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1 PBType Theory

Built: 09 July 2017

Parent Theories: indexedLists, patternMatches

1.1 Datatypes

slCommand = crossLD | conductORP | moveToPB | conductPB
 | completePB | incomplete

slOutput = PlanPB | MoveToORP | ConductORP | MoveToPB
 | ConductPB | CompletePB | unAuthenticated

slState = PLAN_PB | MOVE_TO_ORP | CONDUCT_ORP | MOVE_TO_PB
 | CONDUCT_PB | COMPLETE_PB

stateRole = PlatoonLeader

1.2 Theorems

[slCommand_distinct_clauses]

⊢ crossLD ≠ conductORP ∧ crossLD ≠ moveToPB ∧
 crossLD ≠ conductPB ∧ crossLD ≠ completePB ∧
 crossLD ≠ incomplete ∧ conductORP ≠ moveToPB ∧
 conductORP ≠ conductPB ∧ conductORP ≠ completePB ∧
 conductORP ≠ incomplete ∧ moveToPB ≠ conductPB ∧
 moveToPB ≠ completePB ∧ moveToPB ≠ incomplete ∧
 conductPB ≠ completePB ∧ conductPB ≠ incomplete ∧
 completePB ≠ incomplete

[slOutput_distinct_clauses]

⊢ PlanPB ≠ MoveToORP ∧ PlanPB ≠ ConductORP ∧
 PlanPB ≠ MoveToPB ∧ PlanPB ≠ ConductPB ∧
 PlanPB ≠ CompletePB ∧ PlanPB ≠ unAuthenticated ∧
 MoveToORP ≠ ConductORP ∧ MoveToORP ≠ MoveToPB ∧
 MoveToORP ≠ ConductPB ∧ MoveToORP ≠ CompletePB ∧
 MoveToORP ≠ unAuthenticated ∧ ConductORP ≠ MoveToPB ∧
 ConductORP ≠ ConductPB ∧ ConductORP ≠ CompletePB ∧
 ConductORP ≠ unAuthenticated ∧ MoveToPB ≠ ConductPB ∧
 MoveToPB ≠ CompletePB ∧ MoveToPB ≠ unAuthenticated ∧
 ConductPB ≠ CompletePB ∧ ConductPB ≠ unAuthenticated ∧
 CompletePB ≠ unAuthenticated

[slState_distinct_clauses]

⊢ PLAN_PB ≠ MOVE_TO_ORP ∧ PLAN_PB ≠ CONDUCT_ORP ∧
 PLAN_PB ≠ MOVE_TO_PB ∧ PLAN_PB ≠ CONDUCT_PB ∧
 PLAN_PB ≠ COMPLETE_PB ∧ MOVE_TO_ORP ≠ CONDUCT_ORP ∧
 MOVE_TO_ORP ≠ MOVE_TO_PB ∧ MOVE_TO_ORP ≠ CONDUCT_PB ∧

$$\begin{aligned}
& \text{MOVE_TO_ORP} \neq \text{COMPLETE_PB} \wedge \text{CONDUCT_ORP} \neq \text{MOVE_TO_PB} \wedge \\
& \text{CONDUCT_ORP} \neq \text{CONDUCT_PB} \wedge \text{CONDUCT_ORP} \neq \text{COMPLETE_PB} \wedge \\
& \text{MOVE_TO_PB} \neq \text{CONDUCT_PB} \wedge \text{MOVE_TO_PB} \neq \text{COMPLETE_PB} \wedge \\
& \text{CONDUCT_PB} \neq \text{COMPLETE_PB}
\end{aligned}$$

2 ssmPB Theory

Built: 09 July 2017

Parent Theories: PBType, ssm11, OMNIType

2.1 Definitions

[secContext_def]

$$\begin{aligned}
& \vdash \forall cmd. \\
& \quad \text{secContext } cmd = \\
& \quad [\text{Name PlatoonLeader controls prop (SOME (SLc } cmd))]]
\end{aligned}$$

[ssmPBStateInterp_def]

$$\vdash \forall state. \text{ssmPBStateInterp } state = \text{TT}$$

2.2 Theorems

[authenticationTest_cmd_reject_lemma]

$$\vdash \forall cmd. \neg \text{authenticationTest (prop (SOME } cmd))$$

[authenticationTest_def]

$$\begin{aligned}
& \vdash (\text{authenticationTest (Name PlatoonLeader says prop } cmd) \iff \\
& \quad \text{T}) \wedge (\text{authenticationTest TT} \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest FF} \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (prop } v) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (notf } v_1) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_2 \text{ andf } v_3) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_4 \text{ orf } v_5) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_6 \text{ impf } v_7) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_8 \text{ eqf } v_9) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{10} \text{ says TT) } \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{10} \text{ says FF) } \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{133} \text{ meet } v_{134} \text{ says prop } v_{66}) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{135} \text{ quoting } v_{136} \text{ says prop } v_{66}) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{10} \text{ says notf } v_{67}) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{10} \text{ says (} v_{68} \text{ andf } v_{69}) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{10} \text{ says (} v_{70} \text{ orf } v_{71}) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{10} \text{ says (} v_{72} \text{ impf } v_{73}) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{10} \text{ says (} v_{74} \text{ eqf } v_{75}) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{10} \text{ says } v_{76} \text{ says } v_{77}) \iff \text{F}) \wedge \\
& \quad (\text{authenticationTest (} v_{10} \text{ says } v_{78} \text{ speaks_for } v_{79}) \iff \text{F}) \wedge
\end{aligned}$$

(authenticationTest (v₁₀ says v₈₀ controls v₈₁) \iff F) \wedge
 (authenticationTest (v₁₀ says reps v₈₂ v₈₃ v₈₄) \iff F) \wedge
 (authenticationTest (v₁₀ says v₈₅ domi v₈₆) \iff F) \wedge
 (authenticationTest (v₁₀ says v₈₇ eqi v₈₈) \iff F) \wedge
 (authenticationTest (v₁₀ says v₈₉ doms v₉₀) \iff F) \wedge
 (authenticationTest (v₁₀ says v₉₁ eqs v₉₂) \iff F) \wedge
 (authenticationTest (v₁₀ says v₉₃ eqn v₉₄) \iff F) \wedge
 (authenticationTest (v₁₀ says v₉₅ lte v₉₆) \iff F) \wedge
 (authenticationTest (v₁₀ says v₉₇ lt v₉₈) \iff F) \wedge
 (authenticationTest (v₁₂ speaks_for v₁₃) \iff F) \wedge
 (authenticationTest (v₁₄ controls v₁₅) \iff F) \wedge
 (authenticationTest (reps v₁₆ v₁₇ v₁₈) \iff F) \wedge
 (authenticationTest (v₁₉ domi v₂₀) \iff F) \wedge
 (authenticationTest (v₂₁ eqi v₂₂) \iff F) \wedge
 (authenticationTest (v₂₃ doms v₂₄) \iff F) \wedge
 (authenticationTest (v₂₅ eqs v₂₆) \iff F) \wedge
 (authenticationTest (v₂₇ eqn v₂₈) \iff F) \wedge
 (authenticationTest (v₂₉ lte v₃₀) \iff F) \wedge
 (authenticationTest (v₃₁ lt v₃₂) \iff F)

[authenticationTest_ind]

$\vdash \forall P.$

($\forall cmd. P$ (Name PlatoonLeader says prop cmd)) $\wedge P$ TT \wedge
 P FF $\wedge (\forall v. P$ (prop v)) $\wedge (\forall v_1. P$ (notf v₁)) \wedge
 ($\forall v_2 v_3. P$ (v₂ andf v₃)) $\wedge (\forall v_4 v_5. P$ (v₄ orf v₅)) \wedge
 ($\forall v_6 v_7. P$ (v₆ impf v₇)) $\wedge (\forall v_8 v_9. P$ (v₈ eqf v₉)) \wedge
 ($\forall v_{10}. P$ (v₁₀ says TT)) $\wedge (\forall v_{10}. P$ (v₁₀ says FF)) \wedge
 ($\forall v_{133} v_{134} v_{66}. P$ (v₁₃₃ meet v₁₃₄ says prop v₆₆)) \wedge
 ($\forall v_{135} v_{136} v_{66}. P$ (v₁₃₅ quoting v₁₃₆ says prop v₆₆)) \wedge
 ($\forall v_{10} v_{67}. P$ (v₁₀ says notf v₆₇)) \wedge
 ($\forall v_{10} v_{68} v_{69}. P$ (v₁₀ says (v₆₈ andf v₆₉))) \wedge
 ($\forall v_{10} v_{70} v_{71}. P$ (v₁₀ says (v₇₀ orf v₇₁))) \wedge
 ($\forall v_{10} v_{72} v_{73}. P$ (v₁₀ says (v₇₂ impf v₇₃))) \wedge
 ($\forall v_{10} v_{74} v_{75}. P$ (v₁₀ says (v₇₄ eqf v₇₅))) \wedge
 ($\forall v_{10} v_{76} v_{77}. P$ (v₁₀ says v₇₆ says v₇₇)) \wedge
 ($\forall v_{10} v_{78} v_{79}. P$ (v₁₀ says v₇₈ speaks_for v₇₉)) \wedge
 ($\forall v_{10} v_{80} v_{81}. P$ (v₁₀ says v₈₀ controls v₈₁)) \wedge
 ($\forall v_{10} v_{82} v_{83} v_{84}. P$ (v₁₀ says reps v₈₂ v₈₃ v₈₄)) \wedge
 ($\forall v_{10} v_{85} v_{86}. P$ (v₁₀ says v₈₅ domi v₈₆)) \wedge
 ($\forall v_{10} v_{87} v_{88}. P$ (v₁₀ says v₈₇ eqi v₈₈)) \wedge
 ($\forall v_{10} v_{89} v_{90}. P$ (v₁₀ says v₈₉ doms v₉₀)) \wedge
 ($\forall v_{10} v_{91} v_{92}. P$ (v₁₀ says v₉₁ eqs v₉₂)) \wedge
 ($\forall v_{10} v_{93} v_{94}. P$ (v₁₀ says v₉₃ eqn v₉₄)) \wedge
 ($\forall v_{10} v_{95} v_{96}. P$ (v₁₀ says v₉₅ lte v₉₆)) \wedge
 ($\forall v_{10} v_{97} v_{98}. P$ (v₁₀ says v₉₇ lt v₉₈)) \wedge
 ($\forall v_{12} v_{13}. P$ (v₁₂ speaks_for v₁₃)) \wedge
 ($\forall v_{14} v_{15}. P$ (v₁₄ controls v₁₅)) \wedge
 ($\forall v_{16} v_{17} v_{18}. P$ (reps v₁₆ v₁₇ v₁₈)) \wedge
 ($\forall v_{19} v_{20}. P$ (v₁₉ domi v₂₀)) \wedge

$$\begin{aligned}
& (\forall v_{21} v_{22}. P (v_{21} \text{ eqi } v_{22})) \wedge \\
& (\forall v_{23} v_{24}. P (v_{23} \text{ doms } v_{24})) \wedge \\
& (\forall v_{25} v_{26}. P (v_{25} \text{ eqs } v_{26})) \wedge (\forall v_{27} v_{28}. P (v_{27} \text{ eqn } v_{28})) \wedge \\
& (\forall v_{29} v_{30}. P (v_{29} \text{ lte } v_{30})) \wedge (\forall v_{31} v_{32}. P (v_{31} \text{ lt } v_{32})) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

[PBNS_def]

$$\begin{aligned}
& \vdash (\text{PBNS PLAN_PB (exec (SLc crossLD))} = \text{MOVE_TO_ORP}) \wedge \\
& (\text{PBNS PLAN_PB (exec (SLc incomplete))} = \text{PLAN_PB}) \wedge \\
& (\text{PBNS MOVE_TO_ORP (exec (SLc conductORP))} = \text{CONDUCT_ORP}) \wedge \\
& (\text{PBNS MOVE_TO_ORP (exec (SLc incomplete))} = \text{MOVE_TO_ORP}) \wedge \\
& (\text{PBNS CONDUCT_ORP (exec (SLc moveToPB))} = \text{MOVE_TO_PB}) \wedge \\
& (\text{PBNS CONDUCT_ORP (exec (SLc incomplete))} = \text{CONDUCT_ORP}) \wedge \\
& (\text{PBNS MOVE_TO_PB (exec (SLc conductPB))} = \text{CONDUCT_PB}) \wedge \\
& (\text{PBNS MOVE_TO_PB (exec (SLc incomplete))} = \text{MOVE_TO_PB}) \wedge \\
& (\text{PBNS CONDUCT_PB (exec (SLc completePB))} = \text{COMPLETE_PB}) \wedge \\
& (\text{PBNS CONDUCT_PB (exec (SLc incomplete))} = \text{CONDUCT_PB}) \wedge \\
& (\text{PBNS PLAN_PB (trap (SLc crossLD))} = \text{PLAN_PB}) \wedge \\
& (\text{PBNS PLAN_PB (trap (SLc incomplete))} = \text{PLAN_PB}) \wedge \\
& (\text{PBNS MOVE_TO_ORP (trap (SLc conductORP))} = \text{MOVE_TO_ORP}) \wedge \\
& (\text{PBNS MOVE_TO_ORP (trap (SLc incomplete))} = \text{MOVE_TO_ORP}) \wedge \\
& (\text{PBNS CONDUCT_ORP (trap (SLc moveToPB))} = \text{CONDUCT_ORP}) \wedge \\
& (\text{PBNS CONDUCT_ORP (trap (SLc incomplete))} = \text{CONDUCT_ORP}) \wedge \\
& (\text{PBNS MOVE_TO_PB (trap (SLc conductPB))} = \text{MOVE_TO_PB}) \wedge \\
& (\text{PBNS MOVE_TO_PB (trap (SLc incomplete))} = \text{MOVE_TO_PB}) \wedge \\
& (\text{PBNS CONDUCT_PB (trap (SLc completePB))} = \text{CONDUCT_PB}) \wedge \\
& (\text{PBNS CONDUCT_PB (trap (SLc incomplete))} = \text{CONDUCT_PB}) \wedge \\
& (\text{PBNS PLAN_PB (discard (SLc crossLD))} = \text{PLAN_PB}) \wedge \\
& (\text{PBNS MOVE_TO_ORP (discard (SLc conductORP))} = \text{MOVE_TO_ORP}) \wedge \\
& (\text{PBNS CONDUCT_ORP (discard (SLc moveToPB))} = \text{CONDUCT_ORP}) \wedge \\
& (\text{PBNS MOVE_TO_PB (discard (SLc conductPB))} = \text{MOVE_TO_PB}) \wedge \\
& (\text{PBNS CONDUCT_PB (discard (SLc completePB))} = \text{CONDUCT_PB})
\end{aligned}$$

[PBNS_ind]

$$\begin{aligned}
& \vdash \forall P. \\
& P \text{ PLAN_PB (exec (SLc crossLD))} \wedge \\
& P \text{ PLAN_PB (exec (SLc incomplete))} \wedge \\
& P \text{ MOVE_TO_ORP (exec (SLc conductORP))} \wedge \\
& P \text{ MOVE_TO_ORP (exec (SLc incomplete))} \wedge \\
& P \text{ CONDUCT_ORP (exec (SLc moveToPB))} \wedge \\
& P \text{ CONDUCT_ORP (exec (SLc incomplete))} \wedge \\
& P \text{ MOVE_TO_PB (exec (SLc conductPB))} \wedge \\
& P \text{ MOVE_TO_PB (exec (SLc incomplete))} \wedge \\
& P \text{ CONDUCT_PB (exec (SLc completePB))} \wedge \\
& P \text{ CONDUCT_PB (exec (SLc incomplete))} \wedge \\
& P \text{ PLAN_PB (trap (SLc crossLD))} \wedge \\
& P \text{ PLAN_PB (trap (SLc incomplete))} \wedge \\
& P \text{ MOVE_TO_ORP (trap (SLc conductORP))} \wedge \\
& P \text{ MOVE_TO_ORP (trap (SLc incomplete))} \wedge
\end{aligned}$$

P CONDUCT_ORP (trap (SLc moveToPB)) \wedge
 P CONDUCT_ORP (trap (SLc incomplete)) \wedge
 P MOVE_TO_PB (trap (SLc conductPB)) \wedge
 P MOVE_TO_PB (trap (SLc incomplete)) \wedge
 P CONDUCT_PB (trap (SLc completePB)) \wedge
 P CONDUCT_PB (trap (SLc incomplete)) \wedge
 P PLAN_PB (discard (SLc crossLD)) \wedge
 P MOVE_TO_ORP (discard (SLc conductORP)) \wedge
 P CONDUCT_ORP (discard (SLc moveToPB)) \wedge
 P MOVE_TO_PB (discard (SLc conductPB)) \wedge
 P CONDUCT_PB (discard (SLc completePB)) \wedge
 $(\forall v_8 v_6. P v_8 (\text{discard (ESCc } v_6))) \wedge$
 P MOVE_TO_ORP (discard (SLc crossLD)) \wedge
 P CONDUCT_ORP (discard (SLc crossLD)) \wedge
 P MOVE_TO_PB (discard (SLc crossLD)) \wedge
 P CONDUCT_PB (discard (SLc crossLD)) \wedge
 P COMPLETE_PB (discard (SLc crossLD)) \wedge
 P PLAN_PB (discard (SLc conductORP)) \wedge
 P CONDUCT_ORP (discard (SLc conductORP)) \wedge
 P MOVE_TO_PB (discard (SLc conductORP)) \wedge
 P CONDUCT_PB (discard (SLc conductORP)) \wedge
 P COMPLETE_PB (discard (SLc conductORP)) \wedge
 P PLAN_PB (discard (SLc moveToPB)) \wedge
 P MOVE_TO_ORP (discard (SLc moveToPB)) \wedge
 P MOVE_TO_PB (discard (SLc moveToPB)) \wedge
 P CONDUCT_PB (discard (SLc moveToPB)) \wedge
 P COMPLETE_PB (discard (SLc moveToPB)) \wedge
 P PLAN_PB (discard (SLc conductPB)) \wedge
 P MOVE_TO_ORP (discard (SLc conductPB)) \wedge
 P CONDUCT_ORP (discard (SLc conductPB)) \wedge
 P CONDUCT_PB (discard (SLc conductPB)) \wedge
 P COMPLETE_PB (discard (SLc conductPB)) \wedge
 P PLAN_PB (discard (SLc completePB)) \wedge
 P MOVE_TO_ORP (discard (SLc completePB)) \wedge
 P CONDUCT_ORP (discard (SLc completePB)) \wedge
 P MOVE_TO_PB (discard (SLc completePB)) \wedge
 P COMPLETE_PB (discard (SLc completePB)) \wedge
 $(\forall v_9. P v_9 (\text{discard (SLc incomplete)})) \wedge$
 $(\forall v_{13} v_{11}. P v_{13} (\text{trap (ESCc } v_{11}))) \wedge$
 P MOVE_TO_ORP (trap (SLc crossLD)) \wedge
 P CONDUCT_ORP (trap (SLc crossLD)) \wedge
 P MOVE_TO_PB (trap (SLc crossLD)) \wedge
 P CONDUCT_PB (trap (SLc crossLD)) \wedge
 P COMPLETE_PB (trap (SLc crossLD)) \wedge
 P PLAN_PB (trap (SLc conductORP)) \wedge
 P CONDUCT_ORP (trap (SLc conductORP)) \wedge
 P MOVE_TO_PB (trap (SLc conductORP)) \wedge
 P CONDUCT_PB (trap (SLc conductORP)) \wedge
 P COMPLETE_PB (trap (SLc conductORP)) \wedge

$$\begin{aligned}
& P \text{ PLAN_PB } (\text{trap } (\text{SLc moveToPB})) \wedge \\
& P \text{ MOVE_TO_ORP } (\text{trap } (\text{SLc moveToPB})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{trap } (\text{SLc moveToPB})) \wedge \\
& P \text{ CONDUCT_PB } (\text{trap } (\text{SLc moveToPB})) \wedge \\
& P \text{ COMPLETE_PB } (\text{trap } (\text{SLc moveToPB})) \wedge \\
& P \text{ PLAN_PB } (\text{trap } (\text{SLc conductPB})) \wedge \\
& P \text{ MOVE_TO_ORP } (\text{trap } (\text{SLc conductPB})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{trap } (\text{SLc conductPB})) \wedge \\
& P \text{ CONDUCT_PB } (\text{trap } (\text{SLc conductPB})) \wedge \\
& P \text{ COMPLETE_PB } (\text{trap } (\text{SLc conductPB})) \wedge \\
& P \text{ PLAN_PB } (\text{trap } (\text{SLc completePB})) \wedge \\
& P \text{ MOVE_TO_ORP } (\text{trap } (\text{SLc completePB})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{trap } (\text{SLc completePB})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{trap } (\text{SLc completePB})) \wedge \\
& P \text{ COMPLETE_PB } (\text{trap } (\text{SLc completePB})) \wedge \\
& P \text{ COMPLETE_PB } (\text{trap } (\text{SLc incomplete})) \wedge \\
& (\forall v_{17} v_{15}. P v_{17} (\text{exec } (\text{ESCc } v_{15}))) \wedge \\
& P \text{ MOVE_TO_ORP } (\text{exec } (\text{SLc crossLD})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{exec } (\text{SLc crossLD})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{exec } (\text{SLc crossLD})) \wedge \\
& P \text{ CONDUCT_PB } (\text{exec } (\text{SLc crossLD})) \wedge \\
& P \text{ COMPLETE_PB } (\text{exec } (\text{SLc crossLD})) \wedge \\
& P \text{ PLAN_PB } (\text{exec } (\text{SLc conductORP})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{exec } (\text{SLc conductORP})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{exec } (\text{SLc conductORP})) \wedge \\
& P \text{ CONDUCT_PB } (\text{exec } (\text{SLc conductORP})) \wedge \\
& P \text{ COMPLETE_PB } (\text{exec } (\text{SLc conductORP})) \wedge \\
& P \text{ PLAN_PB } (\text{exec } (\text{SLc moveToPB})) \wedge \\
& P \text{ MOVE_TO_ORP } (\text{exec } (\text{SLc moveToPB})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{exec } (\text{SLc moveToPB})) \wedge \\
& P \text{ CONDUCT_PB } (\text{exec } (\text{SLc moveToPB})) \wedge \\
& P \text{ COMPLETE_PB } (\text{exec } (\text{SLc moveToPB})) \wedge \\
& P \text{ PLAN_PB } (\text{exec } (\text{SLc conductPB})) \wedge \\
& P \text{ MOVE_TO_ORP } (\text{exec } (\text{SLc conductPB})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{exec } (\text{SLc conductPB})) \wedge \\
& P \text{ CONDUCT_PB } (\text{exec } (\text{SLc conductPB})) \wedge \\
& P \text{ COMPLETE_PB } (\text{exec } (\text{SLc conductPB})) \wedge \\
& P \text{ PLAN_PB } (\text{exec } (\text{SLc completePB})) \wedge \\
& P \text{ MOVE_TO_ORP } (\text{exec } (\text{SLc completePB})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{exec } (\text{SLc completePB})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{exec } (\text{SLc completePB})) \wedge \\
& P \text{ COMPLETE_PB } (\text{exec } (\text{SLc completePB})) \wedge \\
& P \text{ COMPLETE_PB } (\text{exec } (\text{SLc incomplete})) \Rightarrow \\
& \forall v v_1. P v v_1
\end{aligned}$$

[PBOut_def]

$$\begin{aligned}
& \vdash (\text{PBOut PLAN_PB } (\text{exec } (\text{SLc crossLD})) = \text{MoveToORP}) \wedge \\
& (\text{PBOut PLAN_PB } (\text{exec } (\text{SLc incomplete})) = \text{PlanPB}) \wedge \\
& (\text{PBOut MOVE_TO_ORP } (\text{exec } (\text{SLc conductORP})) = \text{ConductORP}) \wedge
\end{aligned}$$


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(PBOut MOVE_TO_ORP (exec (SLc incomplete)) = MoveToORP) ∧
(PBOut CONDUCT_ORP (exec (SLc moveToPB)) = MoveToPB) ∧
(PBOut CONDUCT_ORP (exec (SLc incomplete)) = ConductORP) ∧
(PBOut MOVE_TO_PB (exec (SLc conductPB)) = ConductPB) ∧
(PBOut MOVE_TO_PB (exec (SLc incomplete)) = MoveToPB) ∧
(PBOut CONDUCT_PB (exec (SLc completePB)) = CompletePB) ∧
(PBOut CONDUCT_PB (exec (SLc incomplete)) = ConductPB) ∧
(PBOut PLAN_PB (trap (SLc crossLD)) = PlanPB) ∧
(PBOut PLAN_PB (trap (SLc incomplete)) = PlanPB) ∧
(PBOut MOVE_TO_ORP (trap (SLc conductORP)) = MoveToORP) ∧
(PBOut MOVE_TO_ORP (trap (SLc incomplete)) = MoveToORP) ∧
(PBOut CONDUCT_ORP (trap (SLc moveToPB)) = ConductORP) ∧
(PBOut CONDUCT_ORP (trap (SLc incomplete)) = ConductORP) ∧
(PBOut MOVE_TO_PB (trap (SLc conductPB)) = MoveToPB) ∧
(PBOut MOVE_TO_PB (trap (SLc incomplete)) = MoveToPB) ∧
(PBOut CONDUCT_PB (trap (SLc completePB)) = ConductPB) ∧
(PBOut CONDUCT_PB (trap (SLc incomplete)) = ConductPB) ∧
(PBOut PLAN_PB (discard (SLc crossLD)) = unAuthenticated) ∧
(PBOut MOVE_TO_ORP (discard (SLc conductORP)) =
  unAuthenticated) ∧
(PBOut CONDUCT_ORP (discard (SLc moveToPB)) =
  unAuthenticated) ∧
(PBOut MOVE_TO_PB (discard (SLc conductPB)) =
  unAuthenticated) ∧
(PBOut CONDUCT_PB (discard (SLc completePB)) =
  unAuthenticated)

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[PBOut_ind]

⊢ ∀ P.

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  P PLAN_PB (exec (SLc crossLD)) ∧
  P PLAN_PB (exec (SLc incomplete)) ∧
  P MOVE_TO_ORP (exec (SLc conductORP)) ∧
  P MOVE_TO_ORP (exec (SLc incomplete)) ∧
  P CONDUCT_ORP (exec (SLc moveToPB)) ∧
  P CONDUCT_ORP (exec (SLc incomplete)) ∧
  P MOVE_TO_PB (exec (SLc conductPB)) ∧
  P MOVE_TO_PB (exec (SLc incomplete)) ∧
  P CONDUCT_PB (exec (SLc completePB)) ∧
  P CONDUCT_PB (exec (SLc incomplete)) ∧
  P PLAN_PB (trap (SLc crossLD)) ∧
  P PLAN_PB (trap (SLc incomplete)) ∧
  P MOVE_TO_ORP (trap (SLc conductORP)) ∧
  P MOVE_TO_ORP (trap (SLc incomplete)) ∧
  P CONDUCT_ORP (trap (SLc moveToPB)) ∧
  P CONDUCT_ORP (trap (SLc incomplete)) ∧
  P MOVE_TO_PB (trap (SLc conductPB)) ∧
  P MOVE_TO_PB (trap (SLc incomplete)) ∧
  P CONDUCT_PB (trap (SLc completePB)) ∧
  P CONDUCT_PB (trap (SLc incomplete)) ∧

```

P PLAN_PB (discard (SLc crossLD)) \wedge
 P MOVE_TO_ORP (discard (SLc conductORP)) \wedge
 P CONDUCT_ORP (discard (SLc moveToPB)) \wedge
 P MOVE_TO_PB (discard (SLc conductPB)) \wedge
 P CONDUCT_PB (discard (SLc completePB)) \wedge
 $(\forall v_8 v_6. P v_8 (\text{discard (ESCc } v_6))) \wedge$
 P MOVE_TO_ORP (discard (SLc crossLD)) \wedge
 P CONDUCT_ORP (discard (SLc crossLD)) \wedge
 P MOVE_TO_PB (discard (SLc crossLD)) \wedge
 P CONDUCT_PB (discard (SLc crossLD)) \wedge
 P COMPLETE_PB (discard (SLc crossLD)) \wedge
 P PLAN_PB (discard (SLc conductORP)) \wedge
 P CONDUCT_ORP (discard (SLc conductORP)) \wedge
 P MOVE_TO_PB (discard (SLc conductORP)) \wedge
 P CONDUCT_PB (discard (SLc conductORP)) \wedge
 P COMPLETE_PB (discard (SLc conductORP)) \wedge
 P PLAN_PB (discard (SLc moveToPB)) \wedge
 P MOVE_TO_ORP (discard (SLc moveToPB)) \wedge
 P MOVE_TO_PB (discard (SLc moveToPB)) \wedge
 P CONDUCT_PB (discard (SLc moveToPB)) \wedge
 P COMPLETE_PB (discard (SLc moveToPB)) \wedge
 P PLAN_PB (discard (SLc conductPB)) \wedge
 P MOVE_TO_ORP (discard (SLc conductPB)) \wedge
 P CONDUCT_ORP (discard (SLc conductPB)) \wedge
 P CONDUCT_PB (discard (SLc conductPB)) \wedge
 P COMPLETE_PB (discard (SLc conductPB)) \wedge
 P PLAN_PB (discard (SLc completePB)) \wedge
 P MOVE_TO_ORP (discard (SLc completePB)) \wedge
 P CONDUCT_ORP (discard (SLc completePB)) \wedge
 P MOVE_TO_PB (discard (SLc completePB)) \wedge
 P COMPLETE_PB (discard (SLc completePB)) \wedge
 $(\forall v_9. P v_9 (\text{discard (SLc incomplete)})) \wedge$
 $(\forall v_{13} v_{11}. P v_{13} (\text{trap (ESCc } v_{11}))) \wedge$
 P MOVE_TO_ORP (trap (SLc crossLD)) \wedge
 P CONDUCT_ORP (trap (SLc crossLD)) \wedge
 P MOVE_TO_PB (trap (SLc crossLD)) \wedge
 P CONDUCT_PB (trap (SLc crossLD)) \wedge
 P COMPLETE_PB (trap (SLc crossLD)) \wedge
 P PLAN_PB (trap (SLc conductORP)) \wedge
 P CONDUCT_ORP (trap (SLc conductORP)) \wedge
 P MOVE_TO_PB (trap (SLc conductORP)) \wedge
 P CONDUCT_PB (trap (SLc conductORP)) \wedge
 P COMPLETE_PB (trap (SLc conductORP)) \wedge
 P PLAN_PB (trap (SLc moveToPB)) \wedge
 P MOVE_TO_ORP (trap (SLc moveToPB)) \wedge
 P MOVE_TO_PB (trap (SLc moveToPB)) \wedge
 P CONDUCT_PB (trap (SLc moveToPB)) \wedge
 P COMPLETE_PB (trap (SLc moveToPB)) \wedge
 P PLAN_PB (trap (SLc conductPB)) \wedge

$P \text{ MOVE_TO_ORP (trap (SLc conductPB))} \wedge$
 $P \text{ CONDUCT_ORP (trap (SLc conductPB))} \wedge$
 $P \text{ CONDUCT_PB (trap (SLc conductPB))} \wedge$
 $P \text{ COMPLETE_PB (trap (SLc conductPB))} \wedge$
 $P \text{ PLAN_PB (trap (SLc completePB))} \wedge$
 $P \text{ MOVE_TO_ORP (trap (SLc completePB))} \wedge$
 $P \text{ CONDUCT_ORP (trap (SLc completePB))} \wedge$
 $P \text{ MOVE_TO_PB (trap (SLc completePB))} \wedge$
 $P \text{ COMPLETE_PB (trap (SLc completePB))} \wedge$
 $P \text{ COMPLETE_PB (trap (SLc incomplete))} \wedge$
 $(\forall v_{17} v_{15}. P v_{17} (\text{exec (ESCc } v_{15}))) \wedge$
 $P \text{ MOVE_TO_ORP (exec (SLc crossLD))} \wedge$
 $P \text{ CONDUCT_ORP (exec (SLc crossLD))} \wedge$
 $P \text{ MOVE_TO_PB (exec (SLc crossLD))} \wedge$
 $P \text{ CONDUCT_PB (exec (SLc crossLD))} \wedge$
 $P \text{ COMPLETE_PB (exec (SLc crossLD))} \wedge$
 $P \text{ PLAN_PB (exec (SLc conductORP))} \wedge$
 $P \text{ CONDUCT_ORP (exec (SLc conductORP))} \wedge$
 $P \text{ MOVE_TO_PB (exec (SLc conductORP))} \wedge$
 $P \text{ CONDUCT_PB (exec (SLc conductORP))} \wedge$
 $P \text{ COMPLETE_PB (exec (SLc conductORP))} \wedge$
 $P \text{ PLAN_PB (exec (SLc moveToPB))} \wedge$
 $P \text{ MOVE_TO_ORP (exec (SLc moveToPB))} \wedge$
 $P \text{ MOVE_TO_PB (exec (SLc moveToPB))} \wedge$
 $P \text{ CONDUCT_PB (exec (SLc moveToPB))} \wedge$
 $P \text{ COMPLETE_PB (exec (SLc moveToPB))} \wedge$
 $P \text{ PLAN_PB (exec (SLc conductPB))} \wedge$
 $P \text{ MOVE_TO_ORP (exec (SLc conductPB))} \wedge$
 $P \text{ CONDUCT_ORP (exec (SLc conductPB))} \wedge$
 $P \text{ CONDUCT_PB (exec (SLc conductPB))} \wedge$
 $P \text{ COMPLETE_PB (exec (SLc conductPB))} \wedge$
 $P \text{ PLAN_PB (exec (SLc completePB))} \wedge$
 $P \text{ MOVE_TO_ORP (exec (SLc completePB))} \wedge$
 $P \text{ CONDUCT_ORP (exec (SLc completePB))} \wedge$
 $P \text{ MOVE_TO_PB (exec (SLc completePB))} \wedge$
 $P \text{ COMPLETE_PB (exec (SLc completePB))} \wedge$
 $P \text{ COMPLETE_PB (exec (SLc incomplete))} \Rightarrow$
 $\forall v v_1. P v v_1$

[PlatoonLeader_exec_slCommand_justified_thm]

$\vdash \forall NS \text{ Out } M \text{ } O_i \text{ } O_s.$
 $\text{TR } (M, O_i, O_s) (\text{exec (SLc slCommand)})$
 $(\text{CFG authenticationTest ssmPBStateInterp}$
 $\quad (\text{secContext slCommand})$
 $\quad (\text{Name PlatoonLeader says prop (SOME (SLc slCommand))} ::$
 $\quad \quad \text{ins) } s \text{ outs})$
 $(\text{CFG authenticationTest ssmPBStateInterp}$
 $\quad (\text{secContext slCommand}) \text{ ins}$
 $\quad (NS \text{ s (exec (SLc slCommand))}))$

$$\begin{aligned}
& (Out\ s\ (exec\ (SLc\ slCommand))::outs)) \iff \\
& authenticationTest \\
& (Name\ PlatoonLeader\ says\ prop\ (SOME\ (SLc\ slCommand))) \wedge \\
& CFGInterpret\ (M, Oi, Os) \\
& (CFG\ authenticationTest\ ssmPBStateInterp \\
& (secContext\ slCommand) \\
& (Name\ PlatoonLeader\ says\ prop\ (SOME\ (SLc\ slCommand)):: \\
& \quad ins)\ s\ outs) \wedge \\
& (M, Oi, Os)\ sat\ prop\ (SOME\ (SLc\ slCommand)) \\
& [PlatoonLeader_justified_slCommand_exec_thm] \\
& \vdash \forall NS\ Out\ M\ Oi\ Os\ cmd\ slCommand\ ins\ s\ outs. \\
& authenticationTest \\
& (Name\ PlatoonLeader\ says\ prop\ (SOME\ (SLc\ slCommand))) \wedge \\
& CFGInterpret\ (M, Oi, Os) \\
& (CFG\ authenticationTest\ ssmPBStateInterp \\
& (secContext\ slCommand) \\
& (Name\ PlatoonLeader\ says\ prop\ (SOME\ (SLc\ slCommand)):: \\
& \quad ins)\ s\ outs) \Rightarrow \\
& TR\ (M, Oi, Os)\ (exec\ (SLc\ slCommand)) \\
& (CFG\ authenticationTest\ ssmPBStateInterp \\
& (secContext\ slCommand) \\
& (Name\ PlatoonLeader\ says\ prop\ (SOME\ (SLc\ slCommand)):: \\
& \quad ins)\ s\ outs) \\
& (CFG\ authenticationTest\ ssmPBStateInterp \\
& (secContext\ slCommand)\ ins \\
& (NS\ s\ (exec\ (SLc\ slCommand)))) \\
& (Out\ s\ (exec\ (SLc\ slCommand))::outs)) \\
& [PlatoonLeader_slCommand_lemma] \\
& \vdash CFGInterpret\ (M, Oi, Os) \\
& (CFG\ authenticationTest\ ssmPBStateInterp \\
& (secContext\ slCommand) \\
& (Name\ PlatoonLeader\ says\ prop\ (SOME\ (SLc\ slCommand)):: \\
& \quad ins)\ s\ outs) \Rightarrow \\
& (M, Oi, Os)\ sat\ prop\ (SOME\ (SLc\ slCommand)) \\
& [PlatoonLeader_slCommand_verified_thm] \\
& \vdash \forall NS\ Out\ M\ Oi\ Os. \\
& TR\ (M, Oi, Os)\ (exec\ (SLc\ slCommand)) \\
& (CFG\ authenticationTest\ ssmPBStateInterp \\
& (secContext\ slCommand) \\
& (Name\ PlatoonLeader\ says\ prop\ (SOME\ (SLc\ slCommand)):: \\
& \quad ins)\ s\ outs) \\
& (CFG\ authenticationTest\ ssmPBStateInterp \\
& (secContext\ slCommand)\ ins \\
& (NS\ s\ (exec\ (SLc\ slCommand)))) \\
& (Out\ s\ (exec\ (SLc\ slCommand))::outs)) \Rightarrow \\
& (M, Oi, Os)\ sat\ prop\ (SOME\ (SLc\ slCommand))
\end{aligned}$$

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