

Search Criteria	<u>BreadthFirst</u>	DepthFirst	IterativeDeepening
Completeness?	Yes	No	Yes
Optimality?	Yes	No	Yes
Time	$b^d$	$b^m$	$b^d$
Space	$b^d$ $(b^d)$	$(bm)$ $bm$	$(bd)$ $bd$

$b$  - maximum branching factor of the search tree

$d$  - depth of the least-cost solution

$m$  - maximum depth of state space (may be  $\infty$ )

### Properties of Greedy Best-First – without $g$

Complete ??

No, can get stuck in loops

Optimal??

No

Time complexity ??

$O(b^m)$

Space complexity ??

$O(b^m)$

keep all nodes in memory

### Properties of A\*

-  $h(n)$  never overestimate cost

Complete ??

Yes

Optimal??

Yes - if  $h(n)$  is both admissible & consistent for graph

Time complexity ??

$O(b^m)$

Space complexity ??

$O(b^m)$

keep all nodes in memory

Criteria	Characteristics
completeness	does it always find a solution if one exists?
optimality	does it always find a least-cost solution?
time complexity	number of nodes generated/expanded
space complexity	maximum number of nodes in memory

Main issue of A\* : run out of memory - not practical for many large scale problems

## Properties of Minimax

有限

**Complete ??** Yes, if tree is finite (Chess has specific rules)

**Optimal??** Yes, against an optimal opponent

**Time complexity ??**  $O(b^m)$

**Space complexity ??**  $O(b*m)$  (depth-first exploration)

Chess:  $b=35$ ,  $m=100$  for ‘reasonable’ games

⇒ Exact solution completely infeasible

But do we need to explore every path ?

⇒ Search efficiency is crucial

## Properties of Alpha-beta

Pruning **does not** affect final result

Good move ordering improves effectiveness of pruning

time  $b^{\frac{m}{2}}$

With “perfect ordering,” time complexity =  $O(b^{m/2})$

⇒ **doubles** solvable depth

A simple example of the value of reasoning about which computations are relevant (a form of **metareasoning**)

Unfortunately,  $35^{50}$  is still impossible!

When Brute Force Minimax/Alpha-Beta are no longer applicable, how could it possibly “plan” ahead when there are so many potential moves and counter moves in GO?

	complete	optimal	time	space
BFS	Yes	Yes	$b^d$	$b^d$
DFS	No	No	$b^m$	$b \cdot m$
IDS	Yes	Yes	$b^d$	$b \cdot d$
Greedy-BF	No	No	$b^m$	$b^m$
$A^*$	Yes	Yes	$b^m$	$b^m$ if heur. admissible
Minimax	Yes	Yes	$b^m$	$b \cdot m$ (≠ DFS)
$\alpha$ - $\beta$ prune	Yes	Yes	$b^{\frac{m}{2}}$	$b \cdot m$

