

Model B : Estimation Results

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Estimation results of **Model B**, specified by the following input:

```
q <- .01
# transition matrix
Q <- rbind( c(0, q, 0, q),
            c(q, 0, q, q),
            c(0, 0, 0, q),
            c(0, 0, 0, 0))
# misclassification matrix
E <- rbind( c( 0, 0, 0, 0),
            c( 0, 0, .1, 0),
            c( 0, 0, 0, 0),
            c( 0, 0, 0, 0) )
# transition names
qnames = c(
  "Healthy - Mild",    # q12
  # "Healthy - Severe", # q13
  "Healthy - Dead",    # q14
  "Mild - Healthy",    # q21
  "Mild - Severe",     # q23
  "Mild - Dead",       # q24
  # "Severe - Healthy", # q31
  # "Severe - Mild",    # q32
  "Severe - Dead"     # q34
)
```

Load environmet

Save fitted models here :

```
[1] "./data/shared/derived/models/model-b-mod-2/"
```

Load data

Before ms encoding:

	id	fu_year	died	age_bl	male	edu	age_death	age_at_visit	mmse	presumed_alive
5120	50402431	0	1	91.41136	FALSE	16	94.82272	91.41136	19	FALSE
5121	50402431	1	1	91.41136	FALSE	16	94.82272	92.33402	12	FALSE
5122	50402431	2	1	91.41136	FALSE	16	94.82272	93.34702	5	FALSE
5123	50402431	3	1	91.41136	FALSE	16	94.82272	94.34634	0	FALSE

After ms encoding

	id	fu_year	died	age_bl	male	edu	age	state	presumed_alive	mmse	firstobs
5120	50402431	0	1	91.41136	FALSE	16	91.41136	3	FALSE	19	1
5121	50402431	1	1	91.41136	FALSE	16	92.33402	3	FALSE	12	0
5122	50402431	2	1	91.41136	FALSE	16	93.34702	3	FALSE	5	0
5123	50402431	3	1	91.41136	FALSE	16	94.34634	3	FALSE	0	0
51201	50402431	NA	1	91.41136	FALSE	16	94.82272	4	FALSE	NA	0

Remove cases

```
#### 1) Remove observations with missing age
# Initial number of observations with missing age :
sum(is.na(ds_ms$age))
```

```
[1] 1
```

```
ds_clean <- ds_ms %>%
  dplyr::filter(!is.na(age))
# Resultant number of observations with missing age
sum(is.na(ds_clean$age))
```

```
[1] 0
```

```
#### 3) Remove subjects with only ONE observed data point
# Initial number of subjects who have *n* observed data points
ds_clean %>%
  dplyr::group_by(id) %>%
  dplyr::summarize(n_data_points = n()) %>%
  dplyr::group_by(n_data_points) %>%
  dplyr::summarize(n_people=n()) %>%
  print()
```

```
# A tibble: 17 × 2
  n_data_points n_people
    <int>         <int>
1           1         119
```

2	2	205
3	3	184
4	4	180
5	5	190
6	6	104
7	7	108
8	8	113
9	9	127
10	10	116
11	11	110
12	12	71
13	13	21
14	14	14
15	15	13
16	16	17
17	17	3

```
# Determine which ids have only a single observation
```

```
remove_ids <- ds_clean %>%
  dplyr::group_by(id) %>%
  dplyr::summarize(n_data_points = n()) %>%
  dplyr::arrange(n_data_points) %>%
  dplyr::filter(n_data_points==1) %>%
  dplyr::select(id)
```

```
remove_ids <- remove_ids$id
```

```
# How many subjects to be removed from the data set:
```

```
length(remove_ids)
```

```
[1] 119
```

```
ds_clean <- ds_clean %>%
  dplyr::filter(!(id %in% remove_ids))
# Resultant number of subjects who have *n* observed data points
ds_clean %>%
  dplyr::group_by(id) %>%
  dplyr::summarize(n_data_points = n()) %>%
  dplyr::group_by(n_data_points) %>%
  dplyr::summarize(n_people=n()) %>%
  print()
```

```
# A tibble: 16 × 2
```

	n_data_points	n_people
	<int>	<int>
1	2	205
2	3	184
3	4	180
4	5	190
5	6	104
6	7	108
7	8	113
8	9	127
9	10	116
10	11	110
11	12	71
12	13	21

13	14	14
14	15	13
15	16	17
16	17	3

```
#### 3) Remove subjects with IMS at the first observation
# Initial view of subjects with intermediate missing state at first observation:
ids_firstobs_ims <- ds_clean %>%
  dplyr::filter(firstobs == TRUE & state == -1) %>%
  dplyr::select(id) %>% print()
```

```
      id
1 80333458
2 90214403
3 90447310
4 91804757
```

```
ids_firstobs_ims <- ids_firstobs_ims[, "id"]
ds_clean <- ds_clean %>%
  dplyr::filter(!id %in% ids_firstobs_ims)
# Resultant view of subjects with intermediate missing state at first observation:
ds_clean %>%
  dplyr::filter(firstobs == TRUE & state == -1) %>%
  dplyr::select(id) %>% print()
```

```
[1] id
<0 rows> (or 0-length row.names)
```

Categorize covariates

How education was categorized:

	educatF	edu	n
1	0-9 years	0	4
2	0-9 years	2	6
3	0-9 years	3	10
4	0-9 years	4	17
5	0-9 years	5	20
6	0-9 years	6	48
7	0-9 years	7	27
8	0-9 years	8	178
9	0-9 years	9	76
10	10-11 years	10	167
11	10-11 years	11	225
12	>11 years	12	2400
13	>11 years	13	862
14	>11 years	14	1199
15	>11 years	15	554
16	>11 years	16	2132
17	>11 years	17	486
18	>11 years	18	942
19	>11 years	19	255
20	>11 years	20	286

21	>11 years	21	207
22	>11 years	22	61
23	>11 years	23	37
24	>11 years	24	26
25	>11 years	25	11
26	>11 years	28	21

Frequencies of categorized education :

```
# A tibble: 3 × 2
  educatF      n
  <fctr> <int>
1 0-9 years  386
2 10-11 years 392
3 >11 years 9479
```

Create dummy variables for testing effects of education:

-1	0	1	<NA>
386	392	9479	0

	0	1
-1	386	0
0	0	392
1	9479	0

	0	1
-1	386	0
0	392	0
1	0	9479

Age diagnostic

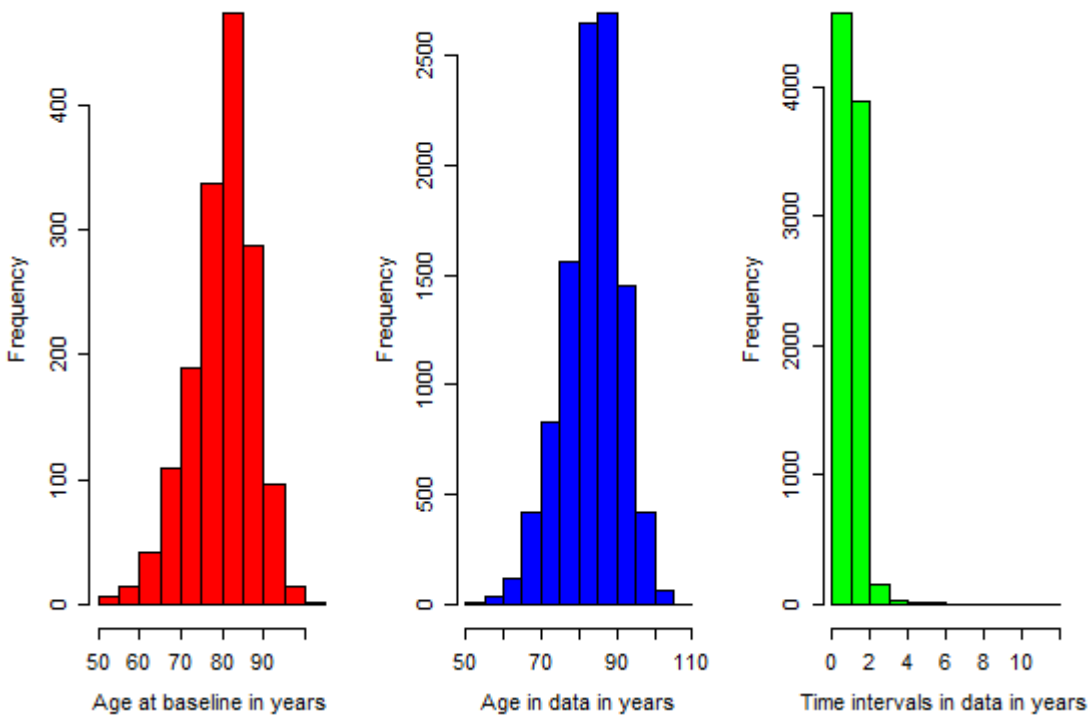
Minimum interval length : 0.00273785

Maximum interval length : 11.86858

Time intervals between observations within individuals:

	0%	25%	50%	75%	100%
	0.00	0.96	1.00	1.03	11.87

Graphs of age distribution :



Estimation prep

Number of subjects with intermediate missing state (-1) : 104

Number of subjects with right censored state (-2) : 46

Number of subjects with either IMS or RC state(s) : 149

Number of subjects with both IMS and RC state(s) : 1

Centering decisions :

The variable `age` is centered at : 75

The variable `age_bl` is centered at : 75

The following dataset will be passed to msm call (view for one person):

	id	age_bl	male	edu	educat	educatF	edu_low_med	edu_low_high	firstobs	fu_year	age	stat
1	90544686	7.696783	0	12	1 >11 years		0	1	1	0	7.696783	
2	90544686	7.696783	0	12	1 >11 years		0	1	0	1	8.682409	

3	90544686	7.696783	0	12	1 >11 years	0	1	0	2	9.731006
4	90544686	7.696783	0	12	1 >11 years	0	1	0	3	10.689254
5	90544686	7.696783	0	12	1 >11 years	0	1	0	4	11.691307
6	90544686	7.696783	0	12	1 >11 years	0	1	0	5	12.709788
7	90544686	7.696783	0	12	1 >11 years	0	1	0	6	13.665298
8	90544686	7.696783	0	12	1 >11 years	0	1	0	7	14.678303
9	90544686	7.696783	0	12	1 >11 years	0	1	0	8	15.680356
10	90544686	7.696783	0	12	1 >11 years	0	1	0	9	16.709788

Subject count : 1572

Frequency of states at baseline

```
# A tibble: 3 × 3
  state count  pct
  <dbl> <int> <dbl>
1     1  1189  0.76
2     2   281  0.18
3     3   102  0.06
```

State table:

	to					
from	-2	-1	1	2	3	4
-2	32	0	0	0	0	0
-1	0	25	27	13	26	47
1	32	59	4855	715	120	251
2	8	20	534	478	256	146
3	6	34	24	96	649	232

The initial values for estimation : 0.76 0.18 0.06 0

Specifications

Fitting functions

```
estimate_multistate <- function(
  model_name
  ,ds                # data object
  ,Q                 # Q-matrix of transitions
  ,E                 # misspecification matrix
  ,qnames            # names of the rows in the Q matrix
  ,cf                # string with covariate names for forward transitions
  ,cb                # string with covariate names for backward transitions
  ,cd                # string with covariate names for death transitions
){
  cov_forward <- as.formula(paste0("~",cf))
  cov_backward <- as.formula(paste0("~",cb))
  cov_death   <- as.formula(paste0("~",cd))
  # covariates_ <- as.formula(paste0("~",cov_names))
  covariates_ = list(
```

```

    "1-2"      = cov_forward,
    "2-3"      = cov_forward,
    "2-1"      = cov_backward,
    "1-4"      = cov_death,
    "2-4"      = cov_death,
    "3-4"      = cov_death
  )
  model <- msm(
    formula      = state ~ age,
    subject      = id,
    data         = ds,
    center       = FALSE,
    qmatrix      = Q,
    ematrix      = E,
    death        = TRUE,
    covariates   = covariates_,
    censor       = c(-1,-2),
    censor.states = list(c(1,2,3), c(1,2,3)),
    method       = method_,
    constraint   = constraint_,
    fixedpars    = fixedpars_,
    initprobs    = initprobs_,
    est.initprobs = TRUE,
    control      = list(trace=0,REPORT=1,maxit=1000,fnscale=10000)
  )
  # model <- paste0("test", covariates_)
  saveRDS(model, paste0(pathSaveFolder,model_name,".rds"))
  return(model)
}

```

Support functions

```

get_crude_Q <- function(ds, Q, cov_names){
  formula_ <- as.formula(paste0("state ~ ",cov_names))
  Q_crude <- crudeinits.msm(
    formula = formula_,
    subject = id,
    qmatrix = Q,
    data = ds,
    censor      = c(-1,-2),
    censor.states = list(c(1,2,3), c(1,2,3))
  )
  return(Q_crude)
}

msm_summary <- function(model){
  cat("\n-2loglik =", model$minus2loglik,"\n")
  cat("Convergence code =", model$opt$convergence,"\n")
  p <- model$opt$par
  p.se <- sqrt(diag(solve(1/2*model$opt$hessian)))
  print(cbind(p=round(p,digits),
              se=round(p.se,digits),"Wald ChiSq"=round((p/p.se)^2,digits),

```



```

        "Pr>ChiSq"=round(1-pchisq((p/p.se)^2,df=1),digits)),
        quote=FALSE)
}

msm_details <- function(model){
  # intensity matrix
  cat("\n Intensity matrix : \n")
  print(qmatrix.msm(model))
  # qmatrix.msm(model, covariates = list(male = 0))
  # transition probability matrix
  t_ <- 2
  cat("\n Transition probability matrix for t = ", t_," : \n")
  print(pmatrix.msm(model, t = t_)) # t = time, in original metric
  # misclassification matrix
  cat("\n Misclassification matrix : \n")
  suppressWarnings(print(ematrix.msm(model), warnings=F))
  # hazard ratios
  cat("\n Hazard ratios : \n")
  print(hazard.msm(model))
  # mean sojourn times
  cat("\n Mean sojourn times : \n")
  print(sojourn.msm(model))
  # probability that each state is next
  cat("\n Probability that each state is next : \n")
  suppressWarnings(print(pnext.msm(model)))
  # total length of stay
  cat("\n Total length of stay : \n")
  print(totlos.msm(model))
  # expected number of visits to the state
  cat("\n Expected number of visits to the state : \n")
  suppressWarnings(print(envisits.msm(model)))
  # ratio of transition intensities
  # qratio.msm(model, ind1 = c(2,1), ind2 = c(1,2))
}

```

Model

```

q <- .01
# transition matrix
Q <- rbind( c(0, q, 0, q),
            c(q, 0, q, q),
            c(0, 0, 0, q),
            c(0, 0, 0, 0))
# misclassification matrix
E <- rbind( c( 0, 0, 0, 0),
            c( 0, 0, .1, 0),
            c( 0, 0, 0, 0),
            c( 0, 0, 0, 0) )
# transition names
qnames = c(
  "Healthy - Mild", # q12
  "Healthy - Severe", # q13

```

```

"Healthy - Dead", # q14
"Mild - Healthy", # q21
"Mild - Severe", # q23
"Mild - Dead",    # q24
# "Severe - Healthy",# q31
# "Severe - Mild",  # q32
"Severe - Dead"   # q34
)

```

msm options

```

digits = 2
method_ = "BFGS"      # alternatively, if does not converge "Nedler-Mead"
constraint_ = NULL    # additional model constraints
fixedpars_ = NULL     # fixed parameters
initprobs_ = initial_probabilities

```

```

# turn this chunk OFF when printing the report
# compile model objects with msm() call
# each model will be saved in the specified folder, namely pathSaveFolder
(Q_crude <- get_crude_Q(ds, Q, "age"))

```

	[,1]	[,2]	[,3]	[,4]
[1,]	-0.1569916	0.1141470	0.0000000	0.04284465
[2,]	0.3504402	-0.6212645	0.1696731	0.10115125
[3,]	0.0000000	0.0000000	-0.2434208	0.24342081
[4,]	0.0000000	0.0000000	0.0000000	0.00000000

```

# estimate_multistate("mB_mod2_1", ds, Q_crude, E, qnames,
#
#                       cf = "age + male + edu_low_med + edu_low_high",
#                       cb = "age",
#                       cd = "age + male")
#
# (Q_crude <- get_crude_Q(ds, Q, "age"))
# m2 <- estimate_multistate("mB_mod2_2", ds, Q_crude, E, qnames,
#
#                       cf = "age + male + edu_low_med + edu_low_high",
#                       cb = "age",
#                       cd = "age + male + edu_low_med + edu_low_high")
#

```

Model results

model 1

The model was fitted using the following specification of covariates:

```

# Forward transitions:
"1-2"      = "age + male + edu_low_med + edu_low_high"
"2-3"      = "age + male + edu_low_med + edu_low_high"
# Backward transitions:
"2-1"      = "age"
# Death transitions:

```

```

"1-4"      = "age + male"
"2-4"      = "age + male"
"3-4"      = "age + male"

```

summary

```

-2loglik = 15002.66
Convergence code = 0

```

	p	se	Wald	ChiSq	Pr>ChiSq
qbase	-1.66	0.19		77.54	0.00
qbase	-4.21	0.18		525.29	0.00
qbase	-0.27	0.08		10.87	0.00
qbase	-1.98	0.30		42.46	0.00
qbase	-3.40	0.42		67.10	0.00
qbase	-2.28	0.20		132.11	0.00
qcov	0.08	0.01		157.07	0.00
qcov	0.08	0.01		31.02	0.00
qcov	-0.02	0.01		7.70	0.01
qcov	0.05	0.01		23.00	0.00
qcov	0.06	0.03		6.42	0.01
qcov	0.07	0.01		35.21	0.00
qcov	0.29	0.08		13.10	0.00
qcov	0.42	0.22		3.67	0.06
qcov	-0.18	0.16		1.38	0.24
qcov	0.72	0.28		6.50	0.01
qcov	0.36	0.14		6.65	0.01
qcov	-0.27	0.24		1.32	0.25
qcov	-0.12	0.40		0.10	0.75
qcov	-0.56	0.18		9.90	0.00
qcov	-0.17	0.29		0.33	0.56
p	-2.15	0.09		590.61	0.00
initp	-1.33	0.06		432.47	0.00
initp	-2.84	0.13		481.41	0.00

details

```

Intensity matrix :

```

	State 1	State 2	State 3
State 1	-0.25700 (-0.27608,-0.23925)	0.22532 (0.20772, 0.24440)	0
State 2	0.64404 (0.58426, 0.70994)	-0.88548 (-0.95896,-0.81763)	0.17435 (0.14811, 0.20524)
State 3	0	0	-0.19402 (-0.23913,-0.15743)
State 4	0	0	0

```

State 4
State 1 0.03169 ( 0.02583, 0.03888)
State 2 0.06708 ( 0.04373, 0.10290)
State 3 0.19402 ( 0.15743, 0.23913)
State 4 0

```

```

Transition probability matrix for t = 2 :

```

	State 1	State 2	State 3	State 4
State 1	0.7224079	0.1683030	0.03522663	0.0740625

```

State 2 0.4810716 0.2529645 0.14008255 0.1258814
State 3 0.0000000 0.0000000 0.67838075 0.3216193
State 4 0.0000000 0.0000000 0.00000000 1.0000000

```

Misclassification matrix :

	State 1	State 2	State 3	State 4
State 1	1.0000	0	0	0
State 2	0	0	0.1039 (0.08881,0.1212)	0
State 3	0	0	1.0000	0
State 4	0	0	0	1.0000

Hazard ratios :

\$age

	HR	L	U
State 1 - State 2	1.080777	1.0677267	1.0939862
State 1 - State 4	1.085146	1.0543871	1.1168023
State 2 - State 1	0.979584	0.9654133	0.9939627
State 2 - State 3	1.055787	1.0326212	1.0794722
State 2 - State 4	1.066975	1.0148080	1.1218231
State 3 - State 4	1.071141	1.0470990	1.0957349

\$male

	HR	L	U
State 1 - State 2	1.3383578	1.1429501	1.567174
State 1 - State 4	1.5254411	0.9901823	2.350043
State 2 - State 1	1.0000000	1.0000000	1.0000000
State 2 - State 3	0.8325447	0.6129781	1.130759
State 2 - State 4	2.0610765	1.1822137	3.593290
State 3 - State 4	1.4287728	1.0892843	1.874067

\$edu_low_med

	HR	L	U
State 1 - State 2	0.7596424	0.4753863	1.213869
State 1 - State 4	1.0000000	1.0000000	1.0000000
State 2 - State 1	1.0000000	1.0000000	1.0000000
State 2 - State 3	0.8827809	0.4036470	1.930653
State 2 - State 4	1.0000000	1.0000000	1.0000000
State 3 - State 4	1.0000000	1.0000000	1.0000000

\$edu_low_high

	HR	L	U
State 1 - State 2	0.5719336	0.4038369	0.8100003
State 1 - State 4	1.0000000	1.0000000	1.0000000
State 2 - State 1	1.0000000	1.0000000	1.0000000
State 2 - State 3	0.8474639	0.4823419	1.4889749
State 2 - State 4	1.0000000	1.0000000	1.0000000
State 3 - State 4	1.0000000	1.0000000	1.0000000

Mean sojourn times :

	estimates	SE	L	U
State 1	3.890975	0.14215479	3.622098	4.179811
State 2	1.129335	0.04593426	1.042800	1.223050
State 3	5.154020	0.54965949	4.181848	6.352198

```

Probability that each state is next :
      State 1      State 2      State 3      State 4
State 1 0      0.87670 (0.84783,0.8990) 0      0.12330 (0.10104,0.1
State 2 0.72734 (0.68784,0.7600) 0      0.19690 (0.16834,0.2264) 0.07576 (0.04796,0.1
State 3 0      0      0      1.00000 (1.00000,1.0
State 4 0      0      0      0

```

```

Total length of stay :
      State 1      State 2      State 3      State 4
10.738426  2.732486  2.455486      Inf

```

```

Expected number of visits to the state :
      State 1      State 2      State 3      State 4
1.7598289  2.4195539  0.4764214  1.0000000

```

model 2

The model was fitted using the following specification of covariates:

```

# Forward transitions:
"1-2"      = "age + age_bl + male + edu_low_med + edu_low_high"
"2-3"      = "age + age_bl + male + edu_low_med + edu_low_high"
# Backward transitions:
"2-1"      = "age + age_bl"
# Death transitions:
"1-4"      = "age + age_bl + male + edu_low_med + edu_low_high"
"2-4"      = "age + age_bl + male + edu_low_med + edu_low_high"
"3-4"      = "age + age_bl + male + edu_low_med + edu_low_high"

```

summary

```

-2loglik = 15001.18
Convergence code = 0
      p      se Wald ChiSq Pr>ChiSq
qbase -1.69 0.19      75.02      0.00
qbase -4.26 0.68      39.60      0.00
qbase -0.28 0.08      11.11      0.00
qbase -1.96 0.31      40.42      0.00
qbase -3.71 0.87      18.20      0.00
qbase -2.18 0.30      52.27      0.00
qcov  0.08 0.01     157.60      0.00
qcov  0.08 0.01      30.52      0.00
qcov -0.02 0.01       7.49      0.01
qcov  0.05 0.01      22.97      0.00
qcov  0.06 0.03       5.71      0.02
qcov  0.07 0.01      36.01      0.00
qcov  0.29 0.08      12.83      0.00
qcov  0.44 0.22       3.92      0.05
qcov -0.16 0.16       1.00      0.32
qcov  0.69 0.29       5.49      0.02
qcov  0.38 0.14       7.23      0.01

```

qcov	-0.26	0.25	1.07	0.30
qcov	0.31	0.79	0.16	0.69
qcov	-0.12	0.42	0.09	0.77
qcov	0.06	1.18	0.00	0.96
qcov	0.12	0.41	0.08	0.78
qcov	-0.53	0.18	8.20	0.00
qcov	0.03	0.67	0.00	0.97
qcov	-0.20	0.30	0.43	0.51
qcov	0.34	0.88	0.15	0.70
qcov	-0.15	0.27	0.32	0.57
p	-2.16	0.09	590.25	0.00
initp	-1.33	0.06	433.05	0.00
initp	-2.85	0.13	481.80	0.00

details

Intensity matrix :

	State 1	State 2	State 3
State 1	-0.25675 (-0.27582,-0.23900)	0.22523 (0.20762, 0.24433)	0
State 2	0.64325 (0.58349, 0.70914)	-0.88436 (-0.95786,-0.81650)	0.17361 (0.14726, 0.20467)
State 3	0	0	-0.19007 (-0.23563,-0.15332)
State 4	0	0	0

	State 4
State 1	0.03152 (0.02557, 0.03886)
State 2	0.06750 (0.04310, 0.10571)
State 3	0.19007 (0.15332, 0.23563)
State 4	0

Transition probability matrix for t = 2 :

	State 1	State 2	State 3	State 4
State 1	0.7226273	0.1684136	0.03518858	0.07377055
State 2	0.4809945	0.2533314	0.14023226	0.12544192
State 3	0.0000000	0.0000000	0.68376659	0.31623341
State 4	0.0000000	0.0000000	0.00000000	1.00000000

Misclassification matrix :

	State 1	State 2	State 3	State 4
State 1	1.0000	0	0	0
State 2	0	0	0.1038 (0.08874,0.1212)	0
State 3	0	0	1.0000	0
State 4	0	0	0	1.0000

Hazard ratios :

\$age	HR	L	U
State 1 - State 2	1.0810352	1.0679642	1.0942662
State 1 - State 4	1.0851747	1.0541584	1.1171036
State 2 - State 1	0.9798409	0.9656587	0.9942314
State 2 - State 3	1.0562092	1.0328517	1.0800948
State 2 - State 4	1.0669022	1.0117297	1.1250835
State 3 - State 4	1.0732165	1.0487328	1.0982718

\$male

	HR	L	U
State 1 - State 2	1.3352491	1.139855	1.564137
State 1 - State 4	1.5558672	1.004304	2.410349
State 2 - State 1	1.0000000	1.000000	1.000000
State 2 - State 3	0.8549199	0.628904	1.162162
State 2 - State 4	1.9935253	1.119284	3.550613
State 3 - State 4	1.4556315	1.107118	1.913855

\$edu_low_med

	HR	L	U
State 1 - State 2	0.7746750	0.4779028	1.255739
State 1 - State 4	1.3660242	0.2927307	6.374536
State 2 - State 1	1.0000000	1.000000	1.000000
State 2 - State 3	0.8851032	0.3914057	2.001524
State 2 - State 4	1.0667119	0.1059017	10.744627
State 3 - State 4	1.1239639	0.5033243	2.509902

\$edu_low_high

	HR	L	U
State 1 - State 2	0.5892899	0.4103330	0.8462946
State 1 - State 4	1.0275460	0.2767308	3.8154442
State 2 - State 1	1.0000000	1.000000	1.000000
State 2 - State 3	0.8221826	0.4573361	1.4780909
State 2 - State 4	1.4076005	0.2532502	7.8236442
State 3 - State 4	0.8566714	0.5022316	1.4612500

Mean sojourn times :

	estimates	SE	L	U
State 1	3.894867	0.1423680	3.625592	4.184142
State 2	1.130764	0.0460590	1.043999	1.224739
State 3	5.261238	0.5767942	4.243947	6.522377

Probability that each state is next :

	State 1	State 2	State 3	State 4
State 1	0	0.87723 (0.84986,0.9016)	0	0.12277 (0.09840,0.14917)
State 2	0.72737 (0.68919,0.7613)	0	0.19631 (0.16746,0.2289)	0.07632 (0.04951,0.10313)
State 3	0	0	0	1.00000 (1.00000,1.00000)
State 4	0	0	0	0

Total length of stay :

State 1	State 2	State 3	State 4
10.761354	2.740683	2.503303	Inf

Expected number of visits to the state :

State 1	State 2	State 3	State 4
1.7629577	2.4237453	0.4758011	1.0000000

Session Info

```
sessionInfo()
```

```
R version 3.3.1 (2016-06-21)
```

```
Platform: x86_64-w64-mingw32/x64 (64-bit)
```

```
Running under: Windows 10 x64 (build 14393)
```

```
locale:
```

```
[1] LC_COLLATE=English_United States.1252 LC_CTYPE=English_United States.1252 LC_MONETARY=English_United States.1252
[4] LC_NUMERIC=C LC_TIME=English_United States.1252
```

```
attached base packages:
```

```
[1] stats      graphics  grDevices  utils      datasets  methods   base
```

```
other attached packages:
```

```
[1] msm_1.6.1      magrittr_1.5  nnet_7.3-12   knitr_1.14
```

```
loaded via a namespace (and not attached):
```

```
[1] Rcpp_0.12.6      formatR_1.4      nloptr_1.0.4      plyr_1.8.4        tools_3.3.1        dig
[7] lme4_1.1-12      evaluate_0.9      tibble_1.2        gtable_0.2.0      nlme_3.1-128      lat
[13] mgcv_1.8-14      Matrix_1.2-7.1    DBI_0.5           yaml_2.1.13       parallel_3.3.1     Spa
[19] mvtnorm_1.0-5    expm_0.999-0      dplyr_0.5.0       stringr_1.1.0     MatrixModels_0.4-1 gri
[25] R6_2.1.3         survival_2.39-5    rmarkdown_1.0     minqa_1.2.4       ggplot2_2.1.0      car
[31] scales_0.4.0     htmltools_0.3.5   splines_3.3.1     MASS_7.3-45       assertthat_0.1     pbk
[37] testit_0.5       colorspace_1.2-6  quantreg_5.26     stringi_1.1.1     lazyeval_0.2.0     mun
```