

# Problem Set 3

Applied Stats/Quant Methods 1

Due: November 20, 2021

## Data

```
1 dat = read_csv("../..../datasets/incumbents_subset.csv")
```

## Question 1

We are interested in knowing how the difference in campaign spending between incumbent and challenger affects the incumbent's vote share.

1. Run a regression where the outcome variable is **voteshare** and the explanatory variable is **difflog**. The function call to generate the model is:

```
1 mod_vote_spend <- lm(voteshare ~ difflog, data = dat)
```

The results are:

Table 1: Vote share as a function of Differential Spending

	<i>Dependent variable:</i>
	voteshare
difflog	0.041666*** (0.000968)
Constant	0.579031*** (0.002251)
Observations	3,193
R <sup>2</sup>	0.367341
Adjusted R <sup>2</sup>	0.367143
Residual Std. Error	0.078673 (df = 3191)
F Statistic	1,852.791000*** (df = 1; 3191)
<i>Note:</i>	*p<0.1; **p<0.05; ***p<0.01

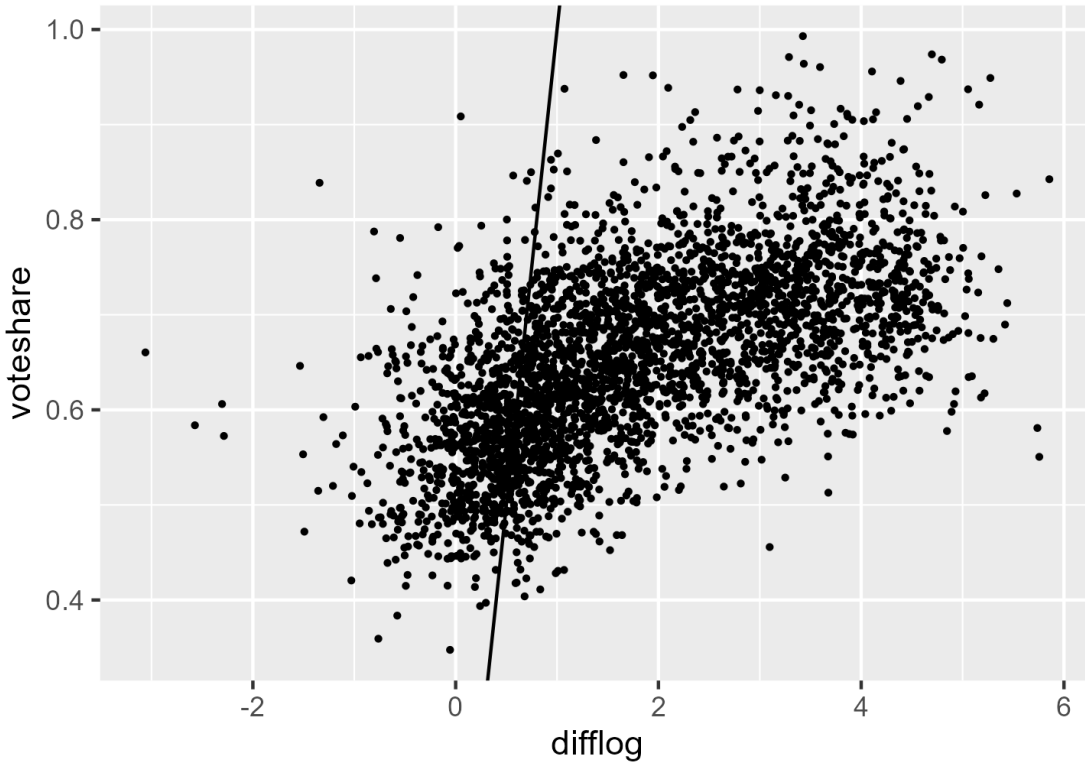


Figure 1: Vote share as a function of Differential Spending

2. Make a scatterplot of the two variables and add the regression line.
3. Save the residuals of the model in a separate object.

```
1 resid_vote_spend <- mod_vote_spend$residuals
```

4. Write the prediction equation.

**Prediction Equation**  $voteshare = 0.579031 + (0.041666) * difflog$  ie the voteshare is 0.579031 when difflog is 0 it increases by 0.041666 for each unit increase in difflog

## Question 2

We are interested in knowing how the difference between incumbent and challenger's spending and the vote share of the presidential candidate of the incumbent's party are related.

1. Run a regression where the outcome variable is **presvote** and the explanatory variable is **difflog**.

The function call to generate the model is:

```
1 mod_pres_spend <- lm(presvote ~ difflog, data = dat)
```

The results are in table 2

Table 2: Presidential vote share as a function of Differential Spending

	<i>Dependent variable:</i>
	presvote
difflog	0.023837*** (0.001359)
Constant	0.507583*** (0.003161)
Observations	3,193
R <sup>2</sup>	0.087951
Adjusted R <sup>2</sup>	0.087665
Residual Std. Error	0.110442 (df = 3191)
F Statistic	307.715400*** (df = 1; 3191)
<i>Note:</i>	*p<0.1; **p<0.05; ***p<0.01

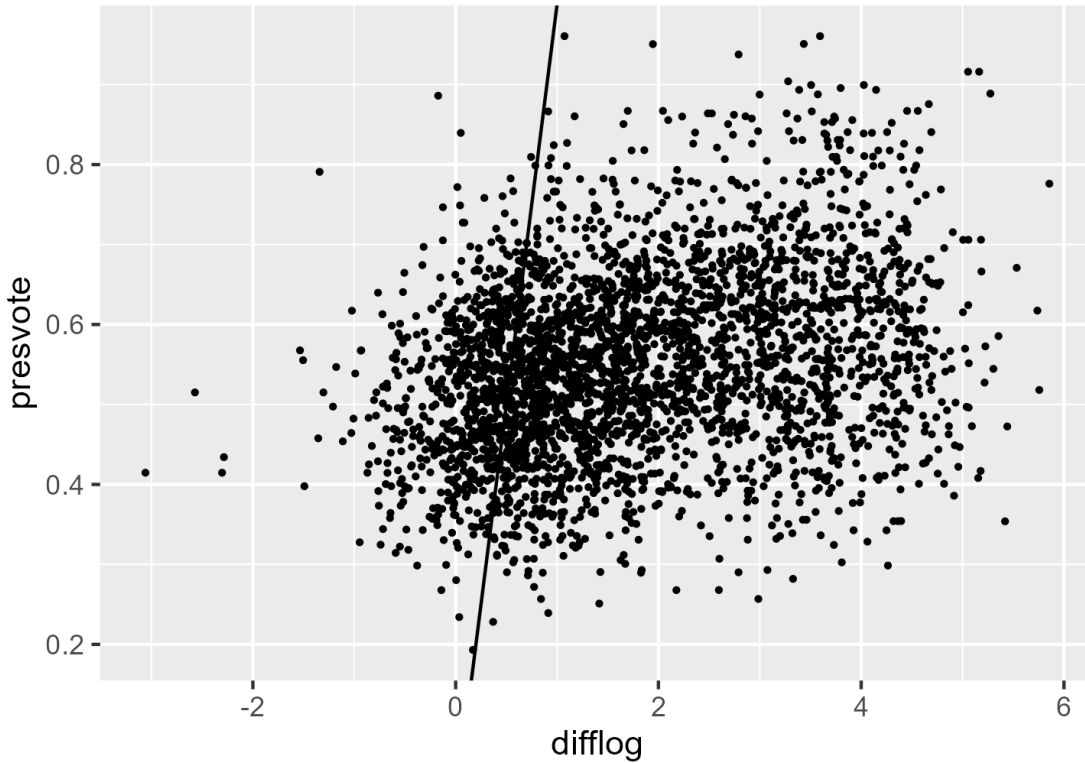


Figure 2: Presidential vote share as a function of Differential Spending

2. Make a scatterplot of the two variables and add the regression line.

3. Save the residuals of the model in a separate object.

```
1 resid_pres_spend <- mod_pres_spend$residuals
```

4. Write the prediction equation. **Prediction Equation**  $presvote = 0.507583 + (0.023837) * difflog$  ie the presvote is 0.507583 when difflog is 0 it increases by 0.023837 for each unit increase in difflog

## Question 3

We are interested in knowing how the vote share of the presidential candidate of the incumbent's party is associated with the incumbent's electoral success.

1. Run a regression where the outcome variable is **voteshare** and the explanatory variable is **presvote**. The function call to generate the model is:

```
1 mod_pres_spend <- lm(presvote ~ difflog , data = dat)
```

and the results are in 3

Table 3: Vote share as a function of Presidential vote share

	<i>Dependent variable:</i>
	voteshare
presvote	0.388018*** (0.013493)
Constant	0.441330*** (0.007599)
Observations	3,193
R <sup>2</sup>	0.205814
Adjusted R <sup>2</sup>	0.205565
Residual Std. Error	0.088146 (df = 3191)
F Statistic	826.950200*** (df = 1; 3191)
<i>Note:</i>	*p<0.1; **p<0.05; ***p<0.01



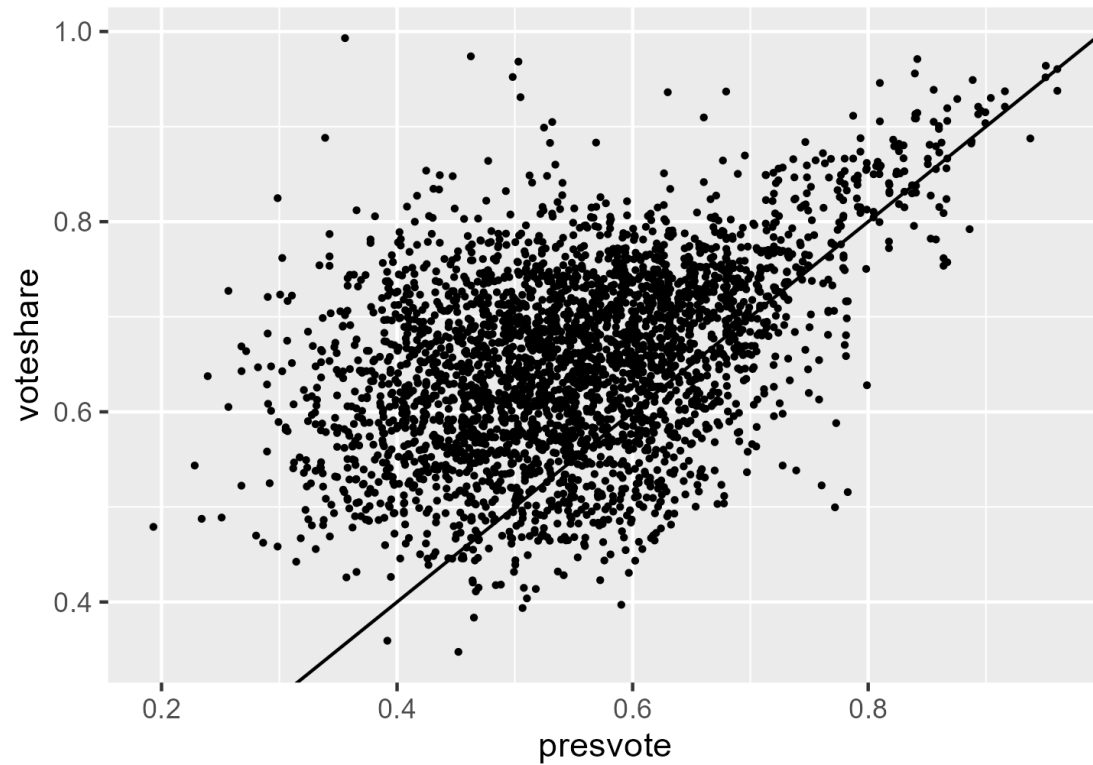


Figure 3: Vote share as a function of Presidential vote share

2. Make a scatterplot of the two variables and add the regression line.
3. Write the prediction equation.

**Prediction Equation**

$voteshare = 0.441330 + (0.388018) * presvote$  ie the voteshare is 0.441330 when presvote is 0 it increases by 0.388018 for each unit increase in presvote

## Question 4

The residuals from part (a) tell us how much of the variation in **voteshare** is *not* explained by the difference in spending between incumbent and challenger. The residuals in part (b) tell us how much of the variation in **presvote** is *not* explained by the difference in spending between incumbent and challenger in the district.

1. Run a regression where the outcome variable is the residuals from Question 1 and the explanatory variable is the residuals from Question 2.

The function call to generate the model is:

```
1 mod_vote_pres <- lm(voteshare ~ presvote, data = dat)
```

The results of the linear model are:

Table 4: Vote share residuals as a function of Presidential vote share residuals

	<i>Dependent variable:</i>
	resid_vote_spend
resid_pres_spend	0.256877*** (0.011762)
Constant	−0.000000 (0.001299)
Observations	3,193
R <sup>2</sup>	0.130038
Adjusted R <sup>2</sup>	0.129765
Residual Std. Error	0.073380 (df = 3191)
F Statistic	476.974700*** (df = 1; 3191)
<i>Note:</i>	*p<0.1; **p<0.05; ***p<0.01

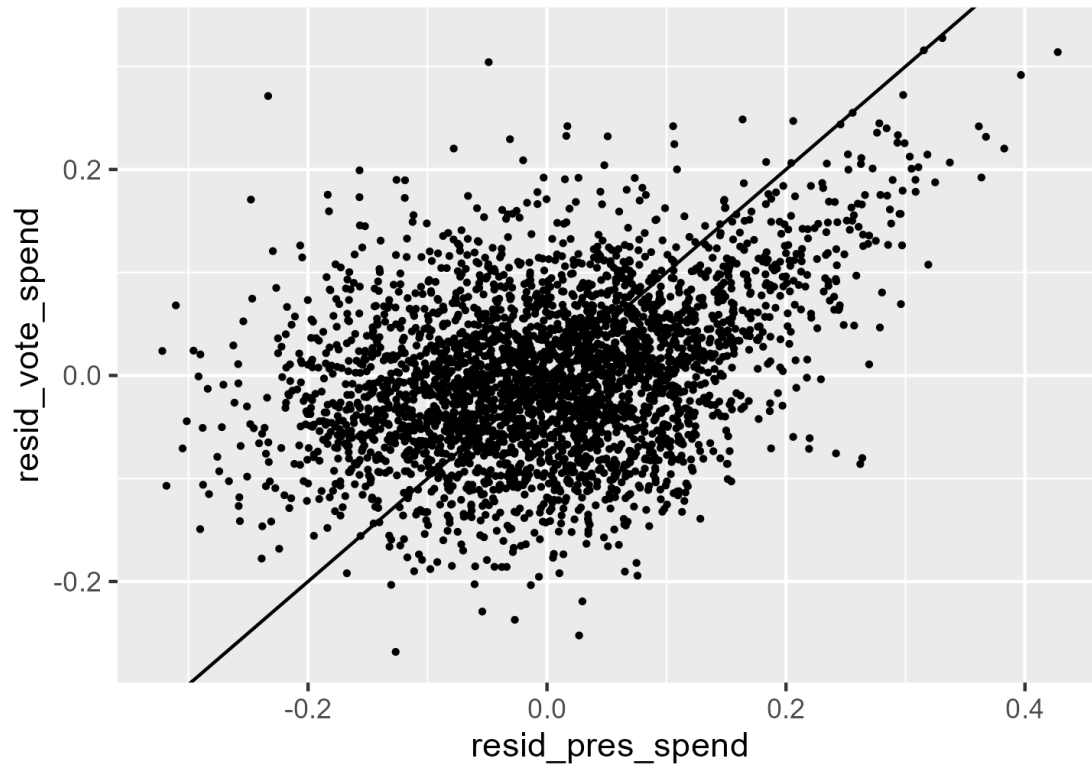


Figure 4: Vote share residuals as a function of Presidential vote share residuals

2. Make a scatterplot of the two residuals and add the regression line.
3. Write the prediction equation.

**Prediction Equation**  $\text{voteshare residuals} = -5.207\text{e-}18 + (0.2569) * \text{presvote residuals}$   
 ie the voteshare residual value is  $-5.207\text{e-}18$  when presvote residual value is 0 it increases by 0.2569 for each unit increase in presvote residuals

ie the value of the incumbent vote share not accounted for by the difference in incumbent spending increases by 0.2569 for each unit increase in the value of the unidentified factors which cause an increase in presidential vote share.

## Question 5

What if the incumbent's vote share is affected by both the president's popularity and the difference in spending between incumbent and challenger?

1. Run a regression where the outcome variable is the incumbent's `voteshare` and the explanatory variables are `difflog` and `presvote`.

The function call to generate the model is:

```
1 mod_vote_spend_pres <- lm(voteshare ~ difflog + presvote, data = dat)
```

The results of the linear model are:

Table 5: Vote share as a function of Presidential vote share and differential spending

	<i>Dependent variable:</i>
	voteshare
difflog	0.035543*** (0.000946)
presvote	0.256877*** (0.011764)
Constant	0.448644*** (0.006330)
Observations	3,193
R <sup>2</sup>	0.449610
Adjusted R <sup>2</sup>	0.449265
Residual Std. Error	0.073391 (df = 3190)
F Statistic	1,302.947000*** (df = 2; 3190)
<i>Note:</i>	*p<0.1; **p<0.05; ***p<0.01

The additional variables are plotted in 5.

2. Write the prediction equation.

**Prediction Equation**  $voteshare = 0.4486442 + (0.0355431) * difflog + (0.2568770) * presvote$

ie the voteshare is 0.4486442 when difflog and presvote are 0 it increases by 0.0355431 for each unit increase in difflog (holding presvote constant) it increases by 0.2568770 for each unit increase in presvote (holding difflog constant)

3. What is it in this output that is identical to the output in Question 4? Why do you think this is the case?

The coefficient for residual president share as a function of incumbent spending (Q4) is the same as the coefficient for presidential vote share.(0.256877)

In model 5, the coefficient for presvote is a partial predictor, with difflog held constant. In model 2, the residuals represent the variation in the value of the presidential vote, excluding difflog (which was specifically included as a predictor). In both models, we are getting a predictive value for presvote on voteshare, with difflog excluded/controlled.

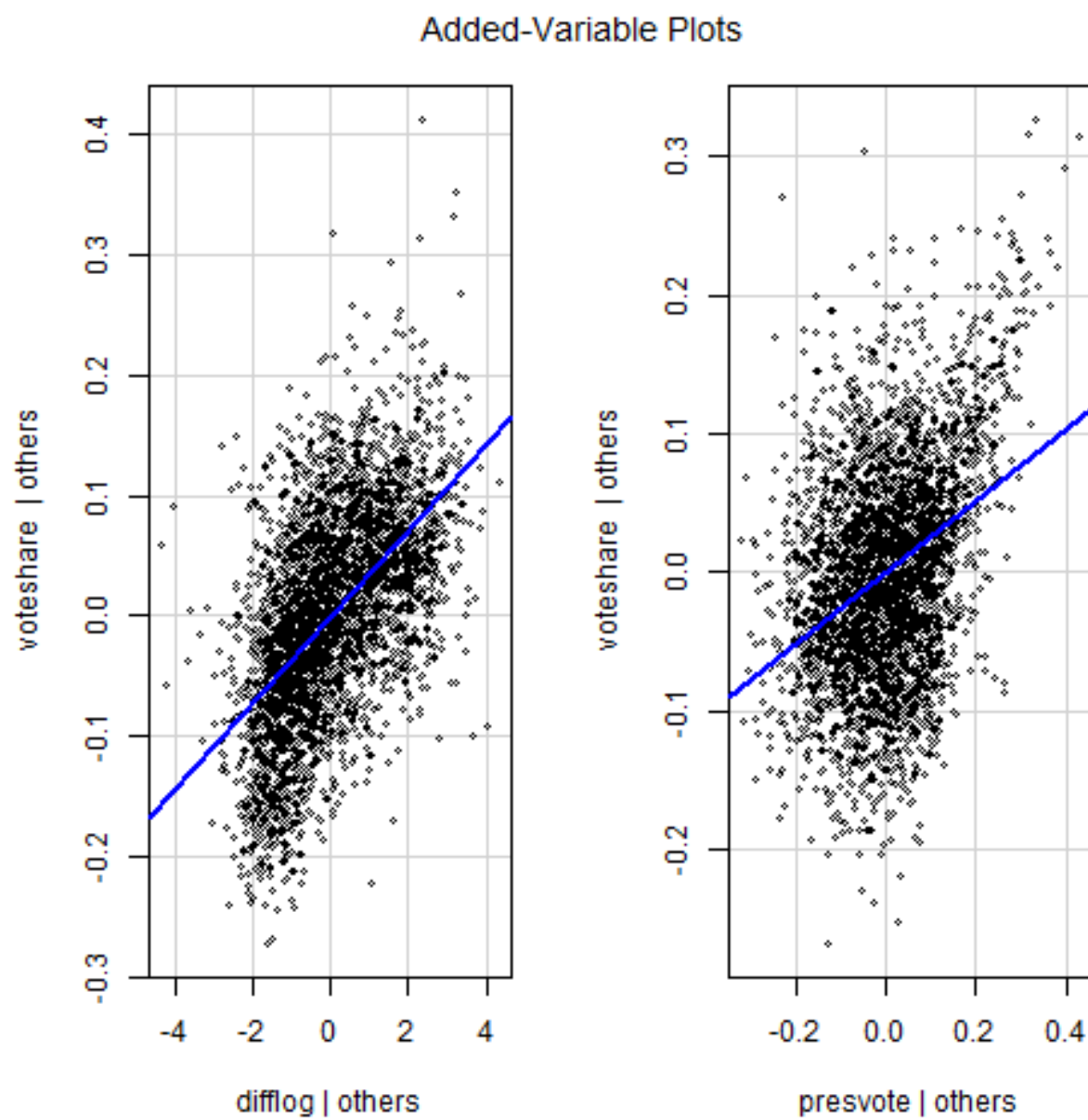


Figure 5: Vote share as a function of differential spending and presidential vote share



## Appendix - Code

```
1 #####
2 # Imelda Finn, 22334657
3 # POP77003 – Stats I
4 # clear global .envir, load libraries, set wd
5 #####
6
7 # remove objects
8 rm(list=ls())
9
10 # detach all libraries
11 detachAllPackages <- function() {
12   basic.packages <- c("package:stats", "package:graphics", "package:grDevices"
13     , "package:utils", "package:datasets", "package:methods", "package:base")
14   package.list <- search()[ifelse(unlist(gregexpr("package:", search()))==1,
15     TRUE, FALSE)]
16   package.list <- setdiff(package.list, basic.packages)
17   if (length(package.list)>0) for (package in package.list) detach(package,
18     character.only=TRUE)
19 }
20 detachAllPackages()
21
22 # load libraries
23 pkgTest <- function(pkg){
24   new.pkg <- pkg[!(pkg %in% installed.packages()[, "Package"])]
25   if (length(new.pkg))
26     install.packages(new.pkg, dependencies = TRUE)
27   supply(pkg, require, character.only = TRUE)
28 }
29
30 # load necessary packages
31 lapply(c("ggplot2", "stargazer", "tidyverse", "stringr", "car"), pkgTest)
32
33 # function to save output to a file that you can read in later to your docs
34 output_stargazer <- function(outputFile, appendVal=TRUE, ...) {
35   output <- capture.output(stargazer(...))
36   cat(paste(output, collapse = "\n"), "\n", file=outputFile, append=appendVal)
37 }
38
39
40 # set working directory to current parent folder
41 setwd(dirname(rstudioapi::getActiveDocumentContext()$path))
42 #####
43
44 #Problem Set 3
45 #Applied Stats/Quant Methods 1
46 #Due: November 20, 2021
47 #Instructions
48 # Please show your work! You may lose points by simply writing in the answer.
49 # If the
```

```

47 #problem requires you to execute commands in R, please include the code you
    used to
48 #get your answers. Please also include the .R file that contains your code. If
    you are
49 #not sure if work needs to be shown for a particular problem, please ask.
50 # Your homework should be submitted electronically on GitHub.
51 # This problem set is due before 23:59 on Sunday November 20, 2022. No late
    assign-
52 # ments will be accepted.
53 # Total available points for this homework is 80.
54 #In this problem set, you will run several regressions and create an add
    variable plot (see the
55 #lecture slides) in R using the incumbents subset.csv dataset. Include all of
    your code.

56
57 #####
58 # get data
59 #####
60 # line in tex = 61
61 dat = read_csv("../..../datasets/incumbents_subset.csv")
62 saveRDS(dat, "Data/incumbents_subset.csv")
63 dat <- readRDS("Data/incumbents_subset.csv")
64
65
66 #####
67 #Question 1
68 #####
69
70 # difflog is the difference between the incumbents' spending
71 # and the challengers' spending
72 dl = sum(dat$difflog - (dat$incspend - dat$chalspend))
73
74 png("Graphics/incumbent_subset.png" )
75 pairs(~voteshare + presvote + difflog, dat)
76 dev.off() # close output
77
78
79
80 mean(dat$difflog)
81 fivenum(dat$difflog)
82 #-3.0600882  0.6733625  1.6105532  2.9856564  5.8558103'
83 fivenum(dat$presvote)
84 #0.1931263  0.4695266  0.5478388  0.6239612  0.9606069
85 fivenum(dat$voteshare)
86 #0.3475569  0.5845994  0.6568562  0.7232970  0.9930361
87
88
89 #We are interested in knowing how the difference in campaign spending between
    incumbent
90 #and challenger affects the incumbent's vote share.
91 #1. Run a regression where the outcome variable is voteshare and the

```

```

    explanatory variable
92 #is difflog.
93 #1
94 #2. Make a scatterplot of the two variables and add the regression line.
95 #3. Save the residuals of the model in a separate object.
96 #4. Write the prediction equation.
97 #2
98
99 #1. # line in tex 100
100 mod_vote_spend <- lm(voteshare ~ difflog, data = dat)
101
102 #2.
103 dat %>% ggplot(aes( x= difflog, y = voteshare)) +
104   geom_point(size=0.5) +
105   geom_abline()
106 ggsave("Graphics/vote_spend.png")
107
108 #3. line in tex 109
109 resid_vote_spend <- mod_vote_spend$residuals
110
111 #4.
112 summary(mod_vote_spend)
113
114 output_stargazer("Tables/mod_vote_spend.tex", appendVal = FALSE, mod_vote_
    spend,
115               title="Vote share as a function of Differential Spending",
116               label="tab:vote_spend", digits = 6 #, summary=FALSE
117 )
118
119 #Prediction Equation
120 # voteshare = 0.579031 + (0.041666) * difflog
121 # ie the voteshare is 0.579031 when difflog is 0
122 # it increases by 0.041666 for each unit increase in difflog
123
124 #Call:
125 # lm(formula = voteshare ~ difflog, data = dat)
126
127 #Residuals:
128 #   Min       1Q   Median       3Q      Max
129 #-0.26832 -0.05345 -0.00377  0.04780  0.32749
130
131 #Coefficients:
132 #   Estimate Std. Error t value Pr(>|t|)
133 # (Intercept)  0.579031   0.002251  257.19  <2e-16 ***
134 #   difflog     0.041666   0.000968   43.04  <2e-16 ***
135 #   ---
136 #   Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
137
138 #Residual standard error: 0.07867 on 3191 degrees of freedom
139 #Multiple R-squared:  0.3673, Adjusted R-squared:  0.3671
140 #F-statistic: 1853 on 1 and 3191 DF, p-value: < 2.2e-16

```

```

141
142
143 #Question 2
144 #We are interested in knowing how the difference between incumbent and
    challenger's
145 # spending and the vote share of the presidential candidate of
146 # the incumbent's party are related.
147 #1. Run a regression where the outcome variable is presvote and the
    explanatory variable
148 #is difflog.
149 #2. Make a scatterplot of the two variables and add the regression line.
150 #3. Save the residuals of the model in a separate object.
151 #4. Write the prediction equation.
152 #3
153
154 #1. # line in tex 155
155 mod_pres_spend <- lm(presvote ~ difflog, data = dat)
156
157 #2.
158 dat %>% ggplot(aes( x= difflog, y = presvote)) +
159   geom_point(size=0.5) +
160   geom_abline()
161 ggsave("Graphics/pres_spend.png")
162
163 #3. line in tex 164
164 resid_pres_spend <- mod_pres_spend$residuals
165
166 #4.
167 summary(mod_pres_spend)
168
169 output_stargazer("Tables/mod_pres_spend.tex", appendVal = FALSE,
170                 mod_pres_spend,
171                 title="Presidential vote share as a function of Differential
    Spending",
172                 label="tab:pres_spend", digits = 6 #, summary=FALSE
173 )
174
175 #Prediction Equation
176 # presvote = 0.507583 + (0.023837) * difflog
177 # ie the presvote is 0.507583 when difflog is 0
178 # it increases by 0.023837 for each unit increase in difflog
179
180 #Call:
181 #lm(formula = presvote ~ difflog, data = dat)
182
183 #Residuals:
184 #   Min       1Q   Median       3Q      Max
185 #-0.32196 -0.07407 -0.00102  0.07151  0.42743
186
187 #Coefficients:
188 #   Estimate Std. Error t value Pr(>|t|)

```

```

189 #(Intercept) 0.507583    0.003161   160.60    <2e-16 ***
190 #   difflog      0.023837    0.001359    17.54    <2e-16 ***
191 #   —————
192 #   Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
193
194 #Residual standard error: 0.1104 on 3191 degrees of freedom
195 #Multiple R-squared:  0.08795,   Adjusted R-squared:  0.08767
196 #F-statistic: 307.7 on 1 and 3191 DF,  p-value: < 2.2e-16
197
198 #Question 3
199 #We are interested in knowing how the vote share of the presidential
200 # candidate of the incumbent's party is associated with the
201 #incumbent's electoral success.
202 #1. Run a regression where the outcome variable is voteshare and the
    explanatory variable
203 #is presvote.
204 #2. Make a scatterplot of the two variables and add the regression line.
205 #3. Write the prediction equation.
206 #4
207
208 #1)    # line in tex 209
209 mod_vote_pres <- lm(voteshare ~ presvote, data = dat)
210
211 #2)
212 dat %>% ggplot(aes( x= presvote, y = voteshare)) +
213   geom_point(size=0.5) +
214   geom_abline()
215 ggsave("Graphics/vote_pres.png")
216
217 #3)
218 summary(mod_vote_pres)
219
220 output_stargazer("Tables/mod_vote_pres.tex", appendVal = FALSE,
221                 mod_vote_pres,
222                 title="Vote share as a function of Presidential vote share",
223                 label="tab:vote_pres", digits = 6 #, summary=FALSE
224 )
225
226 #Prediction Equation
227 # voteshare = 0.441330 + (0.388018) * presvote
228 # ie the voteshare is 0.441330 when presvote is 0
229 #   it increases by 0.388018 for each unit increase in presvote
230
231
232 #Call:
233 # lm(formula = voteshare ~ presvote, data = dat)
234
235 #Residuals:
236 #   Min       1Q   Median       3Q      Max
237 #-0.27330 -0.05888  0.00394  0.06148  0.41365
238

```

```

239 #Coefficients:
240 #   Estimate Std. Error t value Pr(>|t|)
241 #(Intercept) 0.441330    0.007599   58.08   <2e-16 ***
242 #   presvote    0.388018    0.013493   28.76   <2e-16 ***
243 #   -----
244 #   Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
245
246 #Residual standard error: 0.08815 on 3191 degrees of freedom
247 #Multiple R-squared:  0.2058, Adjusted R-squared:  0.2056
248 #F-statistic: 827 on 1 and 3191 DF,  p-value: < 2.2e-16
249
250
251 #Question 4
252 #The residuals from part (a) tell us how much of the variation in voteshare is
    not explained
253 #by the difference in spending between incumbent and challenger. The residuals
    in part (b)
254 #tell us how much of the variation in presvote is not explained by the
    difference in spending
255 #between incumbent and challenger in the district.
256 #1. Run a regression where the outcome variable is the residuals from Question
    1 and the
257 #explanatory variable is the residuals from Question 2.
258 #2. Make a scatterplot of the two residuals and add the regression line.
259 #3. Write the prediction equation.
260
261 #1.    # line in tex 262
262 mod_resid_vote_pres <- lm(resid_vote_spend ~ resid_pres_spend)
263
264 #2.
265
266 ggplot() +
267   geom_point(aes(resid_pres_spend, resid_vote_spend), size=0.5) +
268   geom_abline()
269 ggsave("Graphics/residuals.png")
270
271 #3.
272 summary(mod_resid_vote_pres)
273 output_stargazer("Tables/mod_resid_vote_pres.tex", appendVal = FALSE,
274                 mod_resid_vote_pres,
275                 title="Vote share residuals as a function of Presidential
    vote share residuals",
276                 label="tab:residuals", digits = 6 #, summary=FALSE
277 )
278
279 # residuals for both are clustered around 0
280 #Prediction Equation
281 # voteshare residuals = -5.207e-18 + (0.2569) * presvote residuals
282 # ie the voteshare residual value is -5.207e-18 when presvote residual value
    is 0
283 #   it increases by 0.2569 for each unit increase in presvote residuals

```

```

284
285 fivenum(resid_pres_spend)
286 fivenum(resid_vote_spend)
287 mean(resid_pres_spend)      # ie 0
288 mean(resid_vote_spend)      # ie 0, as expected
289
290
291 #Call:
292 # lm(formula = resid_vote_spend ~ resid_pres_spend)
293
294 #Residuals:
295 #   Min       1Q   Median       3Q      Max
296 #-0.25928 -0.04737 -0.00121  0.04618  0.33126
297
298 #Coefficients:
299 #   Estimate Std. Error t value Pr(>|t|)
300 #(Intercept)    -5.207e-18  1.299e-03     0.00      1
301 #resid_pres_spend  2.569e-01  1.176e-02   21.84 <2e-16 ***
302 #   ---
303 #   Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
304
305 #Residual standard error: 0.07338 on 3191 degrees of freedom
306 #Multiple R-squared:  0.13, Adjusted R-squared:  0.1298
307 #F-statistic:  477 on 1 and 3191 DF, p-value: < 2.2e-16
308
309 #Question 5
310 #What if the incumbent's vote share is affected by both the president's
311 #popularity and the
312 #difference in spending between incumbent and challenger?
313 #1. Run a regression where the outcome variable is the incumbent's voteshare
314 #and the
315 #explanatory variables are difflog and presvote.
316 #2. Write the prediction equation.
317 #3. What is it in this output that is identical to the output in Question 4?
318 #Why do you
319 #think this is the case?
320 # 6
321
322 #1. # line in tex 320
323 mod_vote_spend_pres <- lm(voteshare ~ difflog + presvote, data = dat)
324
325 #2)
326 #install.packages("car")
327 #library(car)
328 png("Graphics/add_variable.png")
329 avPlots(mod_vote_spend_pres, col = carPalette()[1], pch = 1, cex=0.5, id=FALSE)
330 dev.off() # close output
331
332
333 #dat %>% ggplot(aes( ~voteshare + difflog + presvote)) +

```

```

331 # geom_
332 # geom_point() +
333 # geom_abline()
334 #ggsave("Graphics/vote_pres.png")
335
336 #3)
337 summary(mod_vote_spend_pres)
338
339 output_stargazer("Tables/mod_vote_spend_pres.tex", appendVal = FALSE,
340                 mod_vote_spend_pres,
341                 title="Vote share as a function of Presidential vote share
and differential spending",
342                 label="tab:vote_spend_pres", digits = 6 #, summary=FALSE
343 )
344
345 #Prediction Equation
346 # voteshare = 0.4486442 + (0.0355431) * difflog + (0.2568770) * presvote
347 # ie the voteshare is 0.4486442 when difflog and presvote are 0
348 #   it increases by 0.0355431 for each unit increase in difflog
349 #       (holding presvote constant)
350 #   it increases by 0.2568770 for each unit increase in presvote
351 #       (holding difflog constant)
352
353 #Call:
354 # lm(formula = voteshare ~ difflog + presvote, data = dat)
355
356 #Residuals:
357 #   Min       1Q   Median       3Q      Max
358 #-0.25928 -0.04737 -0.00121  0.04618  0.33126
359
360 #Coefficients:
361 #   Estimate Std. Error t value Pr(>|t|)
362 #(Intercept)  0.4486442   0.0063297   70.88  <2e-16 ***
363 #   difflog      0.0355431   0.0009455   37.59  <2e-16 ***
364 #   presvote     0.2568770   0.0117637   21.84  <2e-16 ***
365 #   ---
366 #   Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
367
368 #Residual standard error: 0.07339 on 3190 degrees of freedom
369 #Multiple R-squared:  0.4496, Adjusted R-squared:  0.4493
370 #F-statistic: 1303 on 2 and 3190 DF, p-value: < 2.2e-16

```