

## Resampling Method - Seminar 3

### Math 567: Winter 2016

February 17, 2016

### The jackknife Resampling Method

The **jackknife** is a resampling technique developed by Maurice Quenouille (1949, 1956) and John Tukey (1958). It preceded the **bootstrap** technique, it's most used for **variance** and **bias** estimation.

#### 1. Estimation

To find the **jackknife** estimate of a parameter, we estimate the parameter for each subsample omitting the *i*th observation to estimate the previously unknown value of parameter.

$$\bar{x}_i = \frac{1}{n-1} \sum_j^n x_j$$

#### Variance Estimation

An estimate of the variance of an estimator can be calculated using the jackknife technique.

$$\text{Var}_{(\text{jack})} = \frac{n-1}{n} \sum_{i=1}^n (\bar{x}_i - \bar{x}_{(\cdot)})^2$$

$\bar{x}_i$  is the parameter estimate based on leaving out the *i*th observation, and  $\bar{x}_{(\cdot)}$  is the estimator based on all of the subsamples.

#### 2. The jackknife estimate of bias of our dataset using R language

First we install and load the "bootstrap" package

```
install.packages("bootstrap")  
library(bootstrap)
```

load the data

```
data <- read.csv('Seminar_2.csv', header = TRUE, sep = "")
```