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1 OMNITYPE Theory

Built: 02 July 2017

Parent Theories: indexedLists, patternMatches

1.1 Datatypes

```

command = ESCc escCommand | SLc 'slCommand

escCommand = returnToBase | changeMission | resupply
              | reactToContact

escOutput = ReturnToBase | ChangeMission | Resupply
            | ReactToContact

escState = RTB | CM | RESUPPLY | RTC

output = ESCo escOutput | SLo 'slOutput

principal = SR 'stateRole

state = ESCs escState | SLs 'slState

```

1.2 Theorems

[command_distinct_clauses]

$$\vdash \forall a' a. \text{ESCc } a \neq \text{SLc } a'$$

[command_one_one]

$$\vdash (\forall a a'. (\text{ESCc } a = \text{ESCc } a') \iff (a = a')) \wedge \\ \forall a a'. (\text{SLc } a = \text{SLc } a') \iff (a = a')$$

[escCommand_distinct_clauses]

$$\vdash \text{returnToBase} \neq \text{changeMission} \wedge \text{returnToBase} \neq \text{resupply} \wedge \\ \text{returnToBase} \neq \text{reactToContact} \wedge \text{changeMission} \neq \text{resupply} \wedge \\ \text{changeMission} \neq \text{reactToContact} \wedge \text{resupply} \neq \text{reactToContact}$$

[escOutput_distinct_clauses]

$$\vdash \text{ReturnToBase} \neq \text{ChangeMission} \wedge \text{ReturnToBase} \neq \text{Resupply} \wedge \\ \text{ReturnToBase} \neq \text{ReactToContact} \wedge \text{ChangeMission} \neq \text{Resupply} \wedge \\ \text{ChangeMission} \neq \text{ReactToContact} \wedge \text{Resupply} \neq \text{ReactToContact}$$

[escState_distinct_clauses]

$$\vdash \text{RTB} \neq \text{CM} \wedge \text{RTB} \neq \text{RESUPPLY} \wedge \text{RTB} \neq \text{RTC} \wedge \text{CM} \neq \text{RESUPPLY} \wedge \\ \text{CM} \neq \text{RTC} \wedge \text{RESUPPLY} \neq \text{RTC}$$

[output_distinct_clauses]

$\vdash \forall a' a. \text{ESCo } a \neq \text{SLo } a'$

[output_one_one]

$\vdash (\forall a a'. (\text{ESCo } a = \text{ESCo } a') \iff (a = a')) \wedge$
 $\quad \forall a a'. (\text{SLo } a = \text{SLo } a') \iff (a = a')$

[principal_one_one]

$\vdash \forall a a'. (\text{SR } a = \text{SR } a') \iff (a = a')$

[state_distinct_clauses]

$\vdash \forall a' a. \text{ESCs } a \neq \text{SLs } a'$

[state_one_one]

$\vdash (\forall a a'. (\text{ESCs } a = \text{ESCs } a') \iff (a = a')) \wedge$
 $\quad \forall a a'. (\text{SLs } a = \text{SLs } a') \iff (a = a')$

2 ssmPB Theory

Built: 02 July 2017

Parent Theories: PBType, ssm11, OMNIType

2.1 Definitions

[secContext_def]

$\vdash \forall slCommand.$
 $\quad \text{secContext } slCommand =$
 $\quad [\text{Name PlatoonLeader controls prop (SOME (SLc } slCommand))]$

[ssmPBStateInterp_def]

$\vdash \forall state. \text{ssmPBStateInterp } state = \text{TT}$

2.2 Theorems

[authenticationTest_cmd_reject_lemma]

$\vdash \forall cmd. \neg \text{authenticationTest (prop (SOME } cmd))$

[authenticationTest_def]

$\vdash (\text{authenticationTest (Name PlatoonLeader says prop } cmd) \iff$
 $\quad \text{T}) \wedge (\text{authenticationTest TT} \iff \text{F}) \wedge$
 $\quad (\text{authenticationTest FF} \iff \text{F}) \wedge$
 $\quad (\text{authenticationTest (prop } v) \iff \text{F}) \wedge$
 $\quad (\text{authenticationTest (notf } v_1) \iff \text{F}) \wedge$
 $\quad (\text{authenticationTest } (v_2 \text{ andf } v_3) \iff \text{F}) \wedge$
 $\quad (\text{authenticationTest } (v_4 \text{ orf } v_5) \iff \text{F}) \wedge$

```

(authenticationTest (v6 impf v7)  $\iff$  F)  $\wedge$ 
(authenticationTest (v8 eqf v9)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says TT)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says FF)  $\iff$  F)  $\wedge$ 
(authenticationTest (v133 meet v134 says prop v66)  $\iff$  F)  $\wedge$ 
(authenticationTest (v135 quoting v136 says prop v66)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says notf v67)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says (v68 andf v69))  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says (v70 orf v71))  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says (v72 impf v73))  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says (v74 eqf v75))  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says v76 says v77)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says v78 speaks_for v79)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says v80 controls v81)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says reps v82 v83 v84)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says v85 domi v86)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says v87 eqi v88)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says v89 doms v90)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says v91 eqs v92)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says v93 eqn v94)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says v95 lte v96)  $\iff$  F)  $\wedge$ 
(authenticationTest (v10 says v97 lt v98)  $\iff$  F)  $\wedge$ 
(authenticationTest (v12 speaks_for v13)  $\iff$  F)  $\wedge$ 
(authenticationTest (v14 controls v15)  $\iff$  F)  $\wedge$ 
(authenticationTest (reps v16 v17 v18)  $\iff$  F)  $\wedge$ 
(authenticationTest (v19 domi v20)  $\iff$  F)  $\wedge$ 
(authenticationTest (v21 eqi v22)  $\iff$  F)  $\wedge$ 
(authenticationTest (v23 doms v24)  $\iff$  F)  $\wedge$ 
(authenticationTest (v25 eqs v26)  $\iff$  F)  $\wedge$ 
(authenticationTest (v27 eqn v28)  $\iff$  F)  $\wedge$ 
(authenticationTest (v29 lte v30)  $\iff$  F)  $\wedge$ 
(authenticationTest (v31 lt v32)  $\iff$  F)

```

[authenticationTest_ind]

$\vdash \forall P.$

```

(∀ cmd. P (Name PlatoonLeader says prop cmd))  $\wedge$  P TT  $\wedge$ 
P FF  $\wedge$  (∀ v. P (prop v))  $\wedge$  (∀ v1. P (notf v1))  $\wedge$ 
(∀ v2 v3. P (v2 andf v3))  $\wedge$  (∀ v4 v5. P (v4 orf v5))  $\wedge$ 
(∀ v6 v7. P (v6 impf v7))  $\wedge$  (∀ v8 v9. P (v8 eqf v9))  $\wedge$ 
(∀ v10. P (v10 says TT))  $\wedge$  (∀ v10. P (v10 says FF))  $\wedge$ 
(∀ v133 v134 v66. P (v133 meet v134 says prop v66))  $\wedge$ 
(∀ v135 v136 v66. P (v135 quoting v136 says prop v66))  $\wedge$ 
(∀ v10 v67. P (v10 says notf v67))  $\wedge$ 
(∀ v10 v68 v69. P (v10 says (v68 andf v69)))  $\wedge$ 
(∀ v10 v70 v71. P (v10 says (v70 orf v71)))  $\wedge$ 
(∀ v10 v72 v73. P (v10 says (v72 impf v73)))  $\wedge$ 
(∀ v10 v74 v75. P (v10 says (v74 eqf v75)))  $\wedge$ 
(∀ v10 v76 v77. P (v10 says v76 says v77))  $\wedge$ 
(∀ v10 v78 v79. P (v10 says v78 speaks_for v79))  $\wedge$ 

```

$$\begin{aligned}
& (\forall v_{10} v_{80} v_{81}. P (v_{10} \text{ says } v_{80} \text{ controls } v_{81})) \wedge \\
& (\forall v_{10} v_{82} v_{83} v_{84}. P (v_{10} \text{ says reps } v_{82} v_{83} v_{84})) \wedge \\
& (\forall v_{10} v_{85} v_{86}. P (v_{10} \text{ says } v_{85} \text{ domi } v_{86})) \wedge \\
& (\forall v_{10} v_{87} v_{88}. P (v_{10} \text{ says } v_{87} \text{ eqi } v_{88})) \wedge \\
& (\forall v_{10} v_{89} v_{90}. P (v_{10} \text{ says } v_{89} \text{ doms } v_{90})) \wedge \\
& (\forall v_{10} v_{91} v_{92}. P (v_{10} \text{ says } v_{91} \text{ eqs } v_{92})) \wedge \\
& (\forall v_{10} v_{93} v_{94}. P (v_{10} \text{ says } v_{93} \text{ eqn } v_{94})) \wedge \\
& (\forall v_{10} v_{95} v_{96}. P (v_{10} \text{ says } v_{95} \text{ lte } v_{96})) \wedge \\
& (\forall v_{10} v_{97} v_{98}. P (v_{10} \text{ says } v_{97} \text{ lt } v_{98})) \wedge \\
& (\forall v_{12} v_{13}. P (v_{12} \text{ speaks_for } v_{13})) \wedge \\
& (\forall v_{14} v_{15}. P (v_{14} \text{ controls } v_{15})) \wedge \\
& (\forall v_{16} v_{17} v_{18}. P (\text{reps } v_{16} v_{17} v_{18})) \wedge \\
& (\forall v_{19} v_{20}. P (v_{19} \text{ domi } v_{20})) \wedge \\
& (\forall v_{21} v_{22}. P (v_{21} \text{ eqi } v_{22})) \wedge \\
& (\forall v_{23} v_{24}. P (v_{23} \text{ doms } v_{24})) \wedge \\
& (\forall v_{25} v_{26}. P (v_{25} \text{ eqs } v_{26})) \wedge (\forall v_{27} v_{28}. P (v_{27} \text{ eqn } v_{28})) \wedge \\
& (\forall v_{29} v_{30}. P (v_{29} \text{ lte } v_{30})) \wedge (\forall v_{31} v_{32}. P (v_{31} \text{ lt } v_{32})) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

[authenticationTest_TT_reject_lemma]

$\vdash \neg \text{authenticationTest TT}$

[PBNS_def]

$$\begin{aligned}
& \vdash (\text{PBNS PLAN_PB (exec (SLc crossLD))} = \text{MOVE_TO_ORP}) \wedge \\
& (\text{PBNS PLAN_PB (exec (SLc incomplete))} = \text{PLAN_PB}) \wedge \\
& (\text{PBNS MOVE_TO_ORP (exec (SLc conductorORP))} = \text{CONDUCT_ORP}) \wedge \\
& (\text{PBNS MOVE_TO_ORP (exec (SLc incomplete))} = \text{MOVE_TO_ORP}) \wedge \\
& (\text{PBNS CONDUCT_ORP (exec (SLc moveToPB))} = \text{MOVE_TO_PB}) \wedge \\
& (\text{PBNS CONDUCT_ORP (exec (SLc incomplete))} = \text{CONDUCT_ORP}) \wedge \\
& (\text{PBNS MOVE_TO_PB (exec (SLc conductPB))} = \text{CONDUCT_PB}) \wedge \\
& (\text{PBNS MOVE_TO_PB (exec (SLc incomplete))} = \text{MOVE_TO_PB}) \wedge \\
& (\text{PBNS CONDUCT_PB (exec (SLc completePB))} = \text{COMPLETE_PB}) \wedge \\
& (\text{PBNS CONDUCT_PB (exec (SLc incomplete))} = \text{CONDUCT_PB}) \wedge \\
& (\text{PBNS PLAN_PB (trap (SLc crossLD))} = \text{PLAN_PB}) \wedge \\
& (\text{PBNS PLAN_PB (trap (SLc incomplete))} = \text{PLAN_PB}) \wedge \\
& (\text{PBNS MOVE_TO_ORP (trap (SLc moveToORP))} = \text{MOVE_TO_ORP}) \wedge \\
& (\text{PBNS CONDUCT_ORP (trap (SLc moveToPB))} = \text{CONDUCT_ORP}) \wedge \\
& (\text{PBNS CONDUCT_ORP (trap (SLc incomplete))} = \text{CONDUCT_ORP}) \wedge \\
& (\text{PBNS MOVE_TO_PB (trap (SLc conductPB))} = \text{MOVE_TO_PB}) \wedge \\
& (\text{PBNS MOVE_TO_PB (trap (SLc incomplete))} = \text{MOVE_TO_PB}) \wedge \\
& (\text{PBNS CONDUCT_PB (trap (SLc completePB))} = \text{CONDUCT_PB}) \wedge \\
& (\text{PBNS CONDUCT_PB (trap (SLc incomplete))} = \text{CONDUCT_PB}) \wedge \\
& (\text{PBNS PLAN_PB (discard (SLc crossLD))} = \text{PLAN_PB}) \wedge \\
& (\text{PBNS MOVE_TO_ORP (discard (SLc moveToORP))} = \text{MOVE_TO_ORP}) \wedge \\
& (\text{PBNS CONDUCT_ORP (discard (SLc moveToPB))} = \text{CONDUCT_ORP}) \wedge \\
& (\text{PBNS MOVE_TO_PB (discard (SLc conductPB))} = \text{MOVE_TO_PB}) \wedge \\
& (\text{PBNS CONDUCT_PB (discard (SLc completePB))} = \text{CONDUCT_PB})
\end{aligned}$$

[PBNS_ind]

 $\vdash \forall P.$

$$\begin{aligned}
& P \text{ PLAN_PB (exec (SLc crossLD)) } \wedge \\
& P \text{ PLAN_PB (exec (SLc incomplete)) } \wedge \\
& P \text{ MOVE_TO_ORP (exec (SLc conductORP)) } \wedge \\
& P \text{ MOVE_TO_ORP (exec (SLc incomplete)) } \wedge \\
& P \text{ CONDUCT_ORP (exec (SLc moveToPB)) } \wedge \\
& P \text{ CONDUCT_ORP (exec (SLc incomplete)) } \wedge \\
& P \text{ MOVE_TO_PB (exec (SLc conductPB)) } \wedge \\
& P \text{ MOVE_TO_PB (exec (SLc incomplete)) } \wedge \\
& P \text{ CONDUCT_PB (exec (SLc completePB)) } \wedge \\
& P \text{ CONDUCT_PB (exec (SLc incomplete)) } \wedge \\
& P \text{ PLAN_PB (trap (SLc crossLD)) } \wedge \\
& P \text{ PLAN_PB (trap (SLc incomplete)) } \wedge \\
& (\forall \text{ moveToORP}. P \text{ MOVE_TO_ORP (trap (SLc moveToORP))}) \wedge \\
& P \text{ CONDUCT_ORP (trap (SLc moveToPB)) } \wedge \\
& P \text{ CONDUCT_ORP (trap (SLc incomplete)) } \wedge \\
& P \text{ MOVE_TO_PB (trap (SLc conductPB)) } \wedge \\
& P \text{ MOVE_TO_PB (trap (SLc incomplete)) } \wedge \\
& P \text{ CONDUCT_PB (trap (SLc completePB)) } \wedge \\
& P \text{ CONDUCT_PB (trap (SLc incomplete)) } \wedge \\
& P \text{ PLAN_PB (discard (SLc crossLD)) } \wedge \\
& (\forall \text{ moveToORP}. P \text{ MOVE_TO_ORP (discard (SLc moveToORP))}) \wedge \\
& P \text{ CONDUCT_ORP (discard (SLc moveToPB)) } \wedge \\
& P \text{ MOVE_TO_PB (discard (SLc conductPB)) } \wedge \\
& P \text{ CONDUCT_PB (discard (SLc completePB)) } \wedge \\
& (\forall v_8 \ v_6. P \ v_8 \text{ (discard (ESCc } v_6))}) \wedge \\
& P \text{ PLAN_PB (discard (SLc conductORP)) } \wedge \\
& P \text{ PLAN_PB (discard (SLc moveToPB)) } \wedge \\
& P \text{ PLAN_PB (discard (SLc conductPB)) } \wedge \\
& P \text{ PLAN_PB (discard (SLc completePB)) } \wedge \\
& P \text{ PLAN_PB (discard (SLc incomplete)) } \wedge \\
& P \text{ CONDUCT_ORP (discard (SLc crossLD)) } \wedge \\
& P \text{ CONDUCT_ORP (discard (SLc conductORP)) } \wedge \\
& P \text{ CONDUCT_ORP (discard (SLc conductPB)) } \wedge \\
& P \text{ CONDUCT_ORP (discard (SLc completePB)) } \wedge \\
& P \text{ CONDUCT_ORP (discard (SLc incomplete)) } \wedge \\
& P \text{ MOVE_TO_PB (discard (SLc crossLD)) } \wedge \\
& P \text{ MOVE_TO_PB (discard (SLc conductORP)) } \wedge \\
& P \text{ MOVE_TO_PB (discard (SLc moveToPB)) } \wedge \\
& P \text{ MOVE_TO_PB (discard (SLc completePB)) } \wedge \\
& P \text{ MOVE_TO_PB (discard (SLc incomplete)) } \wedge \\
& P \text{ CONDUCT_PB (discard (SLc crossLD)) } \wedge \\
& P \text{ CONDUCT_PB (discard (SLc conductORP)) } \wedge \\
& P \text{ CONDUCT_PB (discard (SLc moveToPB)) } \wedge \\
& P \text{ CONDUCT_PB (discard (SLc conductPB)) } \wedge \\
& P \text{ CONDUCT_PB (discard (SLc incomplete)) } \wedge \\
& (\forall v_9. P \text{ COMPLETE_PB (discard (SLc } v_9))}) \wedge \\
& (\forall v_{13} \ v_{11}. P \ v_{13} \text{ (trap (ESCc } v_{11}))}) \wedge
\end{aligned}$$

$P \text{ PLAN_PB (trap (SLc conductORP)) } \wedge$
 $P \text{ PLAN_PB (trap (SLc moveToPB)) } \wedge$
 $P \text{ PLAN_PB (trap (SLc conductPB)) } \wedge$
 $P \text{ PLAN_PB (trap (SLc completePB)) } \wedge$
 $P \text{ CONDUCT_ORP (trap (SLc crossLD)) } \wedge$
 $P \text{ CONDUCT_ORP (trap (SLc conductORP)) } \wedge$
 $P \text{ CONDUCT_ORP (trap (SLc conductPB)) } \wedge$
 $P \text{ CONDUCT_ORP (trap (SLc completePB)) } \wedge$
 $P \text{ MOVE_TO_PB (trap (SLc crossLD)) } \wedge$
 $P \text{ MOVE_TO_PB (trap (SLc conductORP)) } \wedge$
 $P \text{ MOVE_TO_PB (trap (SLc moveToPB)) } \wedge$
 $P \text{ MOVE_TO_PB (trap (SLc completePB)) } \wedge$
 $P \text{ CONDUCT_PB (trap (SLc crossLD)) } \wedge$
 $P \text{ CONDUCT_PB (trap (SLc conductORP)) } \wedge$
 $P \text{ CONDUCT_PB (trap (SLc moveToPB)) } \wedge$
 $P \text{ CONDUCT_PB (trap (SLc conductPB)) } \wedge$
 $(\forall v_{14}. P \text{ COMPLETE_PB (trap (SLc } v_{14}))) \wedge$
 $(\forall v_{18} v_{16}. P \text{ } v_{18} \text{ (exec (ESCc } v_{16}))) \wedge$
 $P \text{ MOVE_TO_ORP (exec (SLc crossLD)) } \wedge$
 $P \text{ CONDUCT_ORP (exec (SLc crossLD)) } \wedge$
 $P \text{ MOVE_TO_PB (exec (SLc crossLD)) } \wedge$
 $P \text{ CONDUCT_PB (exec (SLc crossLD)) } \wedge$
 $P \text{ COMPLETE_PB (exec (SLc crossLD)) } \wedge$
 $P \text{ PLAN_PB (exec (SLc conductORP)) } \wedge$
 $P \text{ CONDUCT_ORP (exec (SLc conductORP)) } \wedge$
 $P \text{ MOVE_TO_PB (exec (SLc conductORP)) } \wedge$
 $P \text{ CONDUCT_PB (exec (SLc conductORP)) } \wedge$
 $P \text{ COMPLETE_PB (exec (SLc conductORP)) } \wedge$
 $P \text{ PLAN_PB (exec (SLc moveToPB)) } \wedge$
 $P \text{ MOVE_TO_ORP (exec (SLc moveToPB)) } \wedge$
 $P \text{ MOVE_TO_PB (exec (SLc moveToPB)) } \wedge$
 $P \text{ CONDUCT_PB (exec (SLc moveToPB)) } \wedge$
 $P \text{ COMPLETE_PB (exec (SLc moveToPB)) } \wedge$
 $P \text{ PLAN_PB (exec (SLc conductPB)) } \wedge$
 $P \text{ MOVE_TO_ORP (exec (SLc conductPB)) } \wedge$
 $P \text{ CONDUCT_ORP (exec (SLc conductPB)) } \wedge$
 $P \text{ CONDUCT_PB (exec (SLc conductPB)) } \wedge$
 $P \text{ COMPLETE_PB (exec (SLc conductPB)) } \wedge$
 $P \text{ PLAN_PB (exec (SLc completePB)) } \wedge$
 $P \text{ MOVE_TO_ORP (exec (SLc completePB)) } \wedge$
 $P \text{ CONDUCT_ORP (exec (SLc completePB)) } \wedge$
 $P \text{ MOVE_TO_PB (exec (SLc completePB)) } \wedge$
 $P \text{ COMPLETE_PB (exec (SLc completePB)) } \wedge$
 $P \text{ COMPLETE_PB (exec (SLc incomplete)) } \Rightarrow$
 $\forall v \ v_1. P \ v \ v_1$

[PBOut_def]

$\vdash (\text{PBOut PLAN_PB (exec (SLc crossLD))} = \text{MoveToORP}) \wedge$
 $(\text{PBOut PLAN_PB (exec (SLc incomplete))} = \text{PlanPB}) \wedge$


```

(PBOut MOVE_TO_ORP (exec (SLc conductORP)) = ConductORP) ∧
(PBOut MOVE_TO_ORP (exec (SLc incomplete)) = MoveToORP) ∧
(PBOut CONDUCT_ORP (exec (SLc moveToPB)) = MoveToPB) ∧
(PBOut CONDUCT_ORP (exec (SLc incomplete)) = ConductORP) ∧
(PBOut MOVE_TO_PB (exec (SLc conductPB)) = ConductPB) ∧
(PBOut MOVE_TO_PB (exec (SLc incomplete)) = MoveToPB) ∧
(PBOut CONDUCT_PB (exec (SLc completePB)) = CompletePB) ∧
(PBOut CONDUCT_PB (exec (SLc incomplete)) = ConductPB) ∧
(PBOut PLAN_PB (trap (SLc crossLD)) = PlanPB) ∧
(PBOut PLAN_PB (trap (SLc incomplete)) = PlanPB) ∧
(PBOut MOVE_TO_ORP (trap (SLc moveToORP)) = MoveToORP) ∧
(PBOut CONDUCT_ORP (trap (SLc moveToPB)) = ConductORP) ∧
(PBOut CONDUCT_ORP (trap (SLc incomplete)) = ConductORP) ∧
(PBOut MOVE_TO_PB (trap (SLc conductPB)) = MoveToPB) ∧
(PBOut MOVE_TO_PB (trap (SLc incomplete)) = MoveToPB) ∧
(PBOut CONDUCT_PB (trap (SLc completePB)) = ConductPB) ∧
(PBOut CONDUCT_PB (trap (SLc incomplete)) = ConductPB) ∧
(PBOut PLAN_PB (discard (SLc crossLD)) = unAuthenticated) ∧
(PBOut MOVE_TO_ORP (discard (SLc moveToORP)) =
  unAuthenticated) ∧
(PBOut CONDUCT_ORP (discard (SLc moveToPB)) =
  unAuthenticated) ∧
(PBOut MOVE_TO_PB (discard (SLc conductPB)) =
  unAuthenticated) ∧
(PBOut CONDUCT_PB (discard (SLc completePB)) =
  unAuthenticated)

```

[PBOut_ind]

⊢ ∀ P.

```

  P PLAN_PB (exec (SLc crossLD)) ∧
  P PLAN_PB (exec (SLc incomplete)) ∧
  P MOVE_TO_ORP (exec (SLc conductORP)) ∧
  P MOVE_TO_ORP (exec (SLc incomplete)) ∧
  P CONDUCT_ORP (exec (SLc moveToPB)) ∧
  P CONDUCT_ORP (exec (SLc incomplete)) ∧
  P MOVE_TO_PB (exec (SLc conductPB)) ∧
  P MOVE_TO_PB (exec (SLc incomplete)) ∧
  P CONDUCT_PB (exec (SLc completePB)) ∧
  P CONDUCT_PB (exec (SLc incomplete)) ∧
  P PLAN_PB (trap (SLc crossLD)) ∧
  P PLAN_PB (trap (SLc incomplete)) ∧
  (∀ moveToORP. P MOVE_TO_ORP (trap (SLc moveToORP))) ∧
  P CONDUCT_ORP (trap (SLc moveToPB)) ∧
  P CONDUCT_ORP (trap (SLc incomplete)) ∧
  P MOVE_TO_PB (trap (SLc conductPB)) ∧
  P MOVE_TO_PB (trap (SLc incomplete)) ∧
  P CONDUCT_PB (trap (SLc completePB)) ∧
  P CONDUCT_PB (trap (SLc incomplete)) ∧
  P PLAN_PB (discard (SLc crossLD)) ∧

```

$$\begin{aligned}
& (\forall \text{moveToORP}. P \text{ MOVE_TO_ORP } (\text{discard } (\text{SLc } \text{moveToORP}))) \wedge \\
& P \text{ CONDUCT_ORP } (\text{discard } (\text{SLc } \text{moveToPB})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{discard } (\text{SLc } \text{conductPB})) \wedge \\
& P \text{ CONDUCT_PB } (\text{discard } (\text{SLc } \text{completePB})) \wedge \\
& (\forall v_8 \ v_6. P \ v_8 \ (\text{discard } (\text{ESCc } v_6))) \wedge \\
& P \text{ PLAN_PB } (\text{discard } (\text{SLc } \text{conductORP})) \wedge \\
& P \text{ PLAN_PB } (\text{discard } (\text{SLc } \text{moveToPB})) \wedge \\
& P \text{ PLAN_PB } (\text{discard } (\text{SLc } \text{conductPB})) \wedge \\
& P \text{ PLAN_PB } (\text{discard } (\text{SLc } \text{completePB})) \wedge \\
& P \text{ PLAN_PB } (\text{discard } (\text{SLc } \text{incomplete})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{discard } (\text{SLc } \text{crossLD})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{discard } (\text{SLc } \text{conductORP})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{discard } (\text{SLc } \text{conductPB})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{discard } (\text{SLc } \text{completePB})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{discard } (\text{SLc } \text{incomplete})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{discard } (\text{SLc } \text{crossLD})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{discard } (\text{SLc } \text{conductORP})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{discard } (\text{SLc } \text{moveToPB})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{discard } (\text{SLc } \text{completePB})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{discard } (\text{SLc } \text{incomplete})) \wedge \\
& P \text{ CONDUCT_PB } (\text{discard } (\text{SLc } \text{crossLD})) \wedge \\
& P \text{ CONDUCT_PB } (\text{discard } (\text{SLc } \text{conductORP})) \wedge \\
& P \text{ CONDUCT_PB } (\text{discard } (\text{SLc } \text{moveToPB})) \wedge \\
& P \text{ CONDUCT_PB } (\text{discard } (\text{SLc } \text{conductPB})) \wedge \\
& P \text{ CONDUCT_PB } (\text{discard } (\text{SLc } \text{incomplete})) \wedge \\
& (\forall v_9. P \text{ COMPLETE_PB } (\text{discard } (\text{SLc } v_9))) \wedge \\
& (\forall v_{13} \ v_{11}. P \ v_{13} \ (\text{trap } (\text{ESCc } v_{11}))) \wedge \\
& P \text{ PLAN_PB } (\text{trap } (\text{SLc } \text{conductORP})) \wedge \\
& P \text{ PLAN_PB } (\text{trap } (\text{SLc } \text{moveToPB})) \wedge \\
& P \text{ PLAN_PB } (\text{trap } (\text{SLc } \text{conductPB})) \wedge \\
& P \text{ PLAN_PB } (\text{trap } (\text{SLc } \text{completePB})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{trap } (\text{SLc } \text{crossLD})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{trap } (\text{SLc } \text{conductORP})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{trap } (\text{SLc } \text{conductPB})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{trap } (\text{SLc } \text{completePB})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{trap } (\text{SLc } \text{crossLD})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{trap } (\text{SLc } \text{conductORP})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{trap } (\text{SLc } \text{moveToPB})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{trap } (\text{SLc } \text{completePB})) \wedge \\
& P \text{ CONDUCT_PB } (\text{trap } (\text{SLc } \text{crossLD})) \wedge \\
& P \text{ CONDUCT_PB } (\text{trap } (\text{SLc } \text{conductORP})) \wedge \\
& P \text{ CONDUCT_PB } (\text{trap } (\text{SLc } \text{moveToPB})) \wedge \\
& P \text{ CONDUCT_PB } (\text{trap } (\text{SLc } \text{conductPB})) \wedge \\
& (\forall v_{14}. P \text{ COMPLETE_PB } (\text{trap } (\text{SLc } v_{14}))) \wedge \\
& (\forall v_{18} \ v_{16}. P \ v_{18} \ (\text{exec } (\text{ESCc } v_{16}))) \wedge \\
& P \text{ MOVE_TO_ORP } (\text{exec } (\text{SLc } \text{crossLD})) \wedge \\
& P \text{ CONDUCT_ORP } (\text{exec } (\text{SLc } \text{crossLD})) \wedge \\
& P \text{ MOVE_TO_PB } (\text{exec } (\text{SLc } \text{crossLD})) \wedge \\
& P \text{ CONDUCT_PB } (\text{exec } (\text{SLc } \text{crossLD})) \wedge
\end{aligned}$$

```

P COMPLETE_PB (exec (SLc crossLD)) ∧
P PLAN_PB (exec (SLc conductORP)) ∧
P CONDUCT_ORP (exec (SLc conductORP)) ∧
P MOVE_TO_PB (exec (SLc conductORP)) ∧
P CONDUCT_PB (exec (SLc conductORP)) ∧
P COMPLETE_PB (exec (SLc conductORP)) ∧
P PLAN_PB (exec (SLc moveToPB)) ∧
P MOVE_TO_ORP (exec (SLc moveToPB)) ∧
P MOVE_TO_PB (exec (SLc moveToPB)) ∧
P CONDUCT_PB (exec (SLc moveToPB)) ∧
P COMPLETE_PB (exec (SLc moveToPB)) ∧
P PLAN_PB (exec (SLc conductPB)) ∧
P MOVE_TO_ORP (exec (SLc conductPB)) ∧
P CONDUCT_ORP (exec (SLc conductPB)) ∧
P CONDUCT_PB (exec (SLc conductPB)) ∧
P COMPLETE_PB (exec (SLc conductPB)) ∧
P PLAN_PB (exec (SLc completePB)) ∧
P MOVE_TO_ORP (exec (SLc completePB)) ∧
P CONDUCT_ORP (exec (SLc completePB)) ∧
P MOVE_TO_PB (exec (SLc completePB)) ∧
P COMPLETE_PB (exec (SLc completePB)) ∧
P COMPLETE_PB (exec (SLc incomplete)) ⇒
∀ v v1. P v v1

```

3 PBType Theory

Built: 02 July 2017

Parent Theories: indexedLists, patternMatches

3.1 Datatypes

```

slCommand = crossLD | conductORP | moveToPB | conductPB
           | completePB | incomplete

```

```

slOutput = PlanPB | MoveToORP | ConductORP | MoveToPB
          | ConductPB | CompletePB | unAuthenticated

```

```

slState = PLAN_PB | MOVE_TO_ORP | CONDUCT_ORP | MOVE_TO_PB
         | CONDUCT_PB | COMPLETE_PB

```

```

stateRole = PlatoonLeader

```

3.2 Theorems

[slCommand_distinct_clauses]

```

⊢ crossLD ≠ conductORP ∧ crossLD ≠ moveToPB ∧
  crossLD ≠ conductPB ∧ crossLD ≠ completePB ∧

```

$$\begin{aligned}
& \text{crossLD} \neq \text{incomplete} \wedge \text{conductORP} \neq \text{moveToPB} \wedge \\
& \text{conductORP} \neq \text{conductPB} \wedge \text{conductORP} \neq \text{completePB} \wedge \\
& \text{conductORP} \neq \text{incomplete} \wedge \text{moveToPB} \neq \text{conductPB} \wedge \\
& \text{moveToPB} \neq \text{completePB} \wedge \text{moveToPB} \neq \text{incomplete} \wedge \\
& \text{conductPB} \neq \text{completePB} \wedge \text{conductPB} \neq \text{incomplete} \wedge \\
& \text{completePB} \neq \text{incomplete}
\end{aligned}$$

[slOutput_distinct_clauses]

$$\begin{aligned}
& \vdash \text{PlanPB} \neq \text{MoveToORP} \wedge \text{PlanPB} \neq \text{ConductORP} \wedge \\
& \text{PlanPB} \neq \text{MoveToPB} \wedge \text{PlanPB} \neq \text{ConductPB} \wedge \\
& \text{PlanPB} \neq \text{CompletePB} \wedge \text{PlanPB} \neq \text{unAuthenticated} \wedge \\
& \text{MoveToORP} \neq \text{ConductORP} \wedge \text{MoveToORP} \neq \text{MoveToPB} \wedge \\
& \text{MoveToORP} \neq \text{ConductPB} \wedge \text{MoveToORP} \neq \text{CompletePB} \wedge \\
& \text{MoveToORP} \neq \text{unAuthenticated} \wedge \text{ConductORP} \neq \text{MoveToPB} \wedge \\
& \text{ConductORP} \neq \text{ConductPB} \wedge \text{ConductORP} \neq \text{CompletePB} \wedge \\
& \text{ConductORP} \neq \text{unAuthenticated} \wedge \text{MoveToPB} \neq \text{ConductPB} \wedge \\
& \text{MoveToPB} \neq \text{CompletePB} \wedge \text{MoveToPB} \neq \text{unAuthenticated} \wedge \\
& \text{ConductPB} \neq \text{CompletePB} \wedge \text{ConductPB} \neq \text{unAuthenticated} \wedge \\
& \text{CompletePB} \neq \text{unAuthenticated}
\end{aligned}$$

[slState_distinct_clauses]

$$\begin{aligned}
& \vdash \text{PLAN_PB} \neq \text{MOVE_TO_ORP} \wedge \text{PLAN_PB} \neq \text{CONDUCT_ORP} \wedge \\
& \text{PLAN_PB} \neq \text{MOVE_TO_PB} \wedge \text{PLAN_PB} \neq \text{CONDUCT_PB} \wedge \\
& \text{PLAN_PB} \neq \text{COMPLETE_PB} \wedge \text{MOVE_TO_ORP} \neq \text{CONDUCT_ORP} \wedge \\
& \text{MOVE_TO_ORP} \neq \text{MOVE_TO_PB} \wedge \text{MOVE_TO_ORP} \neq \text{CONDUCT_PB} \wedge \\
& \text{MOVE_TO_ORP} \neq \text{COMPLETE_PB} \wedge \text{CONDUCT_ORP} \neq \text{MOVE_TO_PB} \wedge \\
& \text{CONDUCT_ORP} \neq \text{CONDUCT_PB} \wedge \text{CONDUCT_ORP} \neq \text{COMPLETE_PB} \wedge \\
& \text{MOVE_TO_PB} \neq \text{CONDUCT_PB} \wedge \text{MOVE_TO_PB} \neq \text{COMPLETE_PB} \wedge \\
& \text{CONDUCT_PB} \neq \text{COMPLETE_PB}
\end{aligned}$$

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