Prediction by a neuron

$$cost = \frac{1}{m} \sum_{i=1}^{m} (H(x_i) - y_i)^2$$
Correct answer

"로지스틱 리그레션에도 동작할까?"

### 오류 함수



• 로지스틱 리그레션의 오류 함수로 MSE를 <u>사용할 경우 어떤 문제가 발생할까?</u>

#### √ desmos

점 (-3, 0), (-2, 0), (-1, 0), (1, 1), (2, 1), (3, 1) 표시

$$y = wx$$
$$y = \frac{1}{1 + e^{-wx}}$$

점 (1, 1)만 표시

$$E = \left(\frac{1}{1 + e^{-w \cdot 1}} - 1\right)^2$$

(w, E)

#### **W** desmos

점 (-1, 0), (1, 1) 표시

$$y = \frac{1}{1 + e^{-wx}}$$

$$E = \left(\frac{1}{1 + e^{-w \cdot 1}} - 1\right)^2 + \left(\frac{1}{1 + e^{-w \cdot -1}} - 0\right)^2$$

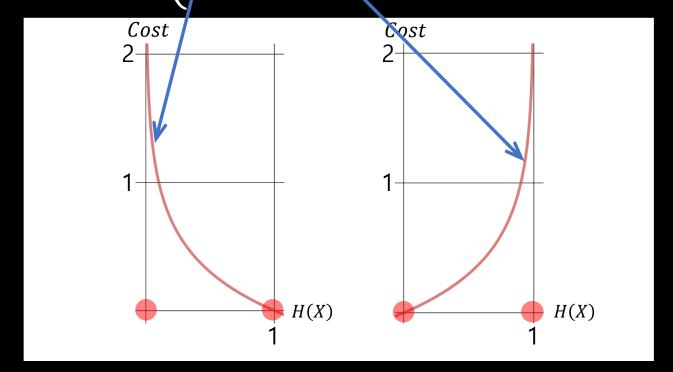
(w, E)

### 오류 함수

Prediction by computer

Correct answer

$$cost = \begin{cases} -\log(H(X)) : y = 1 \\ -\log(1 - H(X)) : y = 0 \end{cases}$$



### 오류 함수

$$cost = \begin{cases} -\log(H(X)) &: y = 1 \\ -\log(1 - H(X)) &: y = 0 \end{cases}$$



$$cost = -y \log(H(X)) - (1 - y) \log(1 - H(X))$$

$$W = W - \alpha \frac{\partial}{\partial W} cost(W)$$

# (실습) 11.py

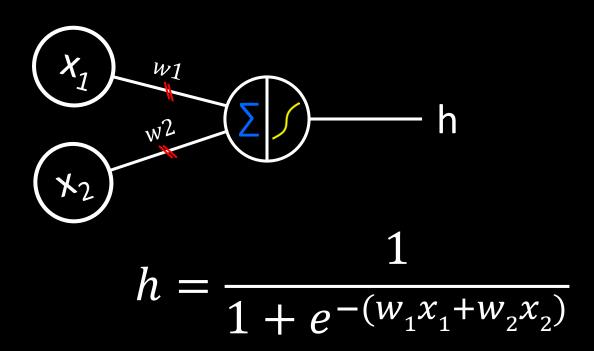
음수는 0으로 양수는 1로 분류

```
x_{data} = [-2., -1, 1, 2]
y_{data} = [0., 0, 1, 1]
#---- a neuron
w = tf.Variable(tf.random_normal([1]))
hypo = tf.sigmoid(x_data * w)
#---- learning
cost = -tf.reduce_mean(y_data * tf.log(hypo) +
        tf.subtract(1., y_data) * tf.log(tf.subtract(1., hypo)))
train = tf.train.GradientDescentOptimizer(learning_rate=0.01).minimize(cost)
sess = tf.Session()
sess.run(tf.global_variables_initializer())
for step in range(5001):
    sess.run(train)
#---- testing(classification)
predicted = tf.cast(hypo > 0.5, dtype=tf.float32)
p = sess.run(predicted)
print("Predicted: ", p)
```

# (실습) 12.py

바이어스를 갖는 뉴런

## 신경세포 (2 입력)



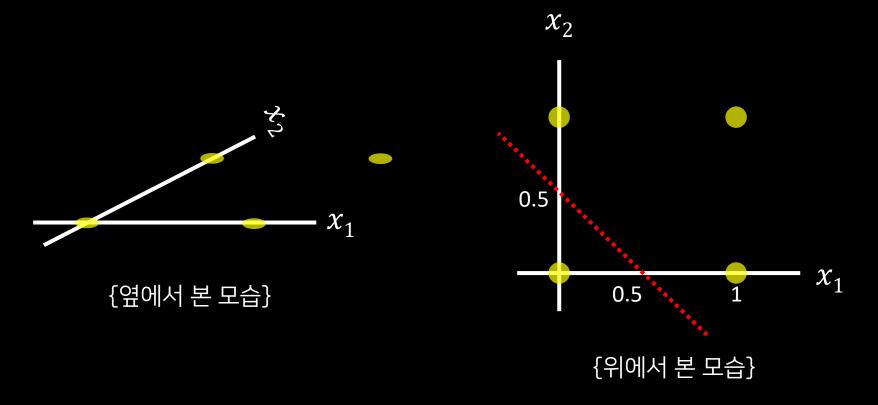
## 신경 세포 (2 입력)

• 결정 경계는?

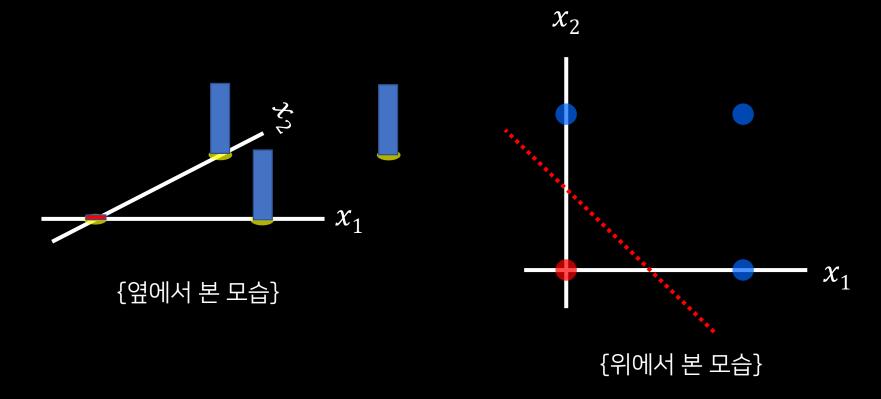
$$w_1 x_1 + w_2 x_2 = 0$$
  
 $x_1 + x_2 = 0$ 

$$w_1 x_1 + w_2 x_2 + b = 0$$
  
 $x_1 + x_2 - 0.5 = 0$ 

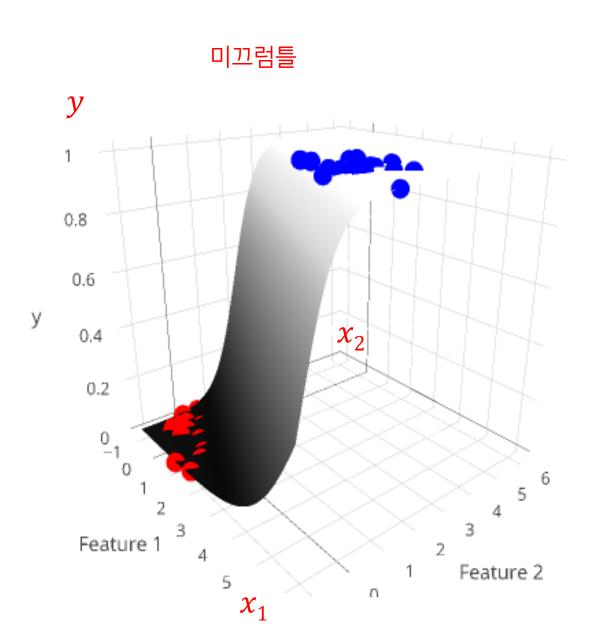
# 신경세포(2입력)

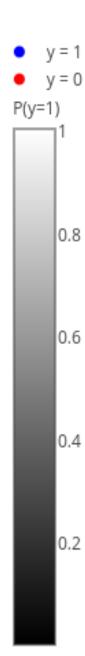


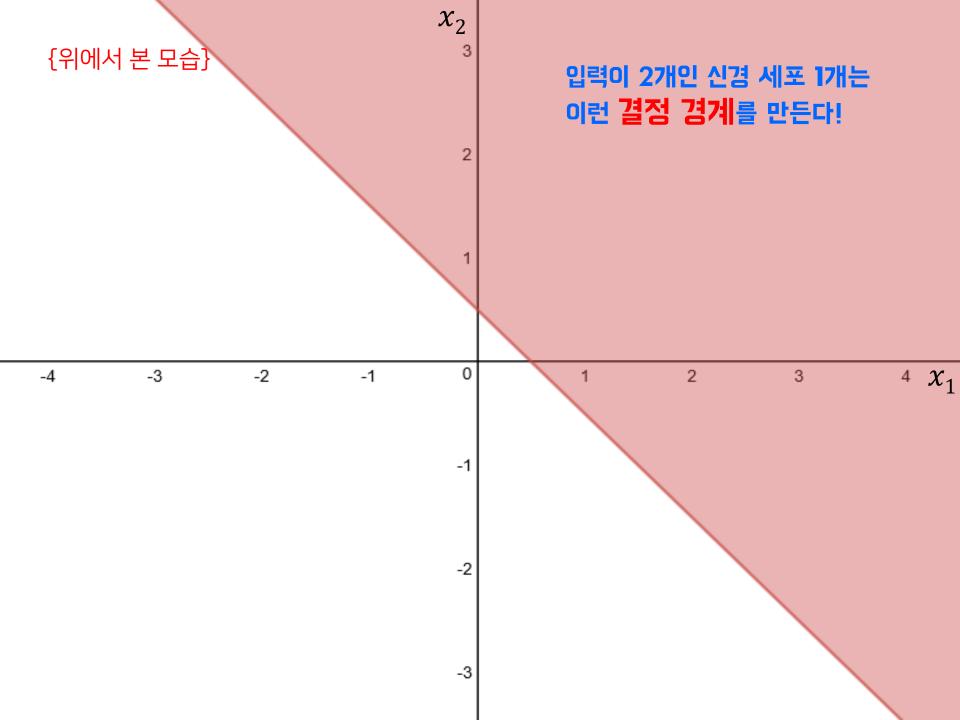
# 신경세포 (2 입력)



#### Logistic Regression: 2 Features

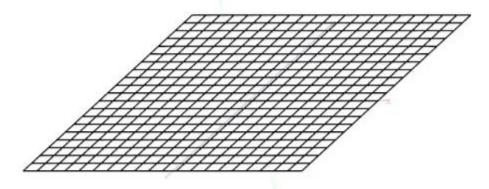






## Decision Boundary in 3D

 $sigmoid(w1 \cdot length + w2 \cdot width + b)$ 



```
surface(f(x,z)=sig(w1·x+w2·z+b))

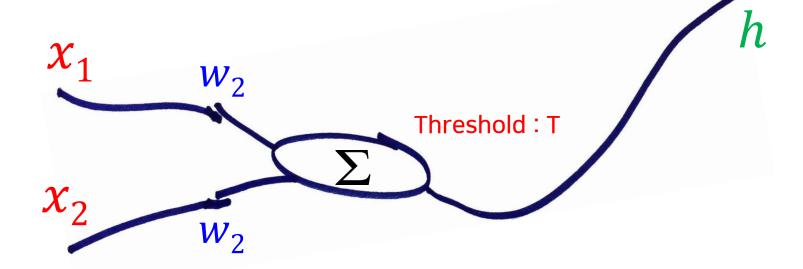
w1 = 10.00

w2 = 0.00

b = 0.00
```

## (실습) 13.py

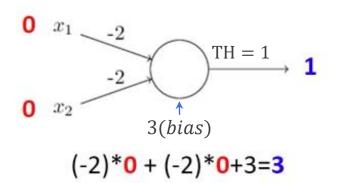
- 입력 두개(x1, x2)를 갖는 뉴런을 이용하여 OR 게이트를 구현함
- 한 개의 결정 경계
- (0, 0) -> 0, <u>그</u> 외 -> 1



$x_1$	$x_2$	AND(h)
0	0	0
0	1	0
1	0	0
1	1	1

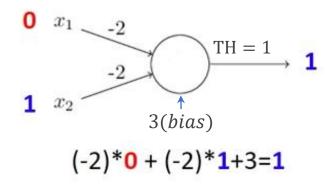
#### **NAND**

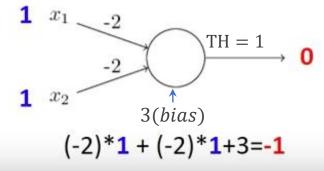
- NAND gates are functionally complete.
- We can build any logical function out of them.

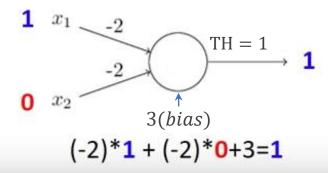


NAND Truth Table

Input A	Input B	Output Q
0	0	1
0	1	1
1	0	1
1	1	0







## 요 약

- 로지스틱 리그레션과 분류(classification)
- 로지스틱 리그레션을 위한 cost 함수
- 한 개의 뉴런이 만들어 내는 결정 경계
- 텐서 플로우를 이용한 ML 프로그래밍