Task 1: Gradient Calculation Assignment

SYSC 4415

January 30, 2025

Problem Statement

Calculate the gradient of the function:

$$f(x, y, z) = e^{x^2} + y^y + e^{xy} + z\cos(x)$$

at point $(0, 1, 1)$

Helpful Derivative Rules

The following derivative rules may be useful:

Basic Function Derivatives

$$\frac{d}{dx}(a^x) = a^x \ln(a)$$
$$\frac{d}{dx}(\cos x) = -\sin x$$
$$\frac{d}{dx}(\sin x) = \cos x$$

Composite Function Derivatives

$$\frac{d}{dx}(a^{u(x)}) = a^{u(x)} \ln(a) \cdot \frac{d}{dx}u(x)$$
$$\frac{d}{dx}(x^x) = x^x(\ln x + 1)$$
$$\frac{d}{dx}(a^{xy}) = a^{xy} \ln(a) \cdot y \text{ (when differentiating with respect to x)}$$
$$\frac{d}{dy}(a^{xy}) = a^{xy} \ln(a) \cdot x \text{ (when differentiating with respect to y)}$$

Chain Rule

For a composite function $f(g(x))$:

$$\frac{d}{dx}f(g(x)) = f'(g(x)) \cdot g'(x)$$

Product Rule

For a product of functions $f(x)g(x)$:

$$\frac{d}{dx}[f(x)g(x)] = f'(x)g(x) + f(x)g'(x)$$