## SYSC 4415 Introduction to Machine Learning Fall 2021

Assignment 1

Submission instructions: Please prepare a single Jupyter Notebook with all of your answers. Some answers will only require text while others require text+code+results. Please use the template solution available from the course GitHub repo under "Assignments/Assig1".

- 1. Calculate the gradient of the  $f(x, y, z) = z^3 + x^2y y^2 + 3yz$  at (-2, 3, 1). What does this vector represent?
- 2. For a data science project, you decided to poll your friends to determine the relationship between their need for excess amounts of coffee (greater than 2 cups) versus how many hours of sleep they got the night before during midterm season. One morning you record the number of hours of sleep your friends got on a 1 to 5 scale, since no student gets more than 5 hours of sleep during midterm season. Below are a sample of your results:

2	1	4	1	3	2	3	2	5	1

a. What is the <u>expected value</u> from this sample? Using an <u>unbiased estimator</u>, what are the sample variance and standard deviation?

Oh No! You found out that a research group has already published a similar study. To get an A+ you'll need to compare your results to theirs. They determined the probability mass function, Pr(x), where x is how many hours of sleep the students got the night before. They also found the probability the students needed excess amounts of coffee given the number of hours they slept, Pr(+|x). They provide the results in the table below but the study did not report Pr(3). You need these results for your project!

o. Your project.									
x	1	2	3	4	5				
Pr(x)	0.25	0.3	??	0.10	0.15				
Pr(+ x)	0.75	0.55	0.35	0.2	0.1				

- b. What is Pr(3)?
- c. Find the expected value and the variance for Pr(x).
- d. Find the probability that a student slept 2 hours the night before (x = 2), given that they **did not** need excessive amounts of coffee. That is, find Pr(2|-). Hint: Pr(+) can be found by summing over Pr(+|x)Pr(x), for all x. Pr(-|x) can be derived from Pr(+|x). Bayes' Theorem might be helpful.
- Create a python notebook that loads the Kaggle Diabetes Data Set
   (https://www.kaggle.com/mathchi/diabetes-data-set)
   This dataset has 8 features and 2 classes of diabetes possibility: Outcome: 0=doesn't have diabetes; 1= has diabetes. Hint: look at the notebooks from Tutorials 2 & 3 for example code for achieving the steps below.
  - a. Split the data, using 75% for training and 25% for test. Make sure you use stratified sampling.

- b. Train and test a logistic regression classifier. How accurate is your classifier?
- c. Repeat part b), but using only the Pregnancies and SkinThickness features from the dataset. Was the classifier accuracy impacted?
- d. Using the 2-feature classifier from part c), create two subplots using the Pregnancies and SkinThickness features from the data set. See Tutorial 3 Part 2 for similar plots.
  - i. On the first, plot the decision boundary and the training data. Use green doesn't have diabetes (Outcome==0) and blue for has diabetes (Outcome==1).
  - ii. On the second, plot the decision boundary and the test data. Use the same colours (blue/green), but highlight all misclassified test points (from either class) in red.
- 4. Linear regression. Download the file "Assig1Q4.csv" from the course GitHub repo under "Assignments/Assig1". The first column represents the X values, while the second column represents the Y values.
  - a. Plot the data
  - We are going to use linear regression to fit a linear and a cubic model to these data.
    <u>Without using sklearn.linear model</u> (or other linear regression libraries), write your own python code to implement the least squares solution for linear regression. That is:

$$\beta = (X^T X)^{-1} X^T y$$

- c. Assuming the model y = mx + b, use your code to best-fit the parameters m and b to the data. Report your optimal parameter values. Hints:
  - i. recall that you must create the 'augmented' feature vector X from the given x data (add a column of 1's).
  - ii. look at numpy.T(), numpy.matmul(), numpy.dot(), and numpy.linalg.inv()
- d. Plot your line of best fit on top of the data
- e. Calculate the mean squared error, as in:

$$MSE(\beta) = \frac{1}{N} \sum_{i=1}^{N} (y_i - x_i \beta)^2$$

- f. Assuming the model  $y = ax^3 + bx^2 + cx + d$ , repeat steps 2-4 using this new model (i.e. estimate the optimal values for a,b,c,d; report those estimates; plot the line of best fit; report the MSE).
- g. Briefly discuss which model would you prefer for these data?
- h. Why is best-fitting the second (cubic) model still considered linear regression?
- 5. Create a Jupyter Notebook based on Tutorial-3\_ComparingMultipleClassifiers.ipynb to use make\_classification to create a linearly separable dataset, with 2 classes, 2 informative features, the number of clusters per class to 1, 1500 samples per class, using a class\_sep=1.7, and a random\_state of 5. Generate some random noise of the same shape as your feature data, drawn from a standard normal distribution (see numpy.random) and a random\_state of 5.
  - a. Create four datasets: 1) no noise, 2) data + 0.5 \* noise, 3) data + 1.0 \* noise, and 4) data + 2.0 \* noise. For all four datasets, plot the data, labelling each (sub)plot by the degree of noise added (i.e. 0, 0.5, 1.0, and 2.0)
  - b. For each dataset, create training and test data using a 70/30 train/test split
  - c. For each dataset, train and test an SVM classifier with a polynomial kernel with degree=2, and C=1.0. Report the test score for each. How does prediction accuracy change with noise level?

d. For a noise level of 0.5, train and test SVM classifiers using the following values for C: {0.001, 0.01, 0.1, 1, 10, 100}. Report the test accuracy for each. How does performance vary with C? Briefly describe what the c controls for sklearn.svc. Hint: look at the documentation for sklearn.svc rather than the class notes here...