

# Binary Tree

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## Preorder

[144. Binary Tree Preorder Traversal](#)

**Idea: root, left, right**

迭代就要有个Stack 不停往左下压栈，左下Node为None之后一个一个pop栈顶Node，往右下再找。

Iterative Solution

```
def preorderTraversal(self, root: Optional[TreeNode]) -> List[int]:
    res, stack = [], []
    while root or stack:
        if root:
            res.append(root.val)
            stack.append(root)
            root = root.left
        else:
            root = stack.pop().right

    return res
```

Recursive Solution

```
def preorderTraversal(self, root: Optional[TreeNode]) -> List[int]:
    if not root:
        return []
    return [root.val] + self.preorderTraversal(root.left) +
        self.preorderTraversal(root.right)
```

## Inorder

[94. Binary Tree Inorder Traversal](#)

**Idea: left, root, right**

Iterative Solution

画个图就清楚了 要先无脑往左走 压栈 走不动了 先pop最底下的 然后加进result list里面 之后再往右边找

```
def inorderTraversal(self, root: Optional[TreeNode]) -> List[int]:
    res, stack = [], []
    while root or stack:
        if root:
            stack.append(root)
            root = root.left
        else:
            root = stack.pop()
            res.append(root.val)
            root = root.right
    return res
```

Recursive Solution

```
def inorderTraversal(self, root: Optional[TreeNode]) -> List[int]:
    if not root:
        return []

    return self.inorderTraversal(root.left) + [root.val] +
self.inorderTraversal(root.right)
```

## Postorder

### [145. Binary Tree Postoder Traversal](#)

Iterative Solution

```
def postorderTraversal(self, root: Optional[TreeNode]) -> List[int]:
    res, stack = [], []
    while root or stack:
        if root:
            # keep to right
            res.append(root.val)
            stack.append(root)
            root = root.right
        else:
            root = stack.pop().left

    return res[::-1]
```

## Recursive Solution

```
def postorderTraversal(self, root: Optional[TreeNode]) -> List[int]:
    if not root: return []
    return self.postorderTraversal(root.left) + self.postorderTraversal(root.right) +
    [root.val]
```

## Level Order Traversal -> BFS, Queue 层序遍历

### [102. Binary Tree Level Order Traversal](#)

**Idea:** 用Queue存每一层的Node List存每一层Node的left、right *value*，生成时先把root存进queue

## Iterative Solution

```
def levelOrder(self, root: Optional[TreeNode]) -> List[List[int]]:
    res = []
    if not root: return res
    q = collections.deque()
    q.append(root)
    while q:
        temp_res = []
        for _ in range(len(q)):
            cur = q.popleft()
            temp_res.append(cur.val)
            if cur.left:
                q.append(cur.left)
            if cur.right:
                q.append(cur.right)

        res.append(temp_res)
    return res
```

## Recursive Solution

```
def levelOrder(self, root: Optional[TreeNode]) -> List[List[int]]:
    # recursive, use dfs
    res = []

    def dfs(root, depth):
```

```

        # depth means the level number in Binary Tree
        if not root: return []
        if len(res) == depth: res.append([])
        res[depth].append(root.val)

        if root.left: dfs(root.left, depth + 1)
        if root.right: dfs(root.right, depth + 1)

    dfs(root, 0)
    return res

```

## Level Order Traversal 2

### [107. Binary Tree Level Order Traversal II](#)

**Idea: Just same with Level Order Traverse 1, just need to reverse the list at last**

Iterative Solution

```

def levelOrderBottom(self, root: Optional[TreeNode]) -> List[List[int]]:
    # level order traversal, reverse list at last
    res = []
    if not root: return res
    q = collections.deque([root])
    while q:
        tmp_res = []
        for _ in range(len(q)):
            cur = q.popleft()
            tmp_res.append(cur.val)
            if cur.left:
                q.append(cur.left)
            if cur.right:
                q.append(cur.right)
        res.append(tmp_res)

    return res[::-1]

```

### [199. Binary Tree Right Side View](#)

**Idea: Find all right view means that every last node.val in corresponding level**

Iterative Solution

```

def rightSideView(self, root: Optional[TreeNode]) -> List[int]:
    # bfs but only add right val (which is the last node value on that level)
    res = []

```

```

if not root: return res
q = collections.deque([root])
while q:
    # give a variable on len(q) since the size of queue will change
    size = len(q)
    for i in range(size):
        cur = q.popleft()
        if cur.left:
            q.append(cur.left)
        if cur.right:
            q.append(cur.right)
        if i == size - 1:
            res.append(cur.val)
return res

```

Recursive Solution

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### [637. Average of Levels in Binary Tree](#)

**Idea: Find every level node.val, put in a list, get the average by doing  $\text{sum}(\text{lst}) / \text{len}(\text{lst})$**

Iterative Solution

```

def averageOfLevels(self, root: Optional[TreeNode]) -> List[float]:
    # get the sum of level node values and get the average( sum(lst) / len(lst) )

    res = []
    if not root: return res
    q = collections.deque([root])
    while q:
        level_lst = []
        for _ in range(len(q)):
            cur = q.popleft()
            level_lst.append(cur.val)
            if cur.left:
                q.append(cur.left)
            if cur.right:
                q.append(cur.right)

        res.append(sum(level_lst) / len(level_lst))

    return res

```

## Recursive Solution

...

### [429. N-ary Tree Level Order Traversal](#)

**Idea: same with level order traversal of binary tree, just need to loop through all the children in corresponding level**

## Iterative Solution

```
def levelOrder(self, root: 'Node') -> List[List[int]]:
    # N-ary tree, add children in queue one by one 多个for loop去找children其余没区别
    res = []
    if not root: return res
    q = collections.deque([root])
    while q:
        size = len(q)
        level_lst = []
        for _ in range(size):
            cur = q.popleft()
            level_lst.append(cur.val)
            for child in cur.children:
                q.append(child)
        res.append(level_lst)
    return res
```

## Recursive Solution

...

### [515. Find Largest Value in Each Tree Row](#)

**Idea: Same with 102, just get max value in each level**

## Iterative Solution

```
def largestValues(self, root: Optional[TreeNode]) -> List[int]:
    # find largest number in each level, store in a list and find max
    res = []
    if not root:
        return res
    q = collections.deque([root])
    ...
```

```

while q:
    level_lst = []
    for _ in range(len(q)):
        cur = q.popleft()
        level_lst.append(cur.val)
        if cur.left: q.append(cur.left)
        if cur.right: q.append(cur.right)
    res.append(max(level_lst))
return res

```

Recursive Solution

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## [116. Popular Next Right Pointers in Each Node](#)

**Idea:** 遇到每层最后一个node之前 先全都连起来 最后一个肯定指向null

Iterative Solution

```

def connect(self, root: 'Optional[Node]') -> 'Optional[Node]':
    if not root: return root
    q = collections.deque([root])
    while q:
        size = len(q)
        for i in range(size):
            cur = q.popleft()
            if cur.left: q.append(cur.left)
            if cur.right: q.append(cur.right)
            # when not reaching to the last node, connect all previous nodes
            if i < size - 1: cur.next = q[0]
        # At last, let the final node point to None
        cur.next = None
    return root

```

Recursive Solution

...

## [117. Popular Next Right Pointers in Each Node II](#)

... ..

## Idea: No difference with 116.

Iterative Solution

```
def connect(self, root: 'Node') -> 'Node':
    if not root:
        return root
    q = collections.deque([root])
    while q:
        size = len(q)
        for i in range(size):
            cur = q.popleft()
            if i < size - 1:
                cur.next = q[0]
            if cur.left:
                q.append(cur.left)
            if cur.right:
                q.append(cur.right)

        cur.next = None
    return root
```

### [104. Maximum Depth of Binary Tree](#)

**idea: Iterate through nodes in level order, everytime we finished a level, cnt++**

Iterative Solution

```
def maxDepth(self, root: Optional[TreeNode]) -> int:
    cnt = 0
    if not root:
        return cnt
    # bfs to get the number of levels in the binary tree
    q = collections.deque([root])
    while q:
        size = len(q)
        for i in range(size):
            cur = q.popleft()
            if cur.left:
                q.append(cur.left)
            if cur.right:
                q.append(cur.right)
        cnt += 1
    return cnt
```

Recursive Solution (1 line)



```
def maxDepth(self, root: Optional[TreeNode]) -> int:
    return 0 if not root else 1 + max(self.maxDepth(root.left),
self.maxDepth(root.right))
    # cnt = 0
    # if not root: return cnt
    # # bfs to get the number of levels in the binary tree
    # cnt = 1 + max(self.maxDepth(root.left), self.maxDepth(root.right))
    # return cnt
```

### [111. Minimum Depth of Binary Tree](#)

**Idea:** 递归要check special cases (一直往左下↙或者一直往右下↘), (still 102变种 记一个level变量更新层数) 用bfs遍历 当遇到第一个node没有左右child的时候就可以返回当前level数了 否则就一直bfs遍历下去

Iterative Solution

```
def minDepth(self, root: Optional[TreeNode]) -> int:
    level = 0
    if not root:
        return level
    q = collections.deque([root])
    level += 1
    while q:
        size = len(q)
        for i in range(size):
            cur = q.popleft()
            if not cur.left and not cur.right:
                return level
            if cur.left:
                q.append(cur.left)
            if cur.right:
                q.append(cur.right)
        level += 1
    return level
```

Recursive Solution

```
def minDepth(self, root: Optional[TreeNode]) -> int:
    if not root:
        return 0
    if not root.left and root.right:
        return 1 + self.minDepth(root.right)
    if not root.right and root.left:
        return 1 + self.minDepth(root.left)
    return 1 + min(self.minDepth(root.left), self.minDepth(root.right))
```

# Invert Binary Tree

## [226. Invert Binary Tree](#)

**Idea:** Iterative is using queue to reverse on every level, Recursive will be start with root and go left and right.

Iterative Solution

```
def invertTree(self, root: Optional[TreeNode]) -> Optional[TreeNode]:
    if not root:
        return root
    q = collections.deque([root])
    while q:
        for i in range(len(q)):
            cur = q.popleft()
            cur.left, cur.right = cur.right, cur.left
            if cur.left: q.append(cur.left)
            if cur.right: q.append(cur.right)
    return root
```

Recursive Solution

```
def invertTree(self, root: Optional[TreeNode]) -> Optional[TreeNode]:
    if not root:
        return root
    # directly do the swap start with root node
    root.left, root.right = root.right, root.left
    self.invertTree(root.left)
    self.invertTree(root.right)
    return root
```

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# Symmetric Tree

## [101. Symmetric Tree](#)

**Idea:** check left right with the right left and left left with right right :)

Iterative Solution

```
def isSymmetric(self, root: Optional[TreeNode]) -> bool:
    if not root:
        return True
    q = collections.deque()
```

```

q = collections.deque()
q.append(root.left)
q.append(root.right)
while q:
    leftn = q.popleft()
    rightn = q.popleft()
    if not leftn and not rightn:
        # means current is symmetric
        continue
    if not leftn or not rightn or leftn.val != rightn.val:
        # Not symmetric
        return False
    # symmetric adding
    q.append(leftn.left)
    q.append(rightn.right)
    # symmetric adding
    q.append(leftn.right)
    q.append(rightn.left)
return True

```

## Recursive Solution

```

def isSymmetric(self, root: Optional[TreeNode]) -> bool:
    if not root:
        return True
    # left is None, right, then return False
    # left, right is None, then return False
    # left is None and right is None, return True
    # left and right and left.val != right.val, return False
    # compare left.right with right.left or compare left.left with right.right
    def dfs(left, right):
        if not left and right: return False
        elif left and not right: return False
        elif not left and not right: return True
        elif left.val != right.val: return False
        outside = dfs(left.left, right.right)
        inside = dfs(left.right, right.left)
        return outside and inside
    return dfs(root.left, root.right)

```

## [222. Count Complete Tree Nodes](#)

Idea: BFS, update cnt

## Idea. DFS, update cnt

### Iterative Solution

```
def countNodes(self, root: Optional[TreeNode]) -> int:
    # use bfs and a counter to update the number of nodes
    cnt = 0
    if not root:
        return cnt
    q = collections.deque([root])
    while q:
        for _ in range(len(q)):
            cur = q.popleft()
            cnt += 1
            if cur.left:
                q.append(cur.left)
            if cur.right:
                q.append(cur.right)
    return cnt
```

### Recursive Solution

递归更简单。。跟找max path类似 别忘了count+1 因为root也算进去

```
def countNodes(self, root: Optional[TreeNode]) -> int:
    # use bfs and a counter to update the number of nodes
    cnt = 0
    if not root:
        return cnt
    return 1 + self.countNodes(root.left) + self.countNodes(root.right)
```