QUANTITATIVE RISK MANAGEMENT IN PYTHON

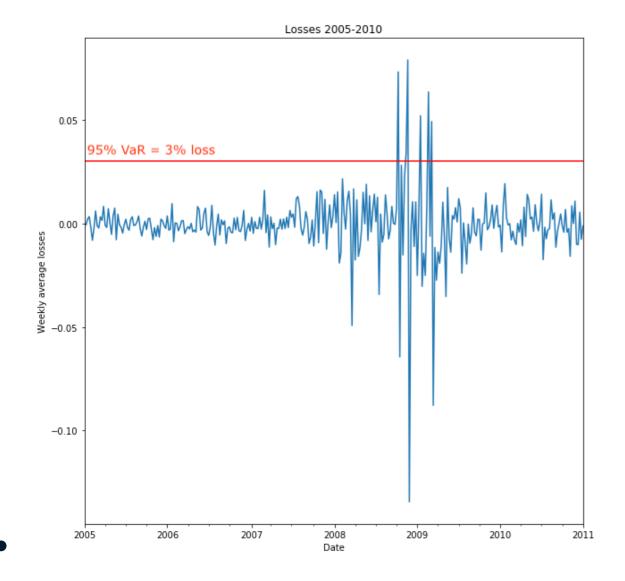


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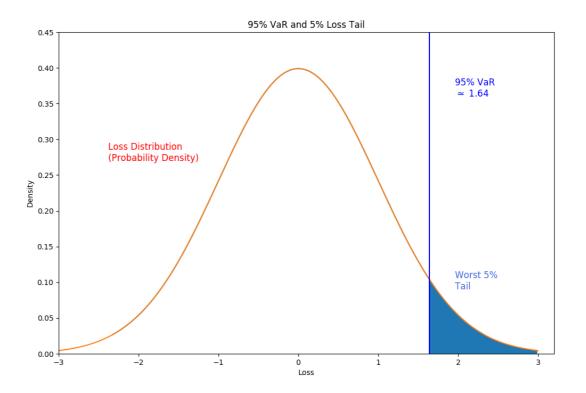


Extreme values

Portfolio losses: extreme values



- Extreme values: from tail of distribution
 - Tail losses: losses exceeding some value
 - Model tail losses => better risk management

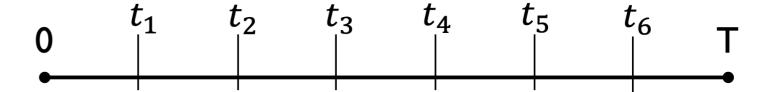




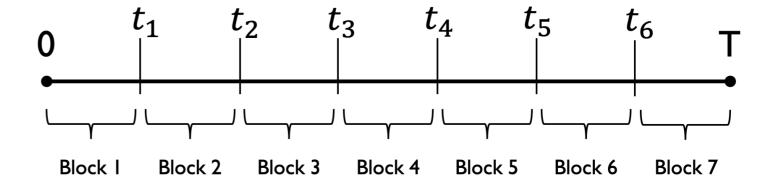
- Extreme value theory: statistical distribution of extreme values
- Block maxima



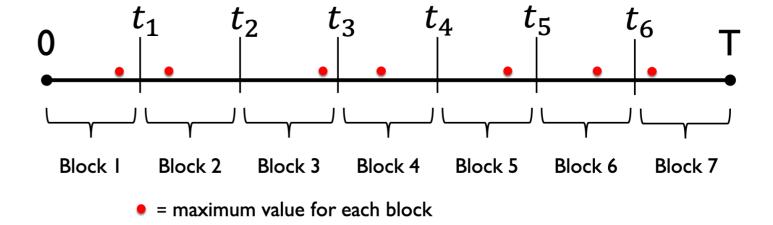
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- Block maxima:
 - Break period into sub-periods



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- Extreme value theory: statistical distribution of extreme values
- Block maxima:
 - Break period into sub-periods
 - Form blocks from each sub-period
 - Set of block maxima = dataset
- Peak over threshold (POT):
 - Find all losses over given level
 - Set of such losses = dataset



Generalized Extreme Value Distribution

- Example: Block maxima for 2007 2009
 - Resample losses with desired period (e.g. weekly)

```
maxima = losses.resample("W").max()
```

- Generalized Extreme Value Distribution (GEV)
 - Distribution of maxima of data
 - Example: parametric estimation using scipy.stats.genextreme

```
from scipy.stats import genextreme
params = genextreme.fit(maxima)
```

VaR and CVaR from GEV distribution

- 99% VaR from GEV distribution
 - Use .ppf() percent point function to find 99% VaR
 - Requires params from fitted GEV distribution
 - Finds maximum loss over one week period at 99% confidence
- 99% CVaR from GEV distribution
 - CVaR is conditional expectation of loss given VaR as minimum loss
 - Use .expect() method to find expected value

```
VaR_99 = genextreme.ppf(0.99, *params)
```

```
CVar_99 = (1 / (1 - 0.99)) * genextreme.expect(lambda x: x, *params, lb = VaR_99)
```

Covering losses

- Risk management: covering losses
 - Regulatory requirement (banks, insurance)
 - Reserves must be available to cover losses
 - For a specified period (e.g. one week)
 - At a specified confidence level (e.g. 99%)
- VaR from GEV distribution:
 - estimates maximum loss
 - given period
 - given confidence level

Covering losses

- **Example**: Initial portfolio value = \$1,000,000
- One week reserve requirement at 99% confidence
 - $\circ
 m VaR_{99}$ from GEV distribution: maximum loss over one week at 99% confidence
- Reserve requirement: Portfolio value x VaR_{99}
 - \circ Suppose VaR_{99} = 0.10, i.e. 10% maximum loss
 - Reserve requirement = \$100,000
- Portfolio value changes => reserve requirement changes
- Regulation sets frequency of reserve requirement updating

Let's practice!

QUANTITATIVE RISK MANAGEMENT IN PYTHON



Kernel density estimation

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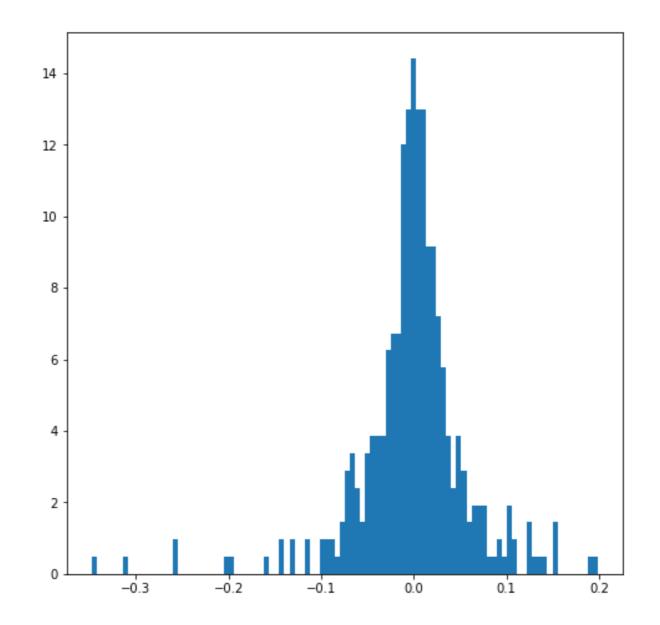


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The histogram revisited

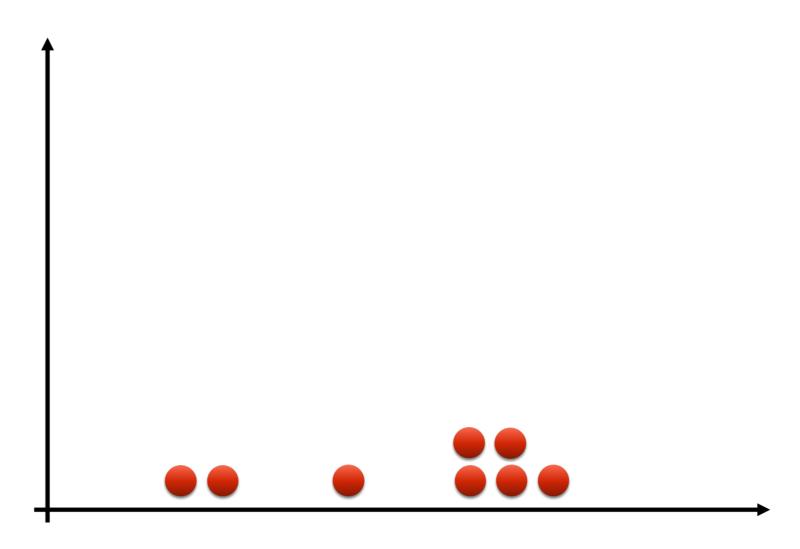
- Risk factor distributions
 - Assumed (e.g. Normal, T, etc.)
 - Fitted (parametric estimation, Monte Carlo simulation)
 - Ignored (historical simulation)
- Actual data: histogram
- How to represent histogram by probability distribution?
 - Smooth data using filtering
 - Non-parametric estimation



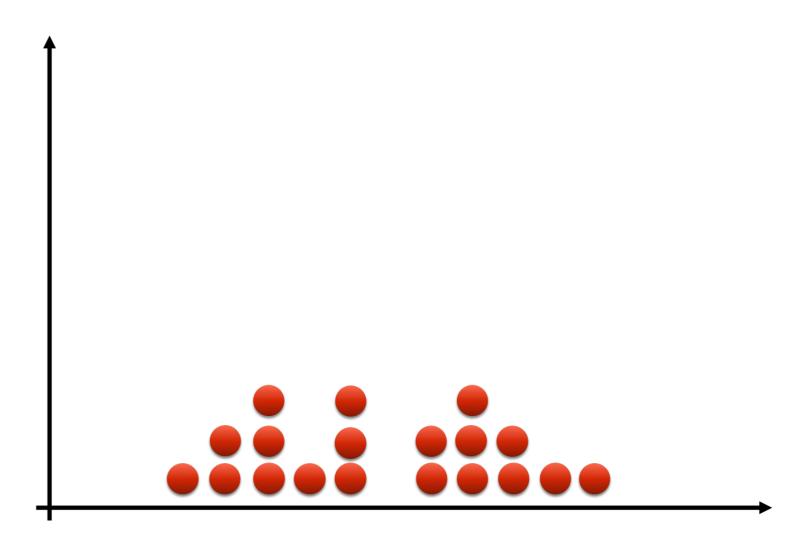
• Filter: smoothen out 'bumps' of histogram



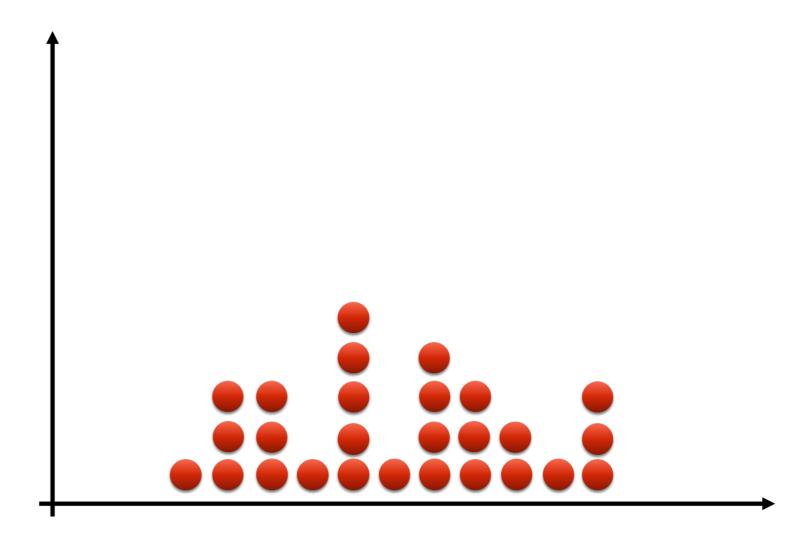
- Filter: smoothen out 'bumps' of histogram
- Observations accumulate in over time



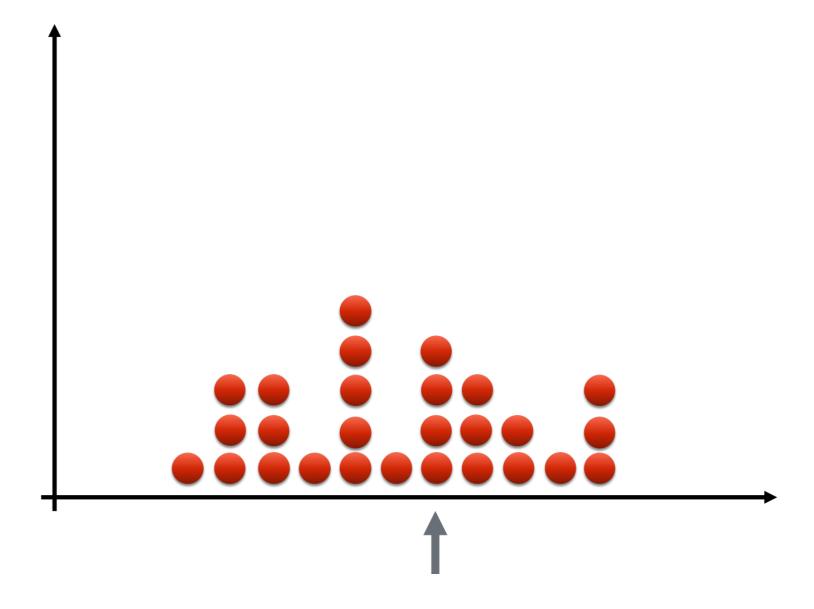
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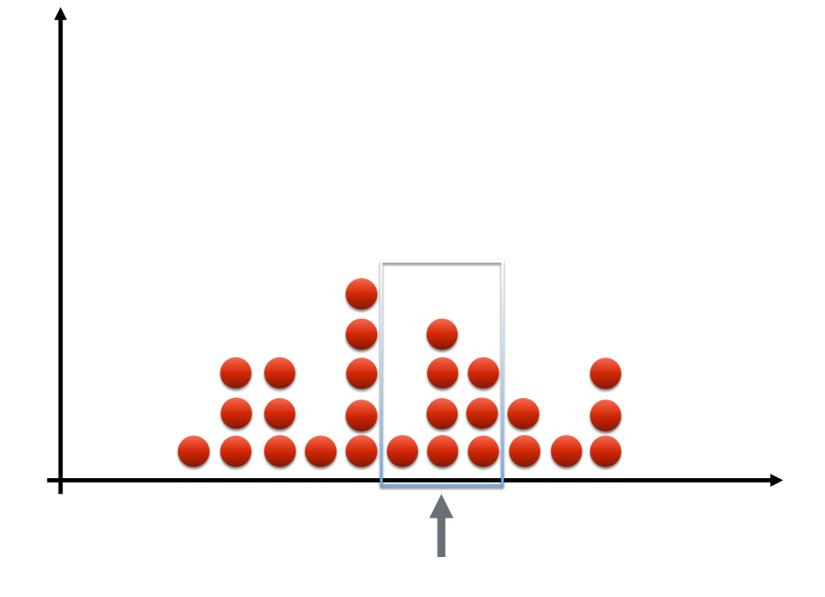
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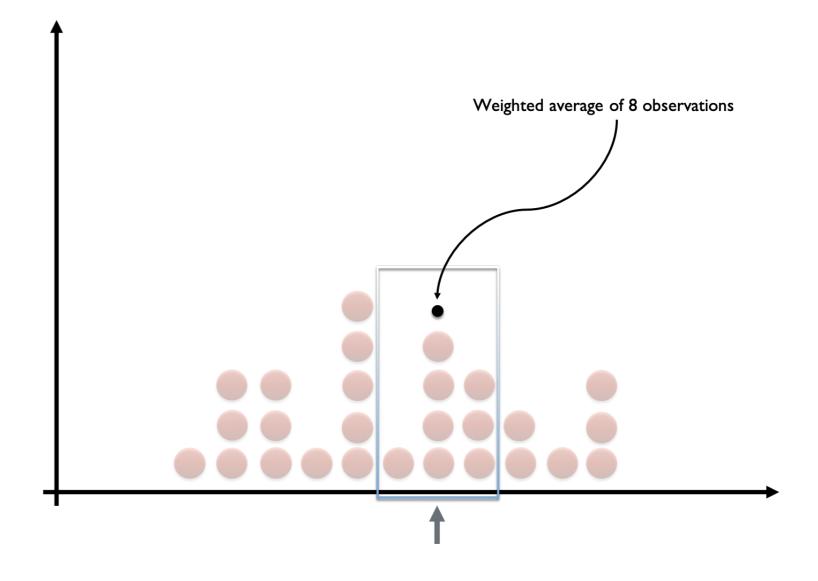
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- Pick particular portfolio loss



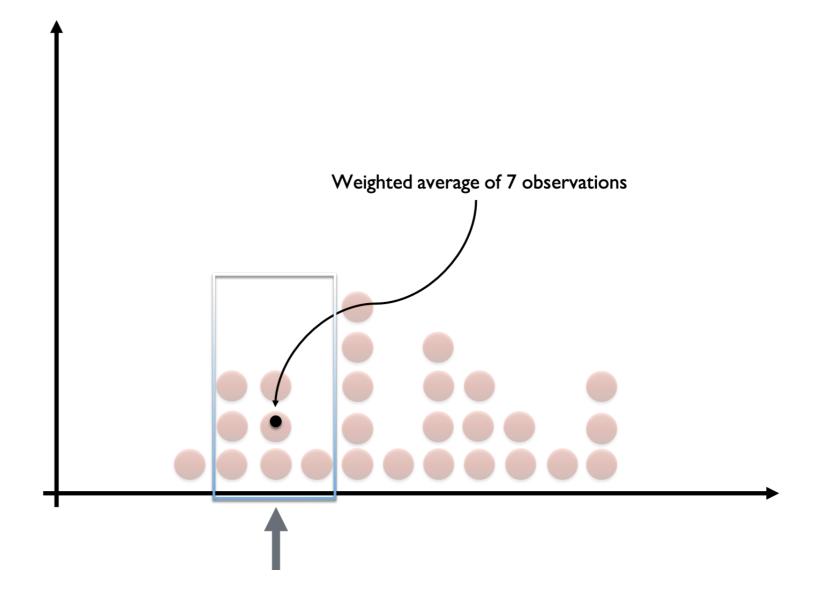
- Filter: smoothen out 'bumps' of histogram
- Observations accumulate in over time
- Pick particular portfolio loss
 - Examine nearby losses



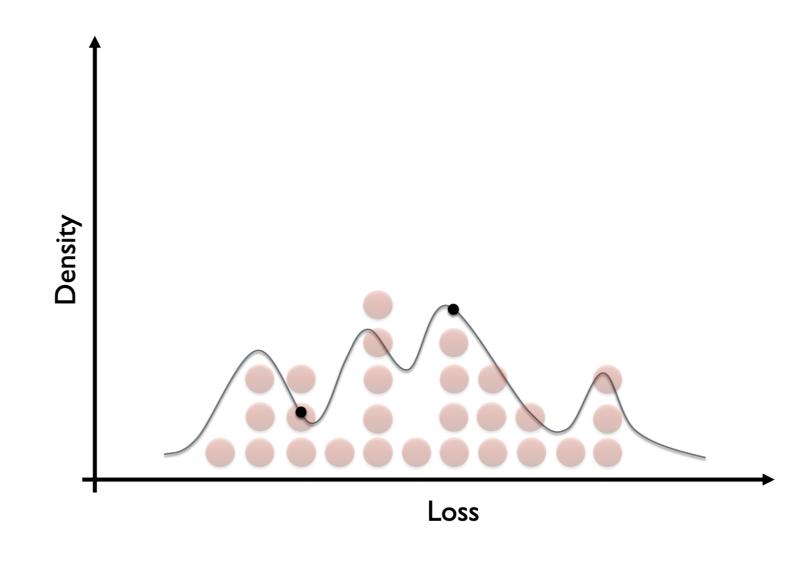
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 - Form "weighted average" of losses
- Kernel: filter choice; determines "window"



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 - Move window to another loss

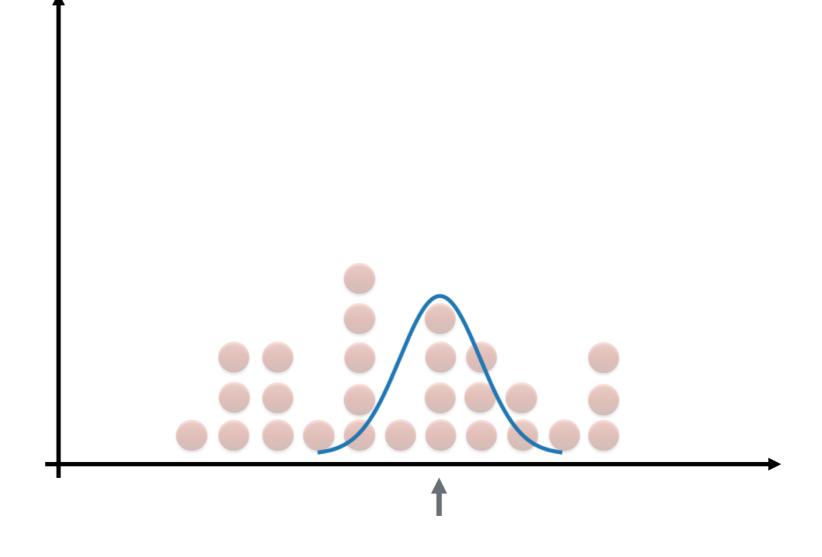


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- Kernel density estimate: probability density



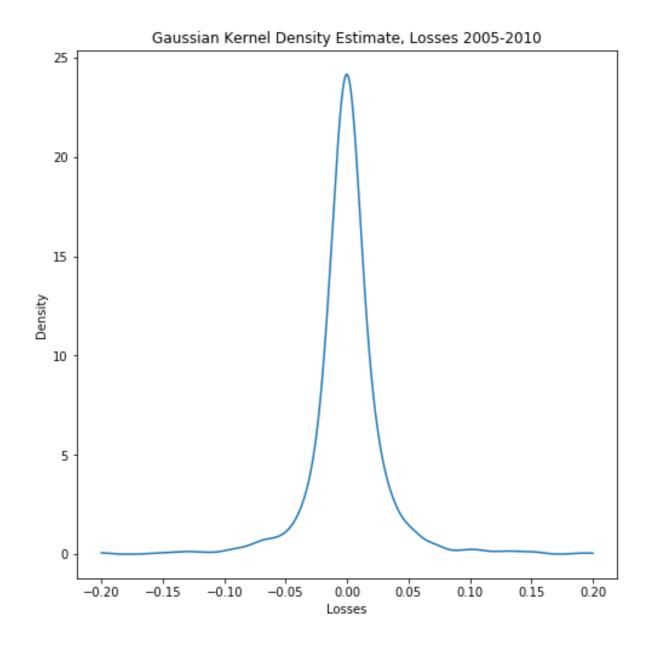
The Gaussian kernel

- Continuous kernel
- Weights all observations by distance from center
- Generally: many different kernels are available
 - Used in time series analysis
 - Used in signal processing



KDE in Python

 Visualization: probability density function from KDE fit





Finding VaR using KDE

- VaR: use gaussian_kde .resample() method
- Find quantile of resulting sample
- CVaR: expected value as previously encountered, but
 - gaussian_kde has no .expect() method => compute integral manually
 - o special .expect() method written for exercise

```
sample = kde.resample(size = 1000)
VaR_99 = np.quantile(sample, 0.99)
print("VaR_99 from KDE: ", VaR_99)
```

```
VaR_99 from KDE: 0.08796423698448601
```



Let's practice!

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Neural network risk management

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Real-time portfolio updating

- Risk management
 - Defined risk measures (VaR, CVaR)
 - Estimated risk measures (parameteric, historical, Monte Carlo)
 - Optimized portfolio (e.g. Modern Portfolio Theory)
- New market information => update portfolio weights
 - **Problem**: portfolio optimization costly
 - \circ Solution: weights = f(prices)
 - \circ Evaluate f in real-time
 - \circ *Update* f only occasionally

Neural networks

- Neural Network: output = f(input)
 - Neuron: interconnected processing node in function
- Initially developed 1940s-1950s
- Early 2000s: application of neural networks to "big data"
 - Image recognition, processing
 - Financial data
 - Search engine data
- Deep Learning: neural networks as part of Machine Learning
 - o 2015: Google releases open-source Tensorflow deep learning library for Python

- Layers: connected processing neurons
 - Input layer

Layers

Input





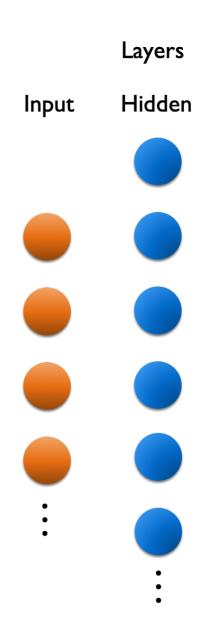




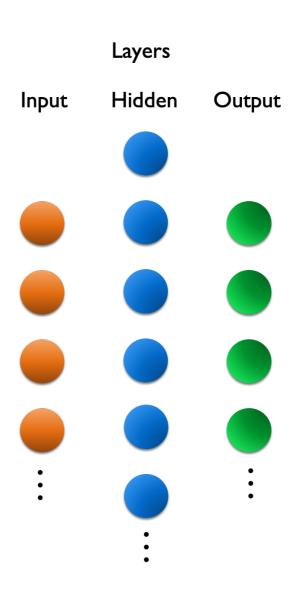
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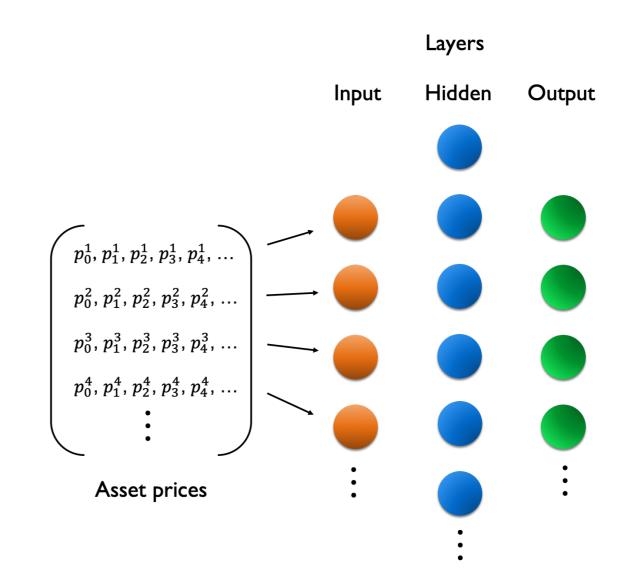
- Neural network structure
 - Input layer
 - Hidden layer



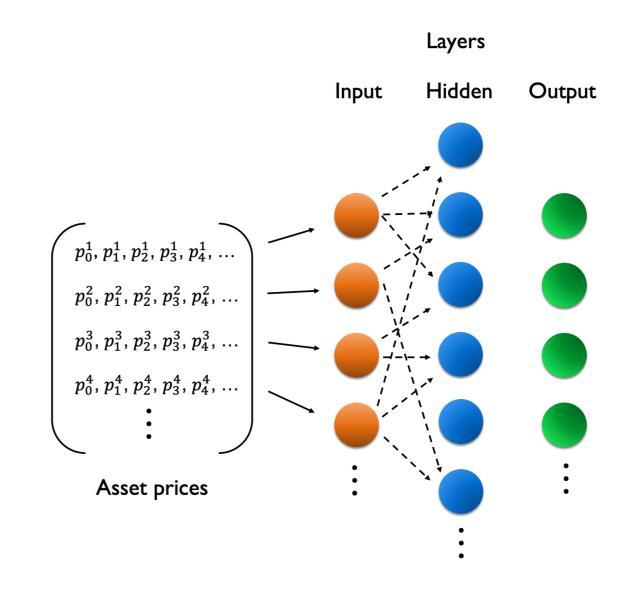
- Neural network structure
 - Input layer
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 - Output layer
- Training: learn relationship between input and output



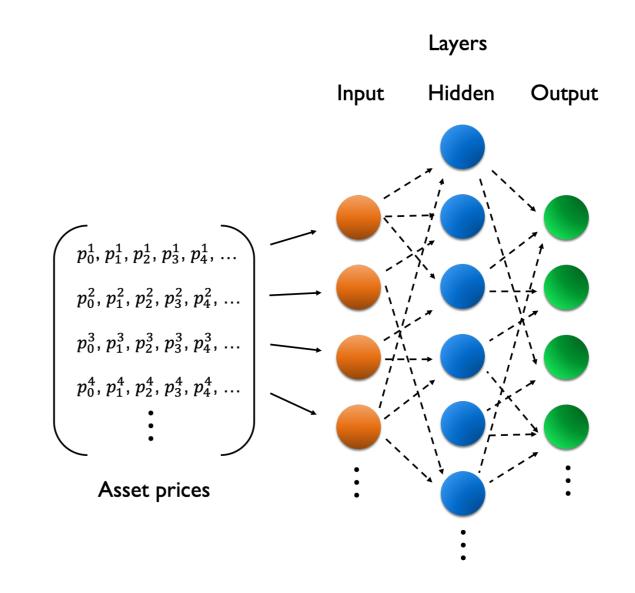
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 - Asset prices => Input layer



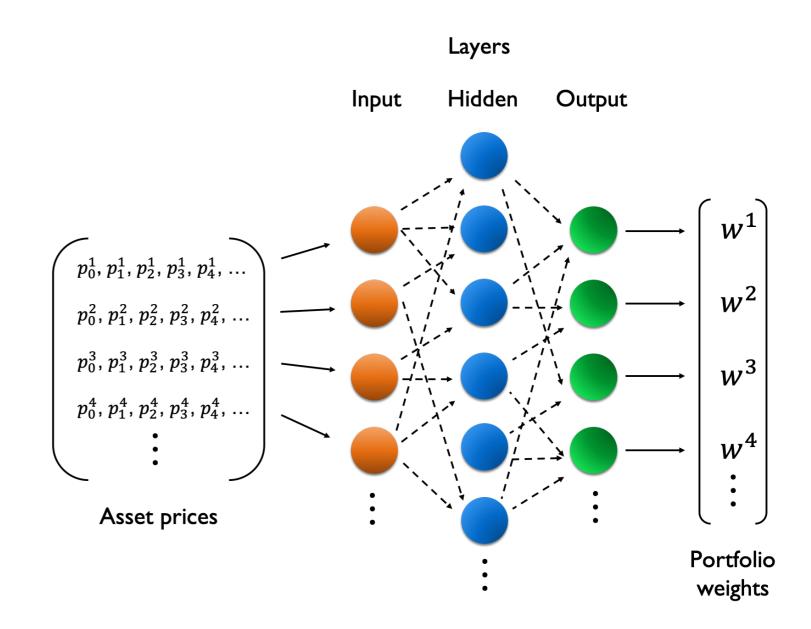
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 - Hidden + output layer processing
 - Output => portfolio weights



Using neural networks for portfolio optimization

Training

- Compare output and pre-existing "best" portfolio weights
- Goal: minimize "error" between output and weights
- Small error => network is trained

Usage

- Input: new, unseen asset prices
- Output: predicted "best" portfolio weights for new asset prices
- Best weights = risk management

Creating neural networks in Python

- Keras: high-level Python library for neural networks/deep learning
- Further info: Introduction to Deep Learning with Keras

```
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense
model = Sequential()
model.add(Dense(10, input_dim=4, activation='sigmoid'))
model.add(Dense(4))
```

Training the network in Python

- Historical asset prices: training_input matrix
- Historical portfolio weights: training_output vector
- Compile model with:
 - given error minimization ('loss')
 - given optimization algorithm ('optimizer')
- Fit model to training data
 - o epochs: number of training loops to update internal parameters

```
model.compile(loss='mean_squared_error', optimizer='rmsprop')
model.fit(training_input, training_output, epochs=100)
```

Risk management in Python

- Usage: provide new (e.g. real-time) asset pricing data
 - New vector new_asset_prices given to input layer
- Evaluate network using model.predict() on new prices
 - Result: predicted portfolio weights
- Accumulate enough data over time => re-train network
 - Test network on previous data => backtesting

```
# new asset prices are in the vector new_asset_prices
predicted = model.predict(new_asset_prices)
```



Let's practice!

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Wrap-up and Future Steps

QUANTITATIVE RISK MANAGEMENT IN PYTHON



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Chapter I

Risk and Return Recap

Return Distribution

Risk Factors

Volatility & Covariance

Modern Portfolio Theory

Efficient Portfolio & Efficient Frontier



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Kernel Density Estimation

Neural Networks

Real-time risk management



Tools in your toolkit

Scipy	Statsmodels	PyPortfolioOpt	Keras
scipy.stats	statsmodels.api	pypfopt	keras
norm()	OLS()	risk_models	models
skewnorm()	add_constant()	cla	layers
t()	.fit()	expected_returns	Sequential()
genextreme()		efficient_frontier	Dense()
<pre>gaussian_kde()</pre>		objective_functions	.add()
anderson()		EfficientFrontier()	.fit()
skewtest()		<pre>mean_historical_return()</pre>	.predict()
.pdf()		CovarianceShrinkage()	
.ppf()		<pre>.negative_cvar()</pre>	
.fit()		.CLA()	
.rvs()		<pre>.ledoit_wolf()</pre>	



Future steps and reference

- Upcoming DataCamp courses
 - Credit Risk Modeling in Python
 - Financial Forecasting in Python
 - Machine Learning for Finance in Python
 - GARCH Models for Finance in Python
- Quantitative Risk Management: Concepts, Techniques and Tools, McNeil, Frey & Embrechts, Princeton UP, 2015.

Best of luck on your data science journey!

QUANTITATIVE RISK MANAGEMENT IN PYTHON

