## Problem Set 2

#### Applied Stats II

Due: February 19, 2023

## Instructions

- Please show your work! You may lose points by simply writing in the answer. If the problem requires you to execute commands in R, please include the code you used to get your answers. Please also include the .R file that contains your code. If you are not sure if work needs to be shown for a particular problem, please ask.
- Your homework should be submitted electronically on GitHub in .pdf form.
- This problem set is due before 23:59 on Sunday February 19, 2023. No late assignments will be accepted.

#### Code in PS2\_ImeldaFinn.R

We're interested in what types of international environmental agreements or policies people support (Bechtel and Scheve 2013). So, we asked 8,500 individuals whether they support a given policy, and for each participant, we vary the (1) number of countries that participate in the international agreement and (2) sanctions for not following the agreement.

Load in the data labeled climateSupport.csv on GitHub, which contains an observational study of 8,500 observations.

```
load(url("https://github.com/ASDS-TCD/StatsII_Spring2023/blob/main/
datasets/climateSupport.RData?raw=true"))

# choice = 1,2
# countries = 1, 2, 3
# sanctions = 1, 2, 3, 4

csFacs <- climateSupport
csFacs$choice <- relevel(csFacs$choice, "Supported")</pre>
```

- Response variable:
  - choice: 1 if the individual agreed with the policy; 0 if the individual did not support the policy

- Explanatory variables:
  - countries: Number of participating countries [20 of 192; 80 of 192; 160 of 192]
  - sanctions: Sanctions for missing emission reduction targets [None, 5%, 15%, and 20% of the monthly household costs given 2% GDP growth]

Please answer the following questions:

1. Remember, we are interested in predicting the likelihood of an individual supporting a policy based on the number of countries participating and the possible sanctions for non-compliance.

Fit an additive model.

```
1 mod <- glm(choice ~., family = binomial(link="logit"),</pre>
```

(a) Provide the summary output,

```
Call:
      glm(formula = choice ~ ., family = binomial(link = "logit"), data
2
       = csFacs)
      Deviance Residuals:
                      1Q
                           Median
                                          3Q
                                                   Max
       -1.4259
                 -1.1480
                           -0.9444
                                      1.1505
                                                1.4298
       Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
       (Intercept) -0.005665
                                 0.021971
                                            -0.258 \ 0.796517
10
      countries.L
                     0.458452
                                 0.038101
                                            12.033
                                                    < 2e-16 ***
       countries.Q -0.009950
                                 0.038056
                                            -0.261 \ 0.793741
12
      \operatorname{sanctions.L} -0.276332
                                 0.043925
                                             -6.291 \ 3.15 e -10 ***
13
      sanctions.Q -0.181086
                                 0.043963
                                             -4.119 \quad 3.80 \,\mathrm{e}{-05} \quad ***
      sanctions.C 0.150207
                                 0.043992
                                             3.414 0.000639 ***
       Signif. codes:
                        0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' 1
18
       (Dispersion parameter for binomial family taken to be 1)
19
20
      Null deviance: 11783 on 8499 degrees of freedom
       Residual deviance: 11568 on 8494 degrees of freedom
      AIC: 11580
23
      Number of Fisher Scoring iterations: 4
26
27
```

(b) the global null hypothesis:

 $H_0$ : the explanatory variables have no effect on the likelihood of an individual supporting a policy

 $H_a$ : one or more of the explanatory variables have some effect on the likelihood of an individual supporting a policy

 $\alpha = 0.05$ 

(c) and p-value. The model was run with no explanatory variables (dummy... TODO). The comparison of the two models is shown in ??



Table 1:

	$\_$ Depender	nt variable:
	ch	oice
	(1)	(2)
countries.L	-0.458***	
	(0.038)	
$\operatorname{countries.Q}$	0.010	
	(0.038)	
sanctions.L	0.276***	
	(0.044)	
$\operatorname{sanctions.Q}$	0.181***	
	(0.044)	
sanctions.C	-0.150***	
	(0.044)	
Constant	0.006	0.007
	(0.022)	(0.022)
Observations	8,500	8,500
Log Likelihood	-5,784.130	-5,891.7
Akaike Inf. Crit.	11,580.260	11,785.4
$\overline{Note}$ :	*p<0.1; **p<0	0.05; ***p<

Table 2:

Statistic	N	Mean	St. Dev.	Min	Max
Resid. Df	2	8,496.500	3.536	8,494	8,499
Resid. Dev	2	11,675.830	152.134	$11,\!568.260$	11,783.410
Df	1	5.000		5	5
Deviance	1	215.150		215.150	215.150

(d) Please describe the results and provide a conclusion.

Table 3

The  $e^{\beta_k}$ s are all non-zero and the 5% Confidence Intervals do not include 0.(Table 3 The estimates for  $\beta_k$  are all significant at p=0.01 except for countries.Q, ie there is no significant difference in likelihood going from 80 to 160 countries.





Table 3:

	lower	estimate	upper
intercept	c('(Intercept)' = 0.9633)	c('(Intercept)' = 1.0057)	c('(Intercept)' = 1.0499)
countries 80	c(countries.L=0.5867)	c(countries.L = 0.6323)	c(countries.L=0.6812)
countries 160	c(countries.Q=0.9374)	c(countries.Q=1.01)	c(countries.Q = 1.0882)
sanctions $5\%$	c(sanctions.L = 1.2096)	c(sanctions.L = 1.3183)	c(sanctions.L = 1.4369)
sanctions $10\%$	c(sanctions.Q = 1.0996)	c(sanctions.Q = 1.1985)	c(sanctions.Q = 1.3064)
sanctions $15\%$	c(sanctions.C = 0.7894)	c(sanctions.C=0.8605)	c(sanctions.C=0.938)

It took 4 iterations to find the maximum likelihood estimates. the log likelihood is -5,784.130

- 2. If any of the explanatory variables are significant in this model, then:
  - (a) For the policy in which nearly all countries participate [160 of 192], how does increasing sanctions from 5% to 15% change the odds that an individual will support the policy? (Interpretation of a coefficient)
  - (b) What is the estimated probability that an individual will support a policy if there are 80 of 192 countries participating with no sanctions?
  - (c) Would the answers to 2a and 2b potentially change if we included the interaction term in this model? Why?
    - Perform a test to see if including an interaction is appropriate.



Table 4:

	$D\epsilon$	ependent variab	ole:		
	choice				
	(1)	(2)	(3)		
countries.L	-0.458***		$-0.457^{***}$		
	(0.038)		(0.038)		
countries.Q	0.010		0.011		
	(0.038)		(0.038)		
sanctions.L	0.276***		0.274***		
	(0.044)		(0.044)		
sanctions.Q	0.181***		0.182***		
	(0.044)		(0.044)		
sanctions.C	-0.150***		-0.153***		
	(0.044)		(0.044)		
countries.L:sanctions.L			0.002		
			(0.077)		
countries.Q:sanctions.L			$-0.134^{*}$		
			(0.076)		
countries.L:sanctions.Q			0.008		
			(0.076)		
countries.Q:sanctions.Q			-0.093		
			(0.076)		
countries.L:sanctions.C			-0.095		
			(0.076)		
countries.Q:sanctions.C			-0.010		
			(0.077)		
Constant	0.006	0.007	0.004		
	(0.022)	(0.022)	(0.022)		
Observations	8,500	8,500	8,500		
Log Likelihood	-5,784,130	-5,891.705			
Akaike Inf. Crit.	11,580.260	11,785.410	11,585.970		
	JL .	p<0.1; **p<0.0	· *** 0 0 4		

Table 5: ANOVA

Statistic	N	Mean	St. Dev.	Min	Max
Resid. Df	2	8,496.500	3.536	8,494	8,499
Resid. Dev	2	$11,\!675.830$	152.134	$11,\!568.260$	11,783.410
Df	1	5.000		5	5
Deviance	1	215.150		215.150	215.150

Table 6: ANOVA

Statistic	N	Mean	St. Dev.	Min	Max
Resid. Df	2	8,491.000	4.243	8,488	8,494
Resid. Dev	2	$11,\!565.110$	4.450	$11,\!561.970$	11,568.260
Df	1	6.000		6	6
Deviance =	1	6.293		6.293	6.293

# ANOVA