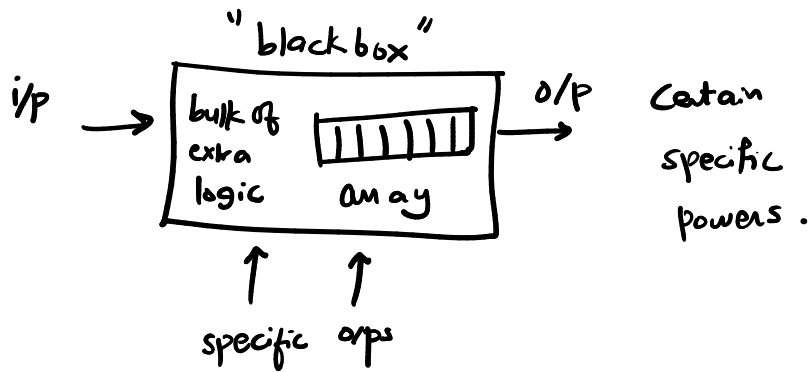


- Today → Arrays ↖
1. leetcode problem 3 → sliding window / set. \*
  2. leetcode problem 76 → sliding window / map. \*\*
  3. leetcode problem 4 → Median of 2 sorted arrays | BS \*\*\*

4. Abstract Data Type | Containers → set, map, queue, stack, heap.



everyone is using an array.

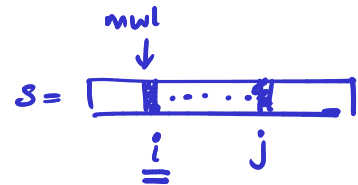
Problem :  $s = \text{"adobecodebanc"}$   $t = \text{"abc"}$  shortest substring such that all chars of  $t$  are in substring.

map.  $s = \text{"abab"}$   $t = \text{"aa"}$  4 substrings. shortest: "banc" o/p

o/p: "aba"

Sol<sup>n</sup>: 1.  $t = \text{"abc"}$  map of this t-string:  $t\_freq$

$t\_freq: \{a:1, b:1, c:1\}$



2. required\_unique = 3

store the no of unique chars that are required in t and are available in window.

3. window\_freq = {}, window\_size = 0

4. min\_window\_left = 0, min\_len = 10e6

5.  $i = j = 0$

"abode" window = 2 . size

$s = \text{"adobecodebanc"}$

keep on going right. → window\_freq

window size.

$t = \text{"abc"}$   $\{a:1, b:1, c:1\}$

$j=0$   $c=a$   $\{a:1\}$  1

$j=1$   $c=d$   $\{a:1, d:1\}$  1

$j=3$   $c=b$   $\{a:1, d:1, o:1, b:1\}$  2

$$j=5 \quad c=c$$

{ a:1  
d:1  
o:1 } { b:1  
e:1  
c:1 }

3

Window-size == required-unique

$$\text{min\_len} = (10^6, 6) = 6$$

shed elements from i.

i=0 ~~α~~ { d:1  
o:1 } { b:1  
e:1  
c:1 } 2

Continue to add elements from right.

j=6 c='o' { d:1  
o:2 } { b:1  
e:1  
c:1 } 2

j=10 c="a" { ... } 3

$$\begin{aligned} \text{min\_len} &= (6, 10-1+1) \\ &= (6, 10) \\ &= \underline{\underline{6}} \end{aligned}$$

∴ j=n

min\_string\_left = i

s.substr(i, minlen)

Q.3. Median of 2 sorted arrays. (Don't want to merge it).

ans1  
m: 1 3 7 9 11 15 18 → 7  
ans2  
n: 2 4 13 21 25 → 5 } unequal sizes.

Assuming if they were merged:

sorted → [ 0 1 2 3 4 5 6 ]  
[ 1 2 3 7 9 9 11 ]  
If 25 X, median = 9.

odd → mid  
even → avg(2 mids)  
7 8 9 10 11  
13 15 18 21 25 }  
median =  $\frac{9+11}{2} = \underline{\underline{10}}$  ans. 6

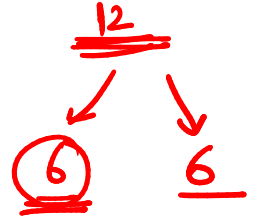
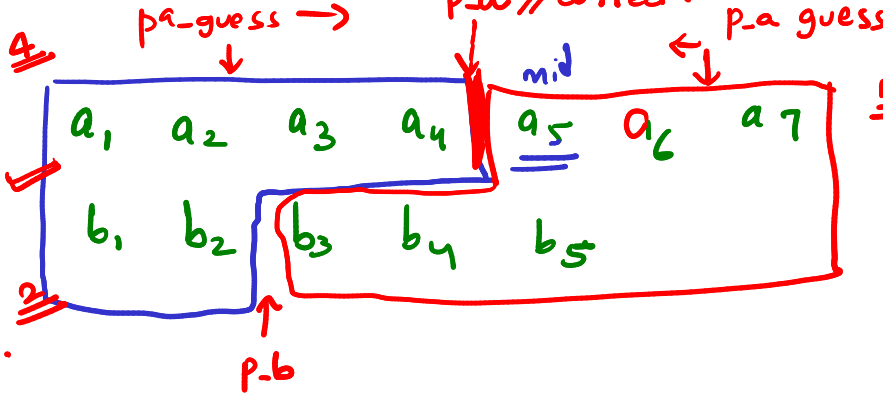
BF:  $O(m+n)$  linear TC  $m+n$  

Optimize:  $O(\log(m, n))$   $\log$  TC

$p-a$   $p-b \Rightarrow$  indices

an1:  $m = 7$   $mid = \frac{m+n}{2} = \frac{12}{2} = \underline{\underline{6}}$

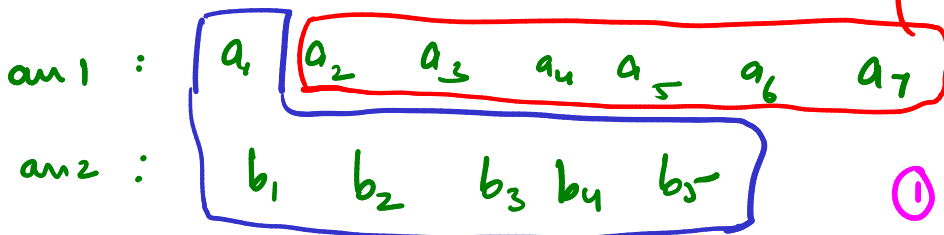
an2:  $n = 5$



$p-a + p-b = \frac{m+n}{2}$

$p-a \rightarrow$  guess here. range: 0 to  $m-1 \leftarrow p-a$

$p-b = \left(\frac{m+n}{2}\right) - p-a$

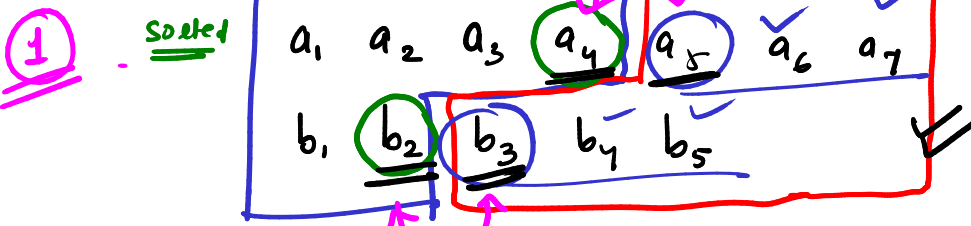


3 unknowns.

$p-a \rightarrow$  guess

① How will I know this  $p-a$  is correct?

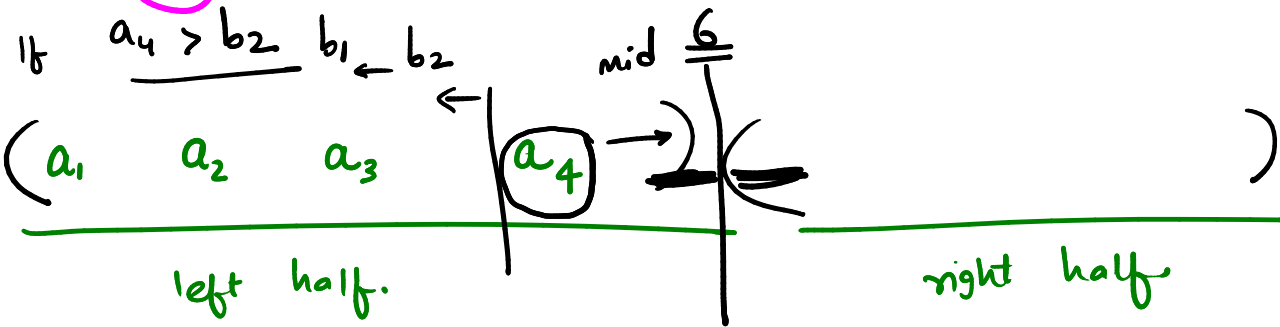
② If  $p-a$  is wrong, figure out  $\Rightarrow$  overestimating OR underestimating?



Is this correct?

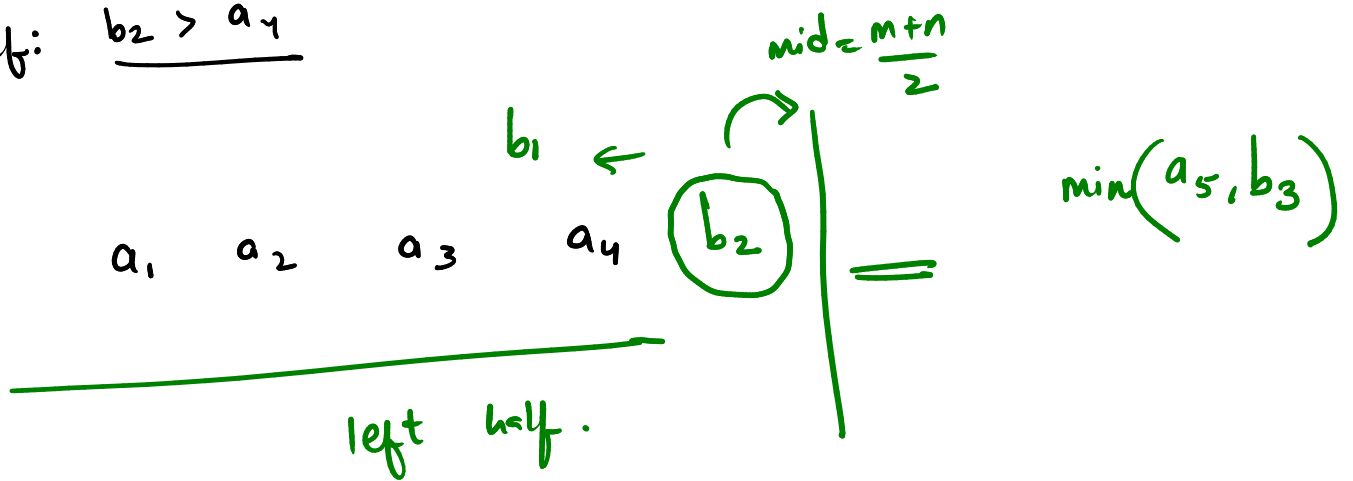
$a_4 \leftrightarrow b_3$   
 $b_2 \leftrightarrow a_5$

Assume it:  
I did



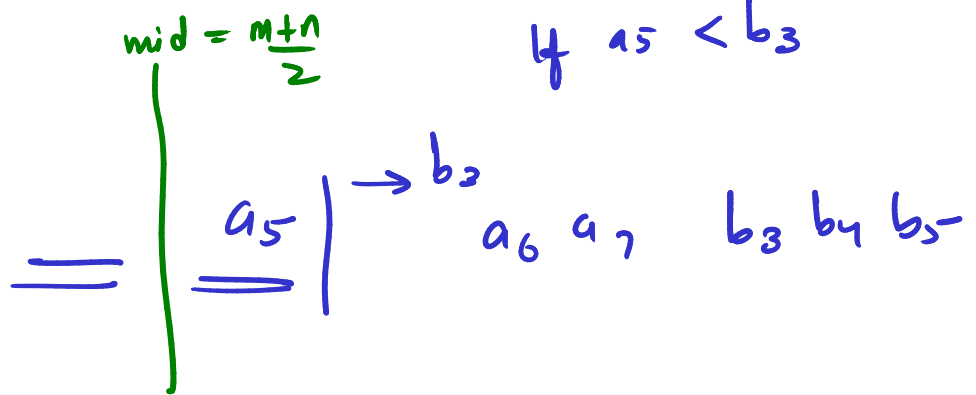
$b_1, a_1, a_2, b_4, a_3, a_4$   
 $a_1, a_2, a_3, b_1, b_2, a_4$

If:  $b_2 > a_4$



mid-left-half  $\max(a_4, b_2)$

Same logic on RHS.



Logic:

✓✓ guess-work:  $p_a = 4$   
 $p_b = 6 - 4 = 2$

mid-elements of the merged array are:

$\max(a[p_a], b[p_b]), \min(a[p_a+1], b[p_b+1])$

Comparisons

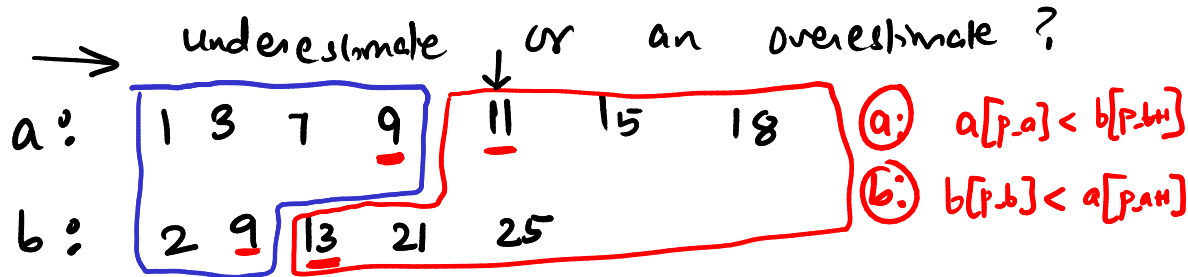
$a_4 < a_5 \rightarrow \text{Trivial}$   
 $b_2 < b_3 \rightarrow \text{Trivial}$

$a$  is sorted x  
 $b$  is sorted

non-trivial  
 $p_a$  is correct split !!  
 $\left\{ \begin{array}{l} a_4 < b_3 \\ b_2 < a_5 \end{array} \right\} \rightarrow \text{This must be true because}$   
 blue  $\rightarrow$  left half      red  $\rightarrow$  right half.

What happens

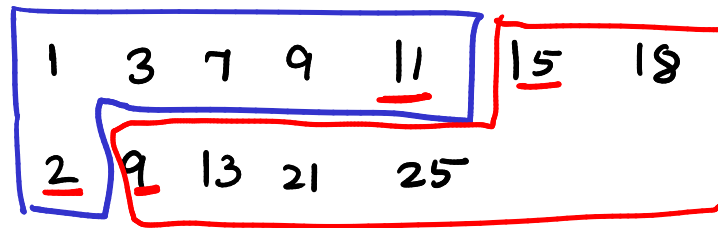
Typical ;  
example



$9 < 13$  ✓

$9 < 11$  ✓

5 elements  
from a :

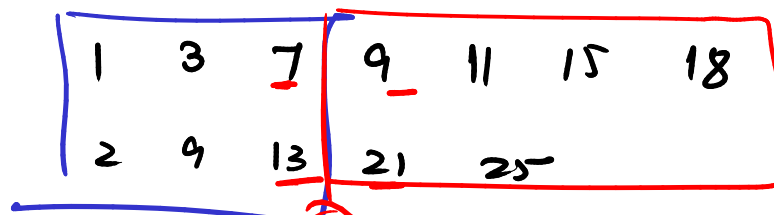


$11 < 9$  ✗ (a)

$2 < 15$  ✓

Overestimating ← (a) ✗  $a[p_a] < b[p_b+1]$

3 elements  
from a :



✓  $7 < 21$  (a)

✗  $13 < 9$  ✗ (b)

Underestimating ← (b) ✗  $b[p_b] < a[p_a+1]$

low      high  
 $p_a$  : 0      to       $m-1$

←  $p_b = \frac{m+n}{2} - p_a$

cond? a

✓

✗

✓

cond? b

✓

✓

✗

→  $p_a$  is right

→  $p_a \downarrow$

→  $p_a \uparrow$

$p_b$  = automatically fixed.

median =  $\max(a[p_a], b[p_b])$

$p_a$  is right ✓      median → odd

median =  $\frac{\max(a[p_a], b[p_b]) + \min(a[p_a+1], b[p_b+1])}{2}$