

BT6270: Computational Neuroscience Assignment 1

EE20B149
Varun M

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1 Introduction

The Hodgkin-Huxley model explains how the dynamics of ion channels (Na⁺, K⁺ etc) contribute to the generation of an Action Potential in a neuron.

An Action Potential is a sharp voltage spike elicited by stimulating a neuron with a current that exceeds a certain threshold value. The current amplitude is increased gradually, at a threshold amplitude, the voltage response does not increase proportionally.

It shows a sharp, disproportionate increase.

Once the membrane voltage reaches a threshold value, it increase further rapidly to maximum value and drops again rapidly to a value that is less than resting value, before returning to the baseline value after a delay.

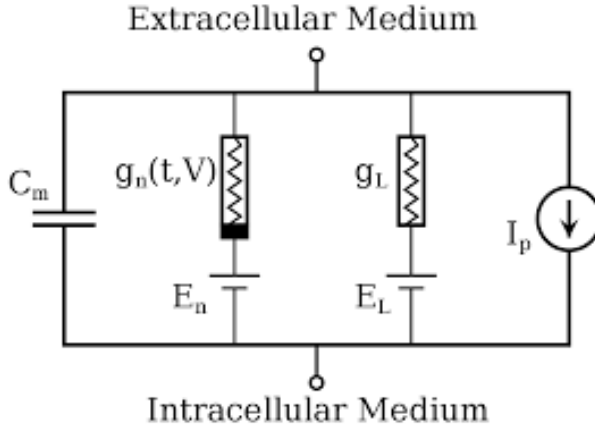


Figure 1: Hodgkin-Huxley model circuit

2 Neural Firing Frequencies and Thresholding

2.1 Threshold Values of External Current

The Threshold Currents are as follows:

- $I_1 = 0.023 \mu A/mm^2$
- $I_2 = 0.0615 \mu A/mm^2$
- $I_3 = 0.458 \mu A/mm^2$

These values were obtained by setting the sampling interval to 0.001 between [0,0.6]. The value of 0.6 is chosen after hit and trial on the MATLAB code and analyzing the Voltage vs Time graph. All the I_1 , I_2 and I_3 values don't exceed more than 0.6.

2.2 Assumptions

Assumptions for the plot are as follows:

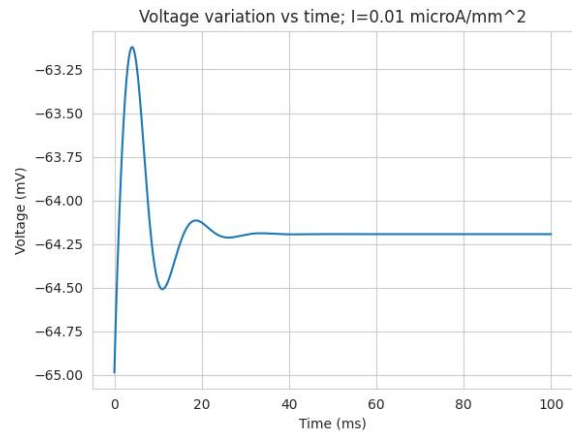
- A peak must exceed a threshold voltage of **5 mV** in order to be classified as an action potential.
- I1 is calculated at the initial non-zero value of the number of Voltage Peaks.
- I2 is calculated at the input current value where the following current instant has **3** or more voltage peaks exceeding **5 mV**.
- I3 is calculated as the input current value at which there are **7** or more voltage peaks above 5 mV in the next current instant.

2.3 Plots

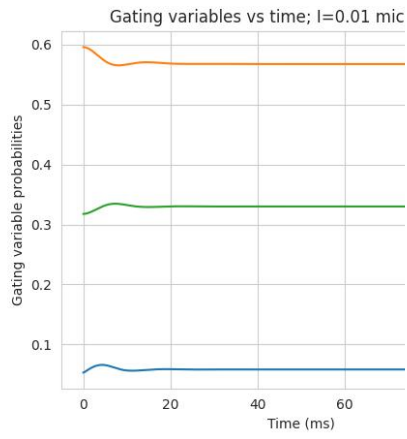
2.3.1 Frequency vs Input current

- As we can see in the obtained plots, we start getting periodic action potentials from $0.0224\mu\text{A}$ to $0.5432\mu\text{A}$.
- Thus we can obtain a frequency vs input current plot for the same. The frequency will be zero initially till $0.0224\mu\text{A}$.
- After that we get a frequency value at $0.0224\mu\text{A}$ and it increases till the input current is increased till $0.5432\mu\text{A}$.
- After $0.5432\mu\text{A}$ again we get zero frequency as we do not have action potentials.

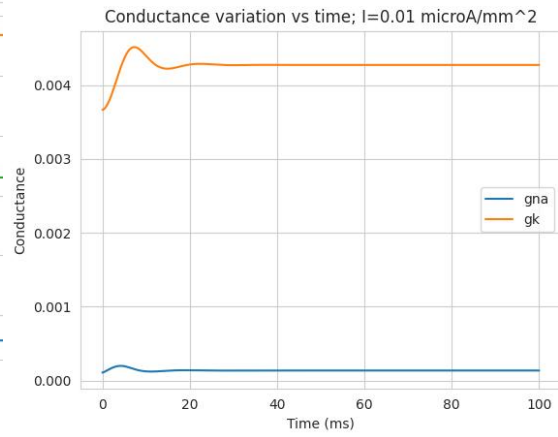
2.3.2 Region 1



(a) Plot of Voltage vs Time for $I=0.01\mu\text{A}$

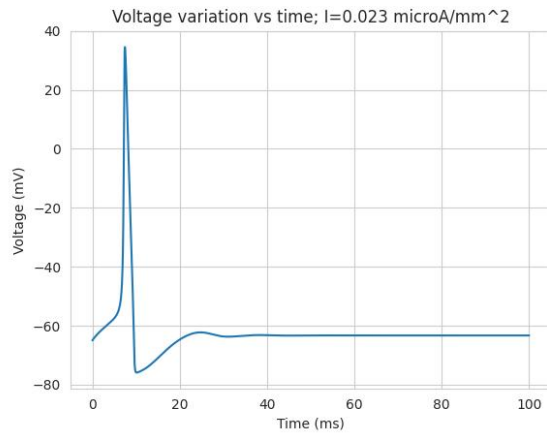


(b) Plot of gating variables for $I=0.01\mu\text{A}$

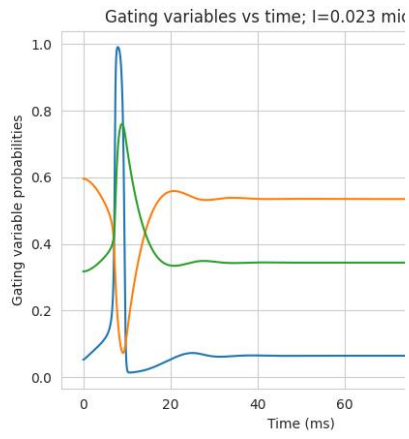


(c) Plot of conductances for $I=0.01\mu\text{A}$

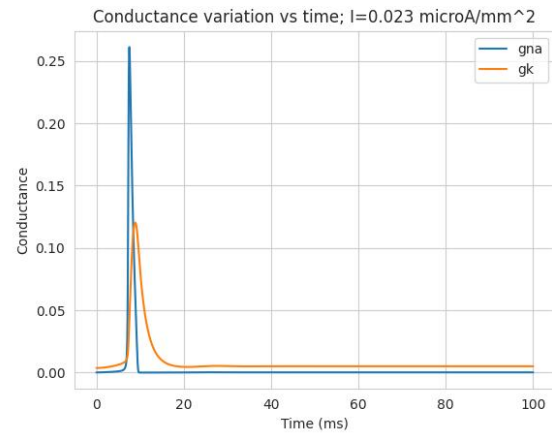
2.3.3 Region 2



(a) Plot of Voltage vs Time for $I=0.023\mu A$

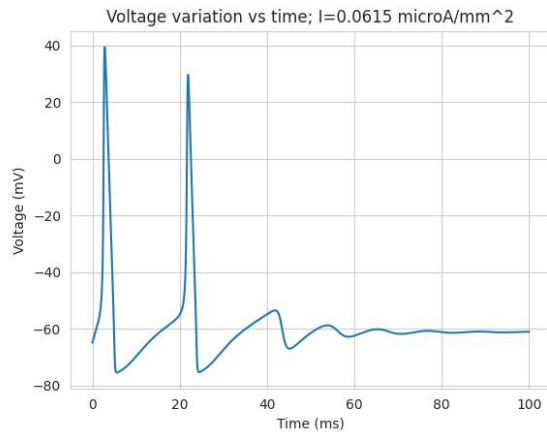


(b) Plot of gating variables for $I=0.023\mu A$

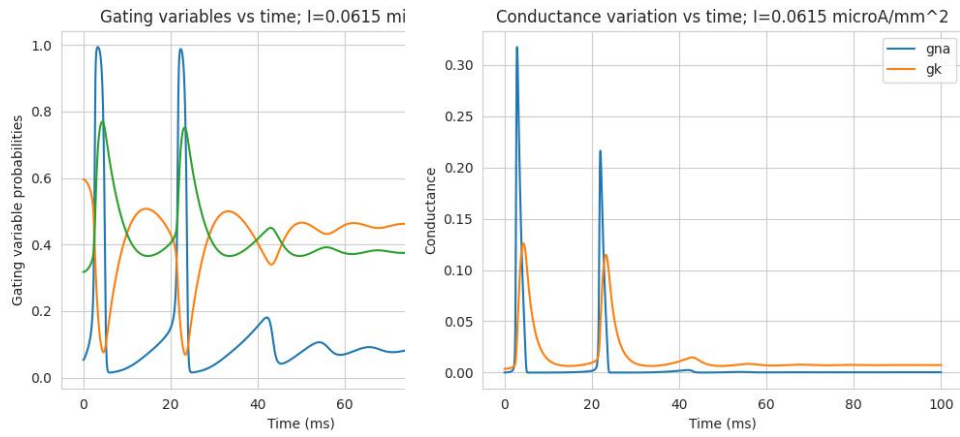


(c) Plot of conductances for $I=0.023\mu A$

2.3.4 Region 3



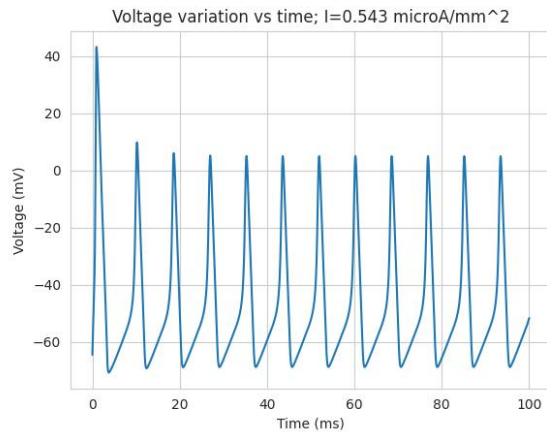
(a) Plot of Voltage vs Time for $I=0.0615 \mu\text{A}$



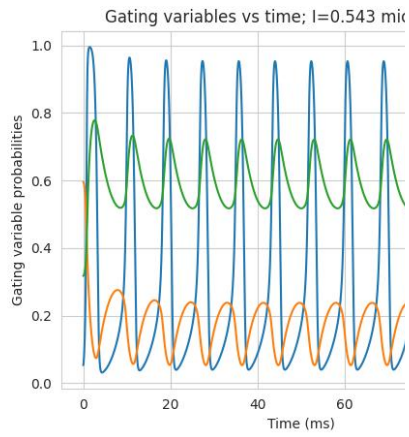
(b) Plot of gating variables for $I=0.0615 \mu\text{A}$

(c) Plot of conductances for $I=0.0615 \mu\text{A}$

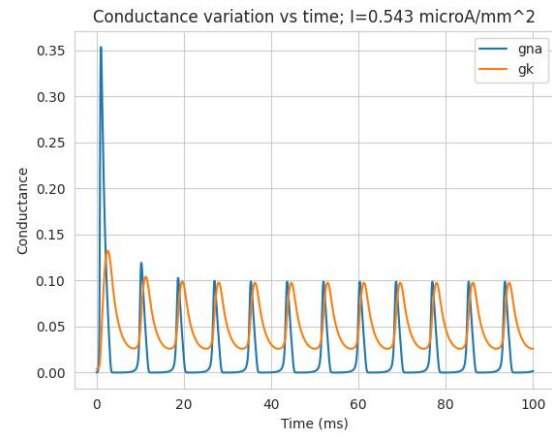
2.3.5 Region 4



(a) Plot of Voltage vs Time for $I=0.543\mu\text{A}$

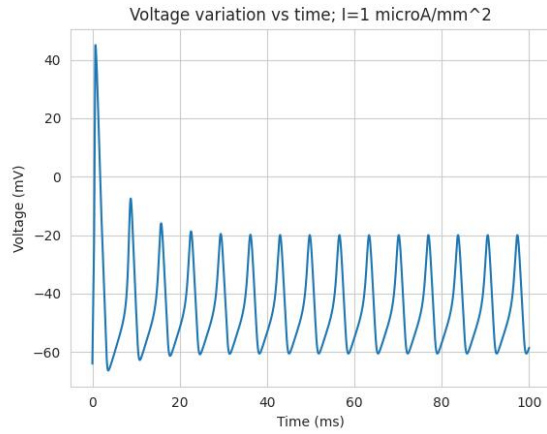


(b) Plot of gating variables for $I=0.543\mu\text{A}$

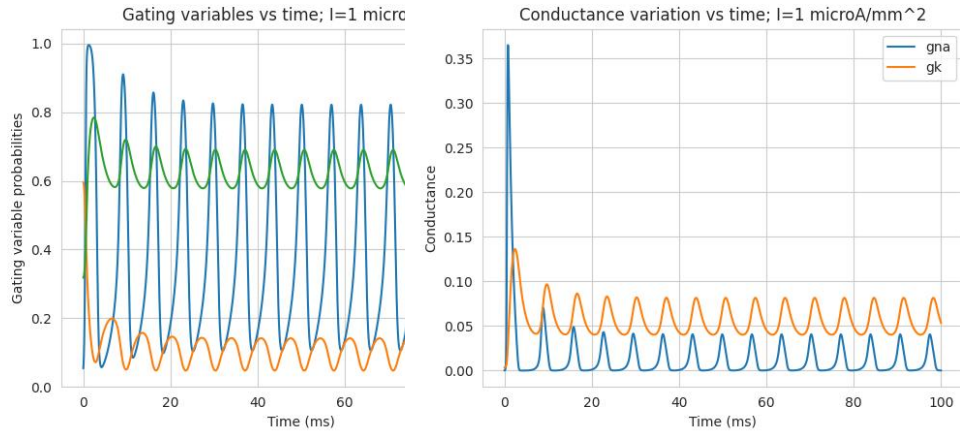


(c) Plot of conductances for $I=0.543\mu\text{A}$

2.3.6 Region 5



(a) Plot of Voltage vs Time for $I=1\mu\text{A}$



(b) Plot of gating variables for $I=1\mu\text{A}$ (c) Plot of conductances for $I=1\mu\text{A}$

3 Frequency vs Input current plot

We have zero frequency before and after Region 3.

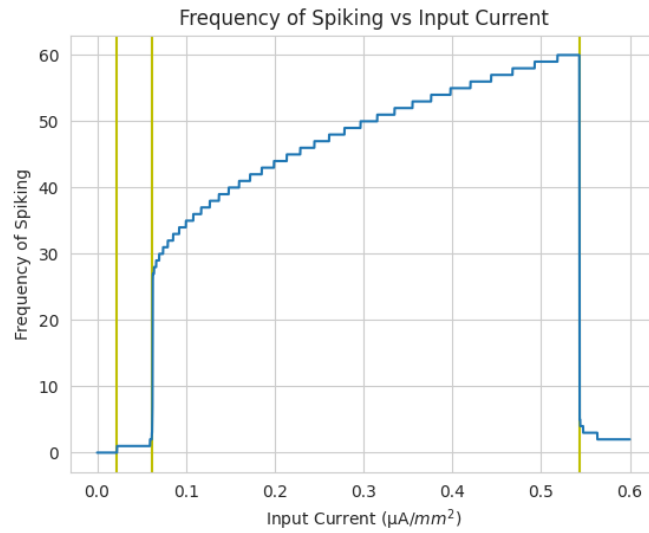


Figure 7: Frequency vs Input current plot