Problem Set 2

Applied Stats II

Due: February 19, 2023

Instructions

• This problem set is due before 23:59 on Sunday February 19, 2023. No late assignments will be accepted.

```
Code in PS2_ImeldaFinn.R
```

We're interested in what types of international environmental agreements or policies people support (Bechtel and Scheve 2013). So, we asked 8,500 individuals whether they support a given policy, and for each participant, we vary the (1) number of countries that participate in the international agreement and (2) sanctions for not following the agreement.

- observational study of 8,500 observations
- Response variable:
 - choice: 1 if the individual agreed with the policy; 0 if the individual did not support the policy
- Explanatory variables:
 - countries: Number of participating countries [20 of 192; 80 of 192; 160 of 192]
 - sanctions: Sanctions for missing emission reduction targets [None, 5%, 15%, and 20% of the monthly household costs given 2% GDP growth]

Read in the data and modified choice variable:

```
load (url("https://github.com/ASDS—TCD/StatsII_Spring2023/blob/main/datasets/climateSupport.RData?raw=true"))

# choice = 1,2
# countries = 1, 2, 3
# sanctions = 1, 2, 3, 4

# get a version of the dataset with the response variable coded as
# True = supported
```

```
# False = not supported
       cs <- climateSupport
       cs $ choice <- as.logical(as.numeric(cs $ choice)-1)
10
       summary (cs)
12
13
       . . .
14
          choice
                                 countries
                                                sanctions
       Mode: logical
                          20 of 192 :2865
                                              None: 2119
16
       FALSE: 4264
                          80 of 192 :2795
                                              5\% : 2133
17
       TRUE : 4236
                          160 of 192:2840
                                              15\% : 2111
1.8
                                              20\% : 2137
19
20
```

1. Remember, we are interested in predicting the likelihood of an individual supporting a policy based on the number of countries participating and the possible sanctions for non-compliance.

Fit an additive model.

1 mod

(a) Summary output,

```
Call:
2
         glm(formula = choice ~ ., family = binomial(link = "logit"),
3
              data = cs
5
         Deviance Residuals:
                                                       Max
             Min
                         1Q
                               Median
                                              3Q
         -1.4259
                              -0.9444
                    -1.1480
                                         1.1505
                                                    1.4298
q
         Coefficients:
10
                        Estimate Std. Error z value Pr(>|z|)
11
         (Intercept)
                       -0.005665
                                     0.021971
                                                -0.258
                                                        0.796517
12
         countries.L 0.458452
                                     0.038101
                                                12.033
                                                         < 2e-16 ***
14
         countries. Q = -0.009950
                                     0.038056
                                                -0.261 \ 0.793741
         sanctions.L -0.276332
                                     0.043925
                                                -6.291 \ 3.15 \,\mathrm{e}{-10} \ ***
         sanctions. Q = -0.181086
                                     0.043963
                                                -4.119 \quad 3.80 \,\mathrm{e}{-05} \quad ***
         sanctions.C
                        0.150207
                                     0.043992
                                                 3.414 0.000639 ***
17
18
                           0 '*** ' 0.001 '** ' 0.01 '* ' 0.05 '. ' 0.1
         Signif. codes:
19
20
         (Dispersion parameter for binomial family taken to be 1)
21
              Null deviance: 11783
                                                  degrees of freedom
                                       on 8499
         Residual deviance: 11568
                                       on 8494
                                                 degrees of freedom
24
         AIC: 11580
25
26
         Number of Fisher Scoring iterations: 4
27
28
```

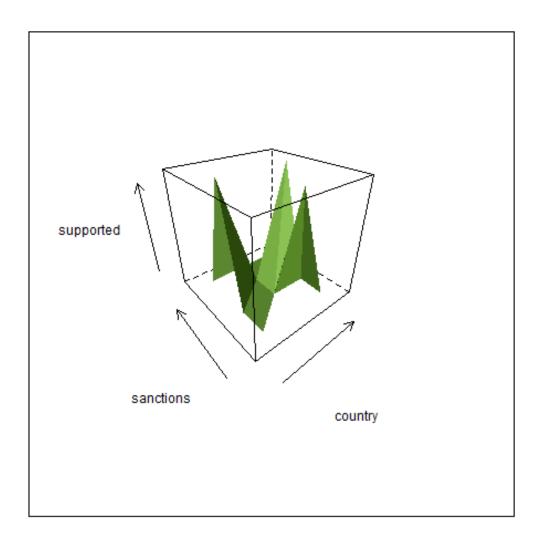


Figure 1: plot of additive (glm) model

(b) The global null hypothesis and p-value.

 H_0 : the explanatory variables have no effect on the likelihood of an individual supporting a policy

 H_a : one or more of the explanatory variables have some effect on the likelihood of an individual supporting a policy

```
\alpha = 0.05
```

The data was modelled with no explanatory variables (choice 1). The comparison of the two models is shown in 1

A test was run to compare the deviances of the two models.

```
anova_null <- anova(null_mod, mod, test = "LRT")
```

The results are shown in 2. The χ^2 statistic = 11783 - 11568 = 215.15. The assocated p-value with 5 degrees of freedom is 2.2×10^{-16} .

As the p-value is below α we reject the null hypothesis. The evidence does not support the assumption that none of the explanatory variables have any effect on our response variable choice. We expect that one or more of our explanatory variables will have a statistically significant effect on the probability of a policy being supported.

Table 1:

	Depender	nt variable:	
	ch	oice	
	logistic		
	(1)	(2)	
countries: 80 of 192	0.458***		
	(0.038)		
countries: 160 of 192	-0.010		
	(0.038)		
sanctions: 5%	-0.276***		
	(0.044)		
sanctions: 5%	-0.181***		
	(0.044)		
sanctions: 5%	0.150***		
	(0.044)		
Constant	-0.006	-0.007	
	(0.022)	(0.022)	
Observations	8,500	8,500	
Log Likelihood	-5,784.130	-5,891.705	
Akaike Inf. Crit.	11,580.260	11,785.410	
\overline{Note} :	*p<0.1; **p<	0.05; ***p<0.01	

Table 2:

Statistic	N	Mean	St. Dev.	Min	Max
Resid. Df	2	8,496.500	3.536	8,494	8,499
Resid. Dev	2	$11,\!675.830$	152.134	$11,\!568.260$	11,783.410
Df	1	5.000		5	5
Deviance	1	215.150		215.150	215.150
$\frac{\Pr(>\text{Chi})}{}$	1	0.000		0	0

(c) Please describe the results and provide a conclusion.

When 20 out of 192 countries are included and there are no sanctions (base case), then the expected odds of a participant agreeing with a policy are $e^{-0.005665} = 0.994351$

A one unit increase in X_k increases the odds of supporting a policy by a multiplicative factor of e^{β_k}

When 20 out of 192 countries are included and there are sanctions of 5%, the logodds change by $e^{-0.276332} = 0.758561$ compared to the base

$$logit(p) = -0.005665 + -0.276332$$

When 80 out of 192 countries are included and there are no sanctions, the logodds change by $e^{-0.458453} = 0.632261$ compared to the base

$$logit(p) = -0.005665 - 0.458453$$

When 80 out of 192 countries are included and there are sanctions of 5%, then:

$$logit(p) = -0.005665 + -0.276332 - 0.458453 = e^{logit(p)} = 0.4768993$$

ie the odds reduce by 48.0%.

The predicted probabilities, and confidence intervals, are in Table 3

The estimates for β_k are all significant at p = 0.01 except for 'countries: 160 of 192' (countries.Q), ie there is a predicted -0.1 change in *logit* going from 80 to 160 countries, but it is not statistically significant.

Table 3:

	countries	sanctions	fit	se.fit	residual.scale	UL	LL	PredictedProb
1	80 of 192	15%	0.483	0.013	1	0.625	0.612	0.618
2	160 of 192	15%	0.560	0.013	1	0.642	0.631	0.637
3	20 of 192	15%	0.400	0.013	1	0.605	0.593	0.599
4	80 of 192	None	0.516	0.013	1	0.632	0.620	0.626
5	160 of 192	None	0.593	0.013	1	0.650	0.638	0.644
6	20 of 192	None	0.432	0.013	1	0.613	0.600	0.606
7	80 of 192	5%	0.564	0.013	1	0.643	0.631	0.637
8	160 of 192	5%	0.638	0.012	1	0.660	0.649	0.654
9	20 of 192	5%	0.480	0.013	1	0.624	0.612	0.618
10	80 of 192	20%	0.440	0.013	1	0.614	0.602	0.608
11	160 of 192	20%	0.518	0.013	1	0.633	0.620	0.627
12	20 of 192	20%	0.360	0.012	1	0.595	0.583	0.589

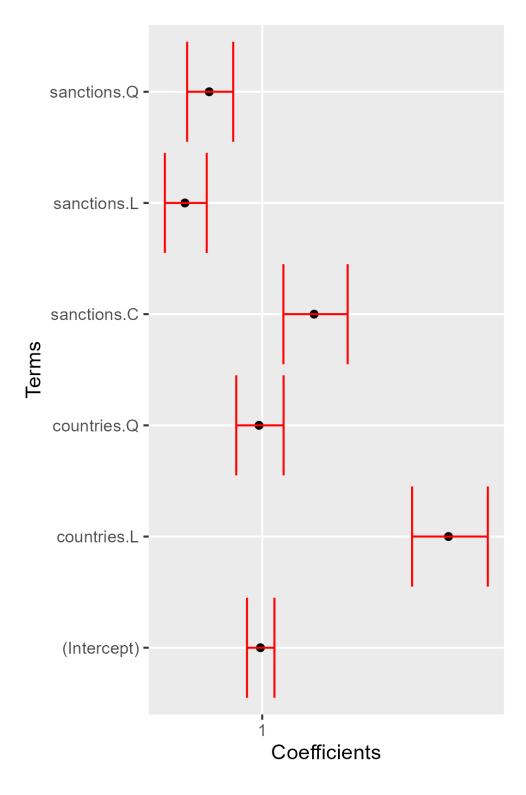


Figure 2: coefficients of additive model

It took 4 iterations to find the maximum likelihood estimates. The log likelihood is -5,784.130

- 2. If any of the explanatory variables are significant in this model, then:
 - (a) For the policy in which nearly all countries participate [160 of 192], how does increasing sanctions from 5% to 15% change the odds that an individual will support the policy? (Interpretation of a coefficient)
 - (b) What is the estimated probability that an individual will support a policy if there are 80 of 192 countries participating with no sanctions?
 - (c) Including an interaction term would potentially change the results in 2a and 2b. The values for the coefficients would potentially be different (eg $beta_k$) and we would have to include the constituent coefficient values in calculating the value of the logit.
 - A model was run on the data, with an interaction between countries and sanctions, and an ANOVA/ χ_2 test was run. The results are shown in Tables 4 and 5.

The test statistic of 6.2928, with 6 degrees of freedom, lead to a p-value of 0.3912. Therefore we cannot reject the null hypothesis that the two models are the same, ie we do not conclude that an interaction term is appropriate.

Table 4:

	Depender	nt variable:		
	ch	oice		
	logistic			
	(1)	(2)		
countries: 80 of 192	0.458***	0.457***		
	(0.038)	(0.038)		
countries: 160 of 192	-0.010	-0.011		
	(0.038)	(0.038)		
sanctions: 5%	-0.276^{***}	-0.274***		
	(0.044)	(0.044)		
sanctions: 5%	-0.181^{***}	-0.182***		
	(0.044)	(0.044)		
sanctions: 5%	0.150***	0.153***		
	(0.044)	(0.044)		
countries.L:sanctions.L		-0.002		
		(0.077)		
${ m countries. Q:} { m sanctions. L}$		0.134^{*}		
		(0.076)		
countries.L:sanctions.Q		-0.008		
		(0.076)		
countries.Q:sanctions.Q		0.093		
		(0.076)		
countries.L:sanctions.C		0.095		
		(0.076)		
countries.Q:sanctions.C		0.010		
		(0.077)		
Constant	-0.006	-0.004		
	(0.022)	(0.022)		
Observations	10 8,500	8,500		
Log Likelihood	-5,784.130	-5,780.983		
Akaike Inf. Crit.	$11,\!580.260$	11,585.970		
Note:	*p<0.1; **p<0.05; ***p<0.01			

Table 5: ANOVA additive vs Interactive

Statistic	N	Mean	St. Dev.	Min	Max
Resid. Df	2	8,491.000	4.243	8,488	8,494
Resid. Dev	2	$11,\!565.110$	4.450	$11,\!561.970$	11,568.260
Df	1	6.000		6	6
Deviance	1	6.293		6.293	6.293
$\Pr(> \mathrm{Chi})$	1	0.391		0.391	0.391