Machine Learning Assignment Number 3

Assignments on Artificial Dataset and Real life datasets. Real life dataset availability: UCI machine learning repository; Datasets: Labelled and unlabelled dataset

Artificial Datasets:

$$\begin{split} &\mu_1{}' = (0,0) \; ; \, \mu_2{}' = (0,1); \, \mu_3{}' = (1,0) \\ &\Sigma_1 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}; \, \Sigma_2 = \begin{pmatrix} 2 & -1 \\ -1 & 1.5 \end{pmatrix}; \, \Sigma_3 = \begin{pmatrix} 2 & 1 \\ 1 & 1.5 \end{pmatrix}; \end{split}$$

Case 1:
$$P_1 = 0.5 = P_2$$

Case 2:
$$P_1 = 0.4$$
; $P_2 = 0.6$

- A) Consider $N(\mu_1, \Sigma_1)$ and $N(\mu_2, \Sigma_1)$ under case (i) Generate n points from mixture density functions. The value of n=100,500,1000,2000,5000
- B) Consider $N(\mu_1, \Sigma_1)$ and $N(\mu_2, \Sigma_1)$ under case (ii) Generate n points from mixture density functions randomly.
- C) Consider $N(\mu_1, \Sigma_1)$ and $N(\mu_2, \Sigma_2)$ under case (ii) Generate n points from mixture density functions randomly.
- **D)** Consider $N(\mu_1, \Sigma_1)$, $N(\mu_2, \Sigma_2)$, and $N(\mu_3, \Sigma_3)$ $P_1 = 0.3, \ P_2 = 0.4, P_3 = 0.3$ Generate n points from mixture density functions randomly.
- 1) Take first $\frac{n}{2}$ points as training set and the rest as test set.
- For each training set and for each class estimate mean, covariance matrix and prior probability.
- 3) After estimating three, apply Bayes' decision rule on each point in the test set by using he estimated values under the assumption of normality, and find the misclassification rate.
- 4) Apply Bayes' decision rule on each point of test by using the actual parameter values under the assumption of normality and find the misclassification rate.