

Classification of Melanoma Lesions Using Sparse Coded Features and Random Forests

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ABSTRACT

Malignant melanoma is the most dangerous type of skin cancer, yet it is the most treatable kind of cancer, conditioned by its early diagnosis which is a challenging task for clinicians and dermatologists. In this regard, CAD systems based on machine learning and image processing techniques are developed to differentiate melanoma lesions from benign and dysplastic nevi using dermoscopic images. Generally, these frameworks are composed of sequential processes: pre-processing, segmentation, and classification. This architecture faces mainly two challenges: (i) each process is complex with the need to tune a set of parameters, and is specific to a given dataset; (ii) the performance of each process depends on the previous one, and the errors are accumulated throughout the framework. In this paper, we propose a framework for melanoma classification based on sparse coding which does not rely on any pre-processing or lesion segmentation. Our framework uses Random Forests classifier and sparse representation of three features: SIFT, Hue and Opponent angle histograms, and RGB intensities. The experiments are carried out on the public PH² dataset using a 10-fold cross-validation. The results show that SIFT sparse-coded feature achieves the highest performance with sensitivity and specificity of 100% and 90.3% respectively, with a dictionary size of 800 atoms and a sparsity level of 2. Furthermore, the descriptor based on RGB intensities achieves similar results with sensitivity and specificity of 100% and 71.3%, respectively for a smaller dictionary size of 100 atoms. In conclusion, dictionary learning techniques encode strong structures of dermoscopic images and provide discriminant descriptors.

Keywords: Melanoma, Classification, Sparse coding, Random forests, Dermoscopy

1. INTRODUCTION

Malignant melanoma is a type of skin cancer and although it accounts for almost 2% of all skin cancer cases, it is the deadliest type causing the vast majority of deaths. The incidence of melanoma has increased in the past decades to currently reach 132,000 melanoma cases, according to the World Health Organisation.¹ The American Cancer Society also reported the estimated deaths of melanoma in 2014 as 9710 individuals and new cases as 76,100 individuals.² Melanoma cancer is incurable in its advanced stages and the patient should go through surgery, possibly immunotherapy, chemotherapy, and/or radiation therapy. However, if it is diagnosed at its early stage, it is the most treatable kind of cancer.^{2,3} In fact the patient survival rate has increased significantly, in the past decades, thanks to early diagnosis and treatment of melanoma in its early stages.

The clinical prognosis of early stage of melanoma is based on the “ABCDE” rule,⁴ standing for: Asymmetry, irregular Borders, variegated Colors, Diameter greater than 6 mm and Evolving stages of the lesion over time. Figure 2 illustrates the first four criterion for melanoma and benign lesions, respectively. At each clinical routine, these criterion are used to visually inspect skin lesions which are acquired through different imaging techniques such as dermoscopy. The similarity between the lesions and the necessity to perform patients follow-up over years makes visual inspection difficult and more prone to errors. Thus, Computer-Aided Diagnosis systems

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(a) Melanoma lesion



(b) Dysplastic lesion

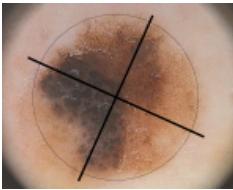


(c) Benign lesion

Figure 1: Samples of PH^2 dataset, representing melanoma, dysplastic and benign lesions, respectively.



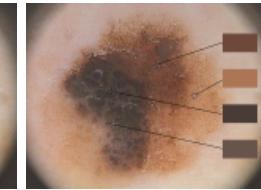
(a) melanoma



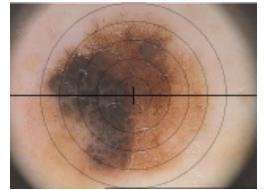
(b) Asymmetric



(c) irregular Borders



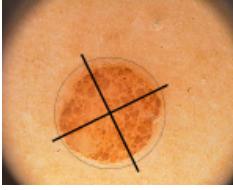
(d) variated Colors



(e) Diameter



(f) benign lesion



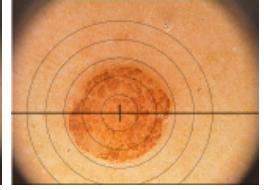
(g) non-Asymmetric



(h) regular Borders



(i) unique Color



(j) Diameter

Figure 2: ABCD-lexicon comparison of two lesions. The top row corresponds to melanoma while the bottom row is a benign lesion.

based on machine learning and image processing techniques have been proposed to assist the dermatologists and clinicians. The proposed algorithms generally attend to mimic the characteristics of the “ABCDE” rule and consist of common steps of pre-processing, segmentation and classification of extracted features.⁵ This sequential architecture is complex and each process of the framework is data-driven.

In this paper, we propose a more general framework which does not need pre-processing and segmentation of the lesions and is based on sparse coded features and Random Forests (RF) classifier⁶ to detect melanoma in dermoscopic images.

The rest of this paper is organized as follows: an overview of related work is presented in Sect. 2. The proposed method is discuss in Sect. 3 while the experiment and obtained results are presented in Sect. 4 and 5, respectively. Finally the paper is concluded in Sect. 6.

2. RELATED WORK

In the past decade, numerous approaches have been proposed for automated recognition of melanoma lesions. The developed methods are commonly based on clinical or dermoscopy modality. These methods follow the usual classification framework of computer vision and consists of four common steps: (i) pre-processing, (ii) segmentation, (iii) feature extraction, and (iv) classification. Korotkov *et al.*⁷ summarizes these methods and their properties. Unfortunately a fair comparison among the state of the art presented methods is not possible due to lack of the benchmark and common datasets.^{5,7} Nevertheless recently a public dataset (PH^2) has been resealed for research purposes, thanks to Mendoncca *et al.*,⁸ Section 4 presents a detailed description of this dataset.

Table 1: Summary of the proposed classification methods using PH² dataset.

Ref	Segmentation	features	Classification		Balancing	Validation	Best performance	
			Classifier	Representation			SE	SP
Ruela <i>et al.</i> ¹¹	✓	Shape, FD ¹	AdB	-	ROS	OvA ¹	92	74
Ruela <i>et al.</i> ¹²	✓	Color statistics	k-NN, AdB	-	ROS	OvA	96	83
Barata <i>et al.</i> ⁹	✓	Opponent histogram gradients	AdB, SVM k-NN	BoW -	ROS	10-fold ² OvA	100	75
Barata <i>et al.</i> ¹³	✓	Opponent histogram	k-NN	BoW	ROS	10-fold	98	86
Abuzaghleh <i>et al.</i> ¹⁴	✓	FFT2, DCT2	SVM	-	-	-	97.7	-
Rastgoo <i>et al.</i> ¹⁵	✓	Shape, color statistics opponent angle and Hue histogram CLBP, GLCM, HoG, Gabor ³	-	RF LC ³	DOS	OvA	94	92

¹ Fourier descriptor (FD), One versus all (Ova).

¹ k-fold corss validation.

² Completed Local Binary Pattern (CLBP), Gray-Level Co-occurrence Matrix (GLCM), Histogram of Gradients (HoG), Learner combination (LC).

Subsequently, we emphasize on the most recent methods which are evaluated using this dataset. Table 1 summarizes these methods.

Barata *et al.*^{9,10} and ruela *et al.*^{11,12} used different subsets of PH² dataset in their works.⁸ Ruela *et al.*^{11,12} compared the role of shape and colors for detection of melanoma vs. benign and dysplastic lesions using AdaBoost (AdB) classifier. Concerning the same problem, Barata *et al.*⁹ proposed to use bag of words (BoW) representation of colors and gradient features. They compared different classifiers, such as AdB, kernel Support Vector Machine (SVM), and k-nearest-neighbor (NN). Their proposed algorithm achieved the highest Sensitivity (SE) and Specificity (SP) of 100% and 75%, respectively, when BoW representation with k-NN classifier was used. The authors, later used a similar scheme (BoW representation, k-NN classifier, and histogram of opponent color space histogram) to compare the effects of manual and automatic segmentation in the classification process. The results indicate that manual outperformed the automatic segmentation Classification frameworks using manual segmentation outperformed the automatic (SE and SP of 98% and 86%, respectively). Feature space, random over-sampling (ROS) was used in all the aforementioned methods to tackle the imbalance problem. **To tackle the imbalance problem, feature space ROS was used in all the aforementioned methods.**

Abuzaghleh *et al.*¹⁴ also used PH² dataset. In this study the authors proposed automated recognition system based on color and shape features such as 2-D Fast Fourier Transform features (FFT2), Discrete Cosine Transform features (DCT2), size and complexity features. The authors proposed two classification approach: (i) multi-class and (ii) two-level classification. In both approaches SVM classifier was used. In later approach, in the first level, normal and abnormal lesions were classified, while in the second level, the abnormal lesions were divided into melanoma and dysplastic lesions. **In later approach, the first level classifies normal and abnormal lesions while the second level works only with the abnormally classified lesions and differentiate melanoma and dysplastic nevi.**

In our previous work, using the same dataset, we compared the effects of various colors, shape and texture features and ensemble approaches.¹⁵ In this work the features were extracted from the segmented area and data space over-sampling (DOS) was used instead of ROS.¹⁵ Using RF ensemble and combination of color and texture features the SE and SP of 94% and 92%, was achieved, respectively.

3. METHODOLOGY

As mentioned in the Sect. 1, the proposed framework, in comparison to previous methods (see Table 1), do not rely on pre-processing an segmentation and focus only on feature detection, extraction and classification. Figure 3 illustrates our proposed framework.

3.1 Feature extraction

3.1.1 Low-level features

In clinical environment, the prognosis of early stage melanoma relies upon visual cues, represented by a set of rules such as “ABCDE”. One of the main characteristic is variegated colors and difference of color representation

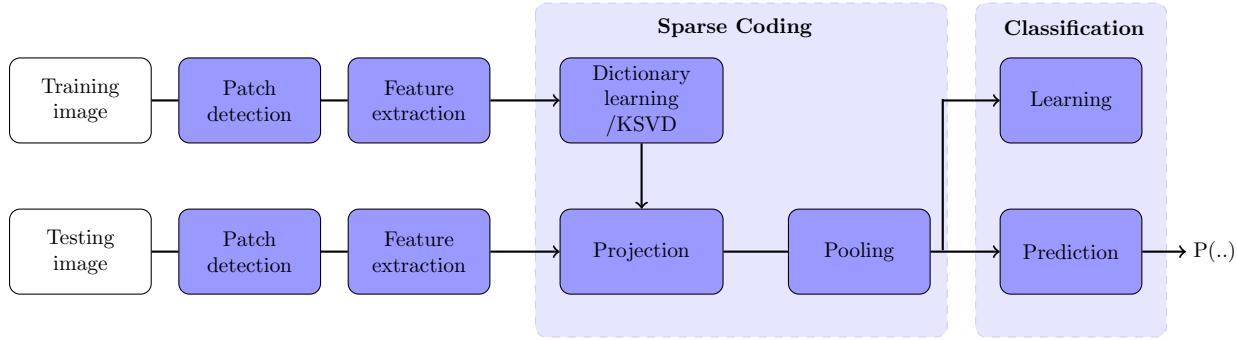


Figure 3: The proposed framework.

between melanoma and benign lesions. Textural difference, irregular and sharp borders are another valuable and distinguishable tool. In this study, three low-level features in line with the previous two discriminative criteria are used. Color variation criteria is described through two descriptors: opponent color space angle and hue histogram (C_1) and R,G,B intensities (C_2). While the texture, gradient and irregular borders is characterized via Scale-Invariant Feature Transform (SIFT) descriptor. These descriptors are presented into details in the remainder of this section. Furthermore, these features are locally extracted by partitioning the dermoscopic images into patches.

Dense Scale-Invariant Feature Transform (SIFT) descriptors are used to encode the local gradient information using an histogram-based representation.¹⁶ SIFT descriptors are extracted over a regular grid such that each grid point is fixed at the center of each image patch. Typically, a region around the center is divided into 4×4 sub-regions from which a 8-bins histogram of the gradient orientations weighted by the gradient magnitudes is computed. Finally, these histograms are concatenated to build the final descriptor with a final size of 128 dimensions. The SIFT implementation used in this work is provided by Vedaldi *et al.*¹⁷

The **opponent color space angle and hue histogram (C_1)** have been first proposed by Van de Weijer and Schmidt as local color features.¹⁸ These descriptors are robust to photometric variations (i.e., shadow, shading, specularities, and light source changes) as well as geometrical variations (i.e, viewpoint, zoom, and object orientation). The hue ($H_{\mathcal{O}}$) and angle ($\theta_{\mathcal{O}}$) of opponent color space ($\mathcal{O}_{1,2,3}$) are formulated as shown in Eq. 2 and Eq. 3, respectively. The opponent color space transformation is defined as in Eq. 1.

$$\begin{pmatrix} \mathcal{O}_1 \\ \mathcal{O}_2 \\ \mathcal{O}_3 \end{pmatrix} = \begin{pmatrix} (R - G)/\sqrt{2} \\ (R + G - 2B)/\sqrt{6} \\ (R + G + B)/\sqrt{3} \end{pmatrix}, \quad (1)$$

$$H^{\mathcal{O}} = \arctan \left(\frac{\sqrt{3}(R - G)}{R + G - 2B} \right), \quad (2)$$

$$\theta_d^{\mathcal{O}} = \arctan \left(\frac{\sqrt{3}(R'_d - G'_d)}{R'_d + G'_d - 2B'_d} \right), \quad (3)$$

where d denotes the spatial coordinates of (x,y) and R'_d , G'_d , B'_d denote the first order derivatives of RGB with respect to the coordinates.

This color descriptor is built by taking a 42 bins histogram for the opponent angle $\theta_d^{\mathcal{O}}$ and the hue channel $H^{\mathcal{O}}$, for a final descriptor size of 84 dimensions.

The color intensities (C_2) represent the color information in a simplest form, their intensities. This descriptor concatenates the color intensities R , G and B to create the feature descriptor.

3.1.2 High-level features

High-level descriptor is computed using sparse coding techniques. Sparse signal representation has become very popular in the past decades and lead to state-of-the-art results in various applications such as face recognition,¹⁹ image denoising, image inpainting,²⁰ and image classification.²¹ The main goal of sparse modeling is to efficiently represent the images as linear combination of a few typical patterns, called atoms, selected from the dictionary. Here, we intend to use sparse representation of the low-level extracted features for melanoma classification. Sparse coding consists of three main steps: (i) dictionary learning, (ii) low-level features projection, and (iii) feature pooling²² (as illustrated in Fig. 3).

Sparse approximation Given a dictionary $\mathbf{D} \in \mathbb{R}^{n \times K}$ composed of K atoms and an original signal $\mathbf{y} \in \mathbb{R}^n$ (i.e., one feature vector), the sparse approximation corresponds to find the sparest vector $\mathbf{x} \in \mathbb{R}^K$ such that:

$$\arg \min_{\mathbf{x}} \|\mathbf{y} - \mathbf{D}\mathbf{x}\|_2 \quad \text{s.t. } \|\mathbf{x}\|_0 \leq \lambda \quad (4)$$

where λ is a specified sparsity level.

Solving the above optimization problem is an NP-hard problem.²³ However, approximate solutions are obtained using greedy algorithms such as Matching Pursuit²⁴ or Orthogonal Matching Pursuit (OMP).^{25,26} We used the batch-OMP variant which offers a more efficient algorithm than the standard OMP for our specific problem.²²

Dictionary learning As stated previously, the sparse approximation is computed given a specific dictionary \mathbf{D} , which involves a learning stage from a set of training data. This dictionary is learned using K -SVD which is a generalized version of K -means clustering and uses Singular Value Decomposition (SVD). The dictionary is built, by iteratively solving the optimization problem of Eq. 5, by alternatively computing the sparse approximation of \mathbf{X} and the dictionary \mathbf{D} .

$$\arg \min_{\mathbf{D}, \mathbf{x}} \|\mathbf{Y} - \mathbf{D}\mathbf{X}\|_2 \quad \text{s.t. } \|\mathbf{x}_i\|_1 \leq \lambda \quad (5)$$

where \mathbf{Y} is a training set of low-level descriptors, \mathbf{X} is the associated sparse coded matrix (i.e., set of high-level descriptors) with a sparsity level λ , and \mathbf{D} is the dictionary with K atoms.

Given \mathbf{D} , \mathbf{X} is computed using the batch-OMP algorithm, while given \mathbf{X} , \mathbf{D} is sequentially updated, one atom at a time using SVD.

Low-level features projection Once the dictionary is learned, each set of low-level features $\mathbf{F}_I \in \mathbb{R}^{n \times p}$ extracted from p patches in an image is encoded using the dictionary \mathbf{D} , solving the optimization problem presented in Eq. 4 such that $\mathbf{F}_I \simeq \mathbf{D}\mathbf{X}_I$.

Feature pooling The sparse coded matrix \mathbf{X}_I is max-pooled to build a final descriptor \mathbf{f} characterizing the given image, such that:

$$\mathbf{f}_i = \max_j (|\mathbf{X}_I(i, j)|), \quad \forall i = 1, \dots, K. \quad (6)$$

Figure 4 illustrate the training and testing stage, using sparse coded features.

3.2 Feature classification

3.2.1 Over-sampling from imbalanced dataset

Similarly to Barata *et al.*,⁹ the imbalanced issue of the dataset is tackled by over-sampling the samples of the minority class. New samples are generated to get a balanced set by randomly repeating original samples of the minority class with an additional Gaussian noise $\mathcal{N}(0, 0.0001)$.

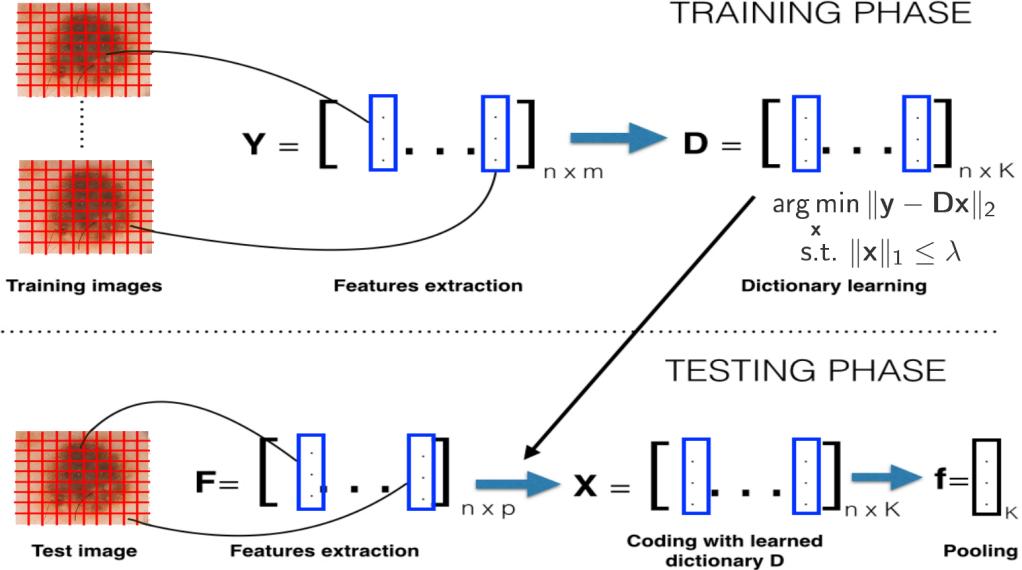


Figure 4: Sparse coded representation for training and testing samples.

3.2.2 Random Forests (RF)

The classification is performed using a RF classifier. RF is an ensemble of decision trees⁶ which generalizes the classification process by applying two types of randomization: at the tree level, each tree is fed by a bootstrap made of S' samples built from the original data of size S such that $S = S'$, and at the node level, a subset of feature dimensions m is randomly selected from the original dimension M such that $m = \sqrt{M}$. The trees in RF are grown to their maximum length without any pruning. Each tree in the ensemble casts a unit vote in the final prediction and the final prediction is based on combination of all the votes. RF is used with 1000 un-pruned trees using gini criterion and the original feature dimension.

4. EXPERIMENTS

The experiments are conducted on the public PH² dataset. This dataset was acquired at *Dermatology Service of Hospital Pedro Hispano, Matosinhos, Portugal*⁸ with Tuebinger Mole Analyzer system with a magnification of 20×. The 8-bits RGB color dermoscopic images were obtained under the same conditions with a resolution of 768 px × 560 px. This dataset contains 200 dermoscopic images divided into 80 benign, 80 dysplastic and 40 melanoma lesions. The lesions are segmented and their histological diagnosis are provided as ground-truth.

In our experiments seven images are discarded due to artefacts such as hair occlusions. Thus, they are conducted on a subset of the dataset consisting of 39 melanoma, 78 benign, and 76 dysplastic lesions. The patch size used to extract the feature is 10 px × 10 px. The three low-level features are sparsely encoded considering three sparsity levels $\lambda = \{2, 4, 8\}$ and different number of atoms $K = \{100, 200, \dots, 1000\}$. The classification is performed in a 10-fold cross-validation model in which 80% of the data is used for training and 20% for testing.

5. RESULTS

The results of the experiment are shown in terms of SE and SP in Table 2. The highest classification rate in respect of each feature type and each sparsity level are highlighted in different shades of gray from dark to light. The results show that $C1$ and SIFT sparse coded features perform better with sparsity levels of 2 and 4, respectively, while $C2$ performs better with sparsity level of 8. In general, larger dictionary sizes lead to better classification performance, independently to the feature type and the sparsity level. More precisely, dictionaries with more than 600 atoms are preferable. Figure 5 illustrate the 12 best results. Although, SIFT and $C1$

Table 2: The obtained results with different number of atoms and sparsity levels. The first, second, and third highest results for each sparsity level are highlighted in different shades of gray from dark to light color, respectively.

Features		Color1				Color2				SIFT									
Sparsity level		2		4		8		2		4		8		2		4		8	
Dictionary size		SE	SP	SE	SP	SE	SP	SE	SP	SE	SP	SE	SP	SE	SP	SE	SP	SE	SP
100		65.6	49.6	51.5	49.4	41.4	59.7	100	71.7	48.5	71.3	59.9	60	1.4	99.4	0	100	1.4	99.7
200		50.1	59.3	52.7	53.5	51.5	50	57.2	64	95.8	86.6	71.4	72	65.6	47.5	34.3	78	20	95
300		59.8	65.4	52.8	71	57.1	62.3	30	80	65.7	75.4	85.7	85.6	58.6	47.7	64.3	51.1	8.6	88.7
400		67	78.6	62.6	81.3	69.9	76	38.5	66	85.8	77.3	78.6	91.4	62.8	74.6	59.9	64.7	71.3	58.2
500		78.7	79	71.4	78.3	51.3	84	54.2	59.7	61.4	69.6	82.9	83.4	58.5	92	61.2	72.9	54	56.7
600		98.6	82.5	68.7	89.6	64	89.9	48.7	78.4	50	64.6	91.4	89.3	85.8	86.6	61.4	73.3	51.3	53.4
700		92.8	89.9	72.8	91.9	54.4	95.9	37.1	75.4	72.8	72	80	82.6	98.6	84.6	73	94.8	47	62.4
800		92.9	81.4	100	88.4	78.5	89.7	40	70.9	58.6	80.1	97.2	83.9	100	90.3	97.1	93	48.5	72.7
900		90	88	80	92	79.9	95.4	25.7	81.3	19.9	91.1	95.7	73.1	95.7	81.8	80	94.5	54.2	78.5
1000		100	86.8	80	89.6	94.3	91.7	34.3	70.7	42.7	76.5	100	73.8	90	83.5	71.4	89.8	51.3	90.3

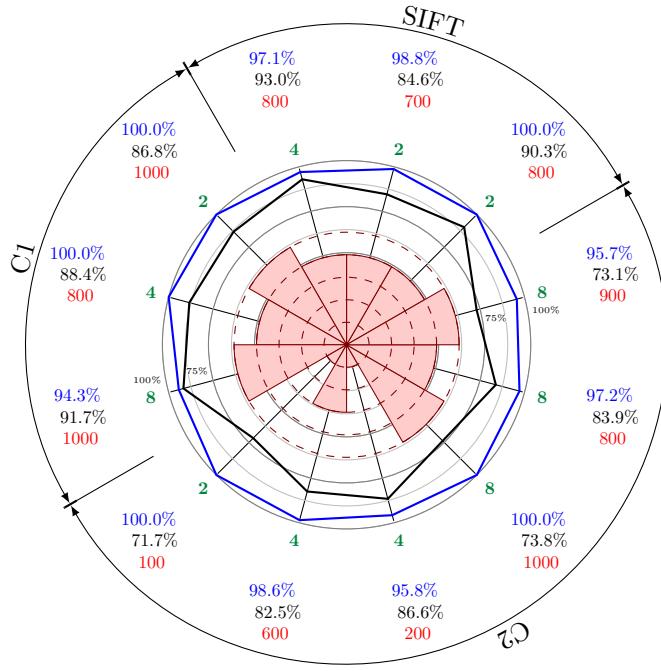


Figure 5: The 12 highest result achieved by RF classifier and sparse representation of SIFT, *color1*, and *color2* features with different **sparsity levels** are illustrated in **blue** and black as sensitivity and specificity, respectively, while their dictionary size is represented in **red**. A comparison of the dictionary sizes is also presented in middle of the graph, which contains five levels with maximum dictionary sizes of 1000, 800, 600, 400, 200 for each level respectively.

sparse coded features achieve the best classification performance in comparison with $C2$, it can be noted that $C2$ features represent the dermoscopic images in their simplest form and create comparable results.

6. CONCLUSION AND FUTURE WORK

In this work, we proposed a novel classification framework of melanoma lesions, based on sparse representation of the low-level features. Our framework does not need the primary steps of pre-processing and segmentation of the lesions and provide more general algorithm to solve this problem. We proposed to use a well-known color descriptor based on Hue and angel histograms of opponent color space, and SIFT as a texture descriptor. We also consider to represent the images in their simplest form and consider the second color descriptor as R,G and B intensities. An extensive comparison based on different dictionary sizes and several sparsity levels were carried out on the PH² dataset. The results highlighted the advantage of the proposed method where an RF classifier and a sparse representation of SIFT features with a dictionary size of 800 and sparsity level of 2 achieved the highest performance (SE and SP of 100% and 90.3%, respectively). In general, the obtained results outperform the state of the art. As avenues for future research, a comparison of sparse learned dictionary with Bag-of-Word models can be performed.

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