



Experimental Twin-Field Quantum Key Distribution Through Sending-or-Not-Sending

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Twin-Field QKD (TF-QKD)

Proposed in 2018, which “greatly extending the range of secure quantum communications”, and “feasible with current technology”.

Lucamarini, M., et.al., *Nature* **557**, 400–403 (2018).

LETTER

<https://doi.org/10.1038/s41586-018-0066-6>

Overcoming the rate-distance limit of quantum key distribution without quantum repeaters

M. Lucamarini^{1*}, Z. L. Yuan¹, J. F. Dynes¹ & A. J. Shields¹

Quantum key distribution (QKD)^{1,2} allows two distant parties to share encryption keys with security based on physical laws. Experimentally, QKD has been implemented via optical means.

latter, outer space provides a low-loss propagation medium, but the key rate per loss unit remains unchanged.

On the other hand, the scheme presented here can overcome the

Recent Progress

Theories

- Nature **557**, 400 (2018).
Phys Rev Appl **12**, 054034 (2018).
Phys Rev Appl **11**, 034053 (2018).
Phys Rev X **8**, 031043 (2018).
Phys Rev A **98**, 042332 (2018).
Npj QI **5**, 64 (2019).
Phys Rev A **98**, 062323 (2018).
New J Phys **21**, 073001 (2019).
New J Phys **21**, 113032 (2019).
New J Phys **22**, 013020 (2019).
PR Applied **11**, 034053 (2019).
Phys Rev A **100**, 062337 (2019).
Phys Rev Appl **12**, 024061 (2019).
Phys Rev A **100**, 022306 (2019).
Sci Report **9**, 14918 (2019).
New J Phys **21**, 123030 (2019).
Npj QI **5**, 64 (2019).
Phys Rev A **99**, 062316 (2019).
Opt Lett **44**, 1468 (2019).
Phys Rev A **101**, 042330 (2020).
New J Phys **22**, 053048 (2020).
Opt Express **28**, 22594 (2020).

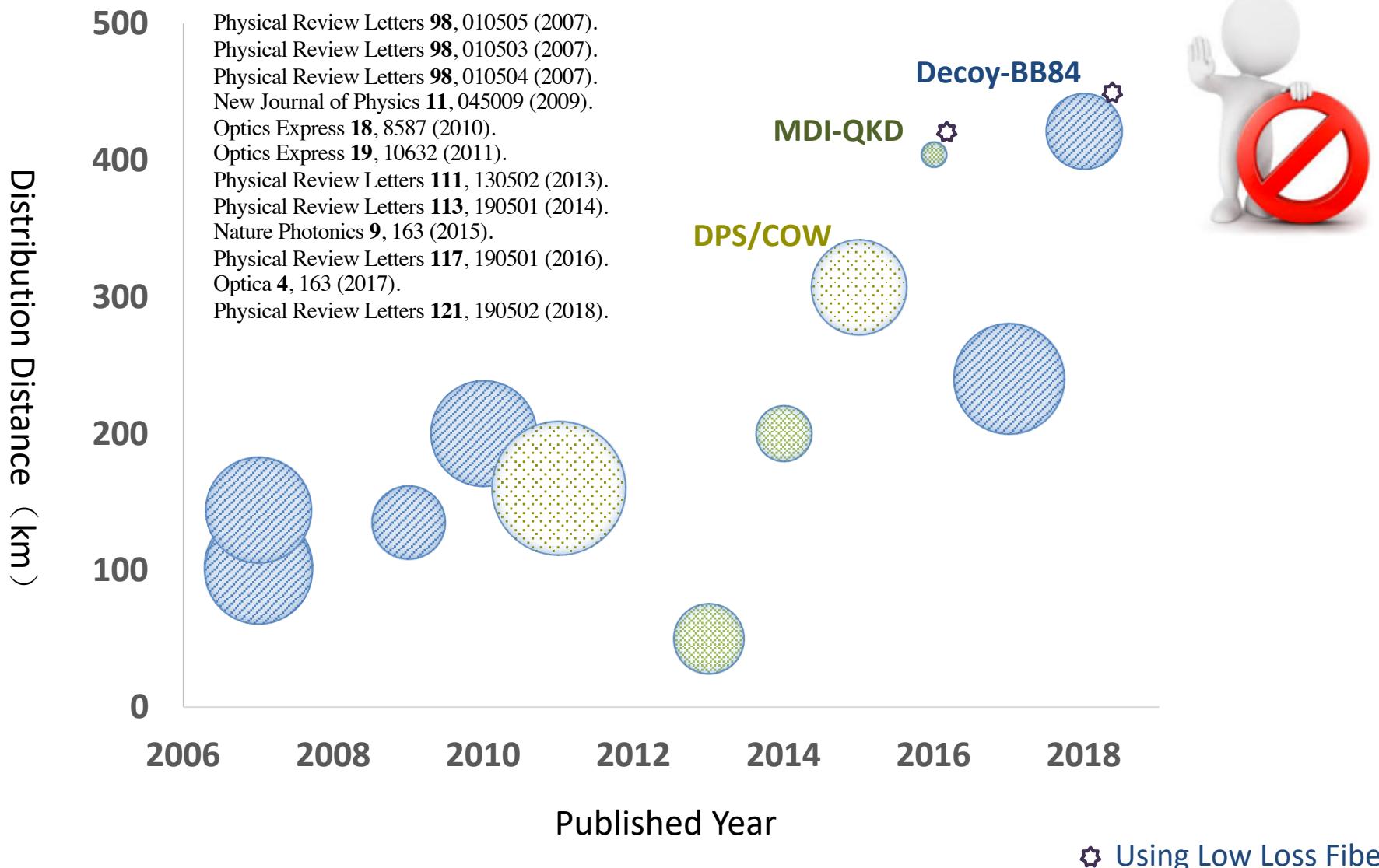
Experiments

- Experimental quantum key distribution beyond the repeaterless secret key capacity, *Nature Photonics* **13**, 334 (2019).
Beating the Fundamental Rate-Distance Limit in a Proof-of-Principle Quantum Key Distribution System, *Physical Review X* **9**, 021046 (2019).
Experimental Twin-Field Quantum Key Distribution Through Sending-or-Not-Sending, *Physical Review Letters* **123**, 100505 (2019).
Proof-of-Principle Experimental Demonstration of Twin-Field Type Quantum Key Distribution, *Physical review letters* **123**, 100506 (2019).
Sending-or-Not-Sending with Independent Lasers: Secure Twin-Field Quantum Key Distribution Over 509 km, *Physical Review Letters* **124**, 070501 (2019).
Implementation of quantum key distribution surpassing the linear rate-transmittance bound, *Nat Photonics* **14**, 422–425 (2020).
(and many more works...)

Previous QKD performances

Status of QKD (before TF-QKD) Systems

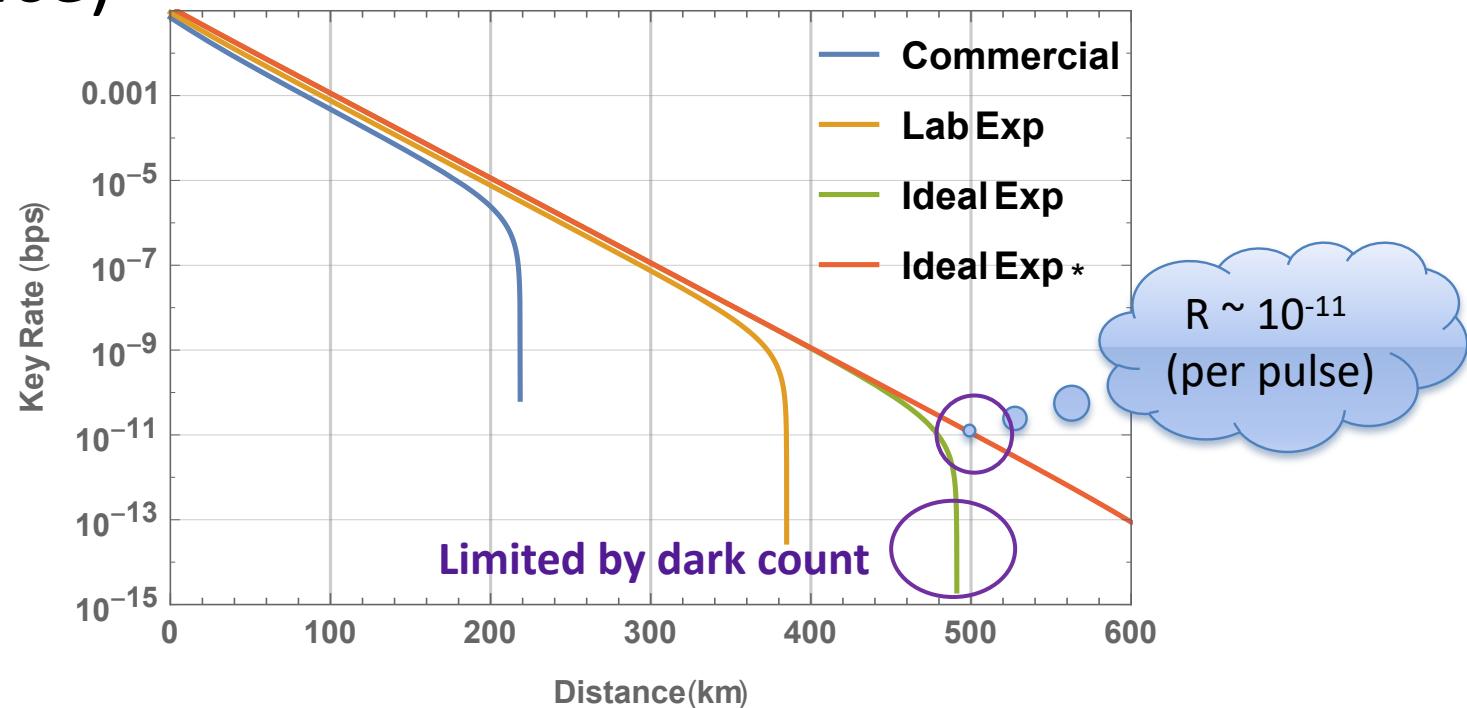
Limited distribution distance in QKD systems



Example: Decoy based BB84 QKD

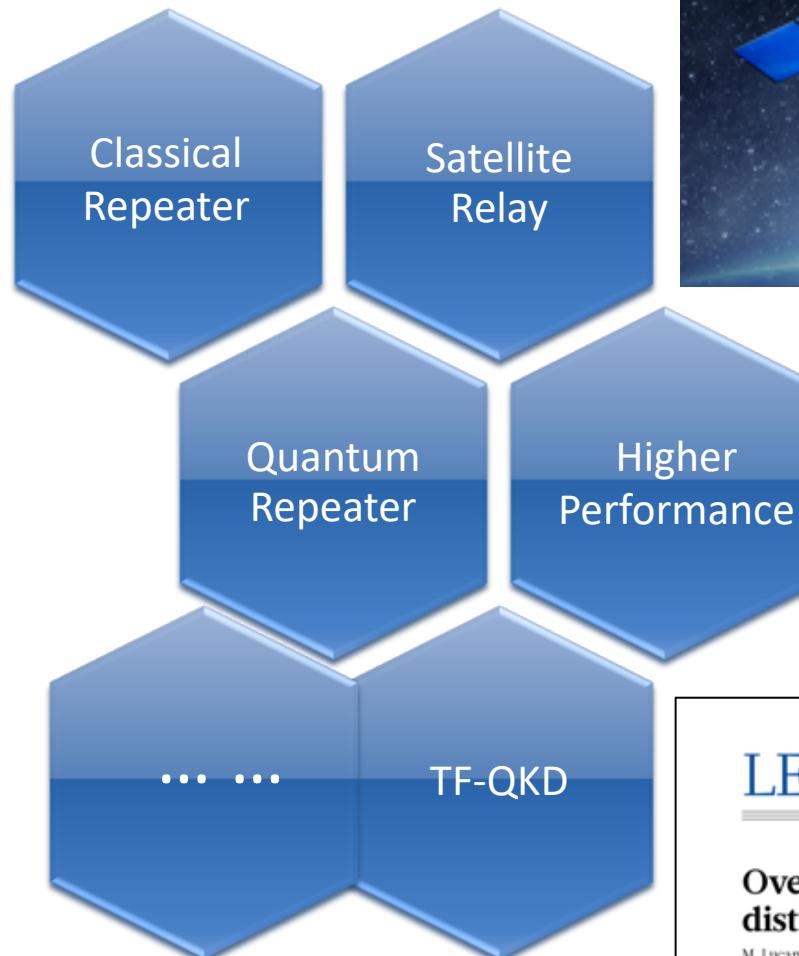
| System | Exp. Time | System Freq. | Det. Efficiency | QBER | Dark count |
|--------------|-----------|--------------|-----------------|------|------------|
| Commercial | 5 mins | 100 MHz | 30% | 2% | 10000 |
| Lab Exp. | 1 Month | 1 GHz | 90% | 1% | 10 |
| Ideal Exp. | >1 Month | 10 GHz | 100% | 0% | 0.1 |
| Ideal Exp. * | >1 Month | 10 GHz | 100% | 0% | 0 |

(In Practice)



To improve the performance...

Further enhancing the distribution distance



Nature 557, 400 (2018)

LETTER

<https://doi.org/10.1038/nature25701>

Overcoming the rate–distance limit of quantum key distribution without quantum repeaters

M. Lucamarini^{1*}, Z. L. Yuan¹, J. F. Dynes¹ & A. J. Shields¹

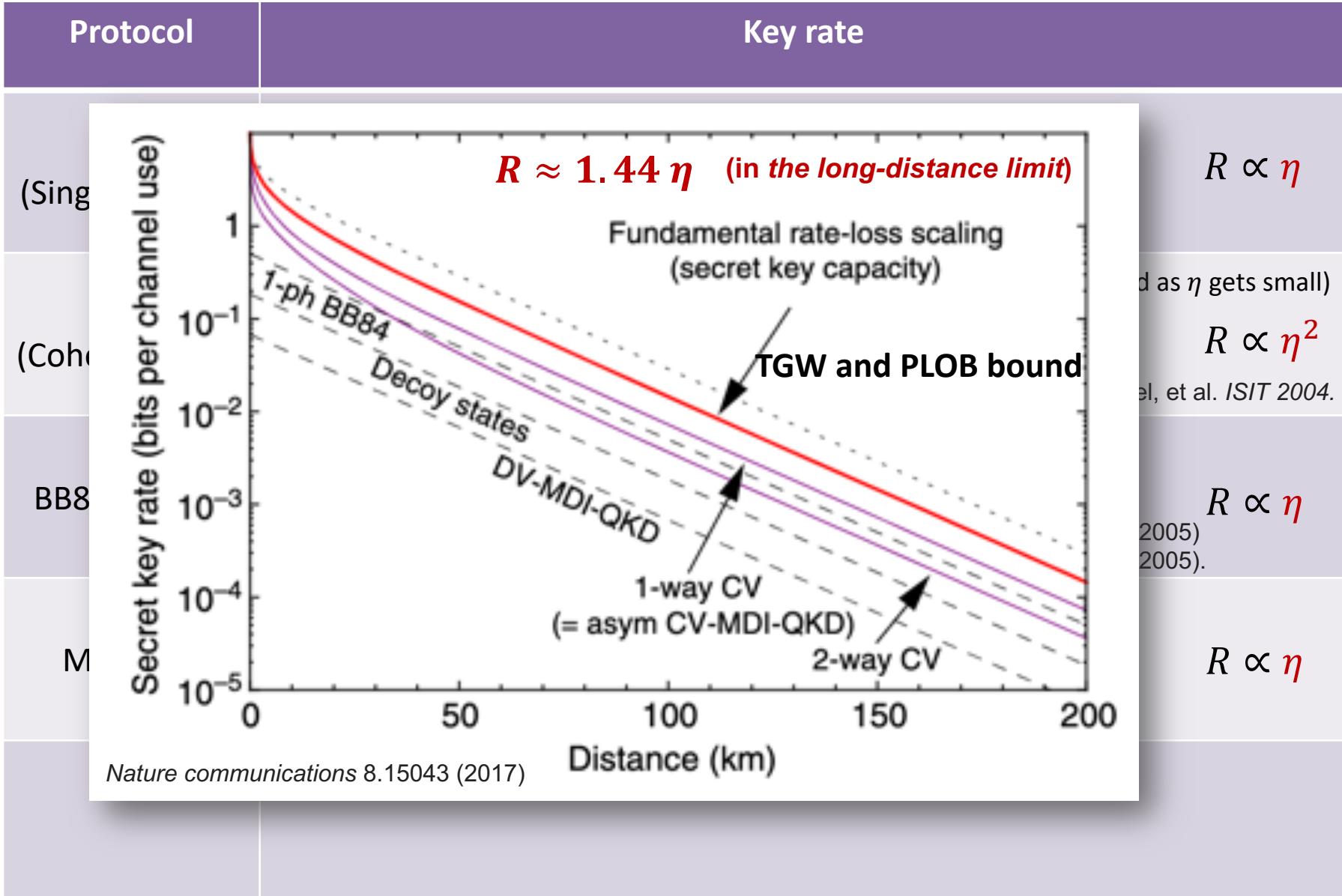
Quantum key distribution (QKD)^{1–2} allows two distant parties to share encryption keys with security based on physical laws. Experimentally, QKD has been implemented via optical means, achieving key rates of 1.26 megabits per second over 50 kilometres of standard optical fibre³ and of 1.16 bits per hour over 404 kilometres of ultralow-loss fibre in a measurement-device-independent configuration⁴. Increasing the bit rate and range of QKD is a latter, outer space provides a low-loss rate per loss unit remains unchanged.

On the other hand, the scheme pre-point-to-point SKC⁵. This is demonstrated by the twin-field QKD (TF-QKD) scheme. TF-QKD (dashed line) overcomes the a

Key rate v.s. Channel loss

| Protocol | Key rate | | |
|--------------------------|--|---|--------------------|
| BB84 (Single Photon) | $R = \eta[1 - H_2(\delta) - H_2(\delta_p)]$ | | $R \propto \eta$ |
| BB84 (Coherent light) | $R = \frac{1}{2} p_D \times R' \approx \eta^2 \Delta \times R'$ $R' = [(1 - \Delta) - H_2(\delta) - (1 - \Delta)H_2\left(\frac{\delta_p}{1 - \Delta}\right)]$ | (if Δ fixed as η gets small) Gottesman, Daniel, et al. <i>ISIT 2004.</i> | $R \propto \eta^2$ |
| BB84 (Decoy) | $R = q\{Q_1[1 - H_2(e_1)] - Q_\mu H_2(E_\mu)\}$ $Q_\mu = Y_0 + 1 - e^{-\eta\mu} \approx \eta\mu$ $Q_1 = \eta\mu e^{-\mu}$ | PRL 94.230503 (2005) PRL 94.230504 (2005). | $R \propto \eta$ |
| MDI-QKD | $R = P_z^{11}Y_z^{11}[1 - H_2(e_x^{1,1})] - Q_z f(E_z)H_2(E_z)$ | | $R \propto \eta$ |
| | | | |

Key rate v.s. Channel loss

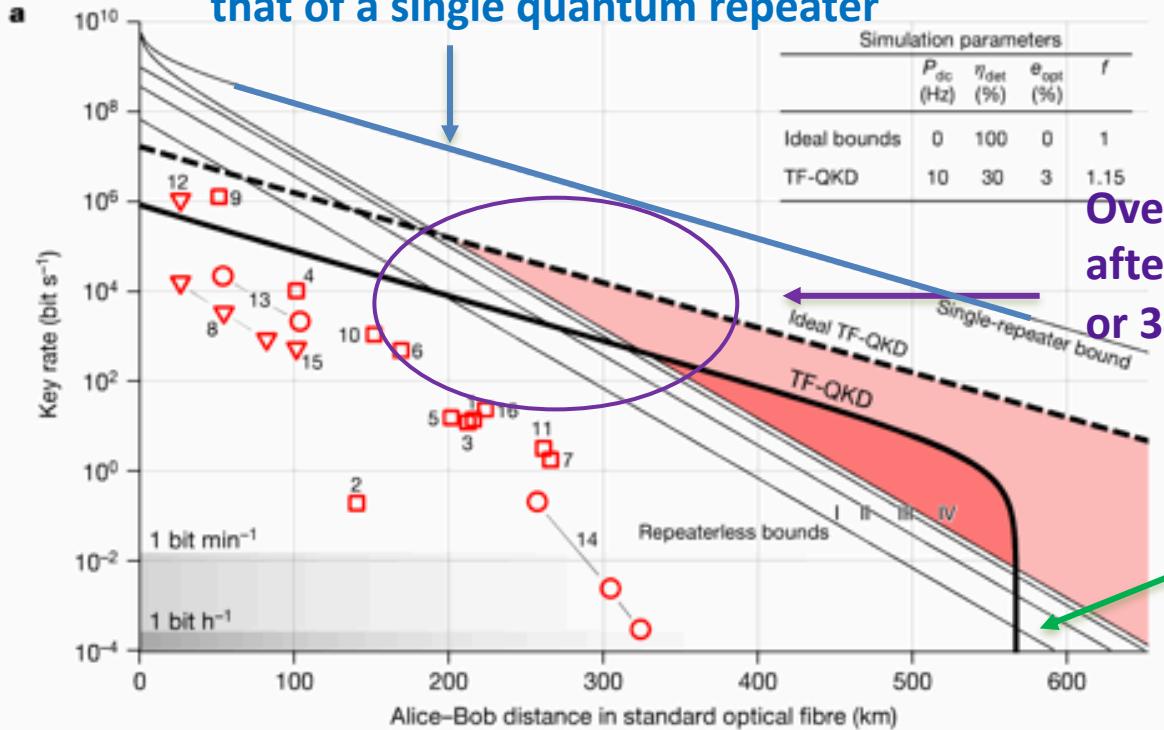


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| TF-QKD | $R = Q_{\mu,L}^1[1 - H_2(e_{\mu,L}^1)] - Q_{\mu,L} f(E_z)H_2(E_{\mu,L})$ | | $R \propto \sqrt{\eta}$ |

Twin-Field QKD (TF-QKD)

Key rate resembles
that of a single quantum repeater

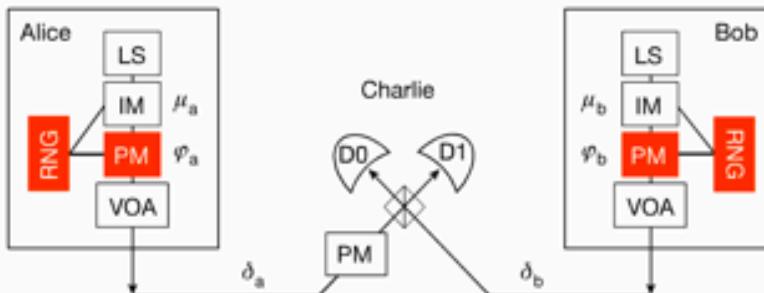


$$R \propto \sqrt{\eta}$$

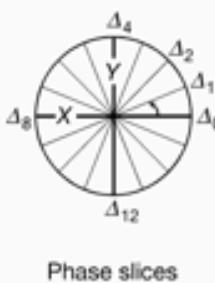
Overcomes the repeaterless bounds
after 200 km (ideal)
or 340 km (practical)

Promises 500 km long
distance distribution

b



c



Lucamarini, et.al., *Nature* 557, 400–403 (2018).

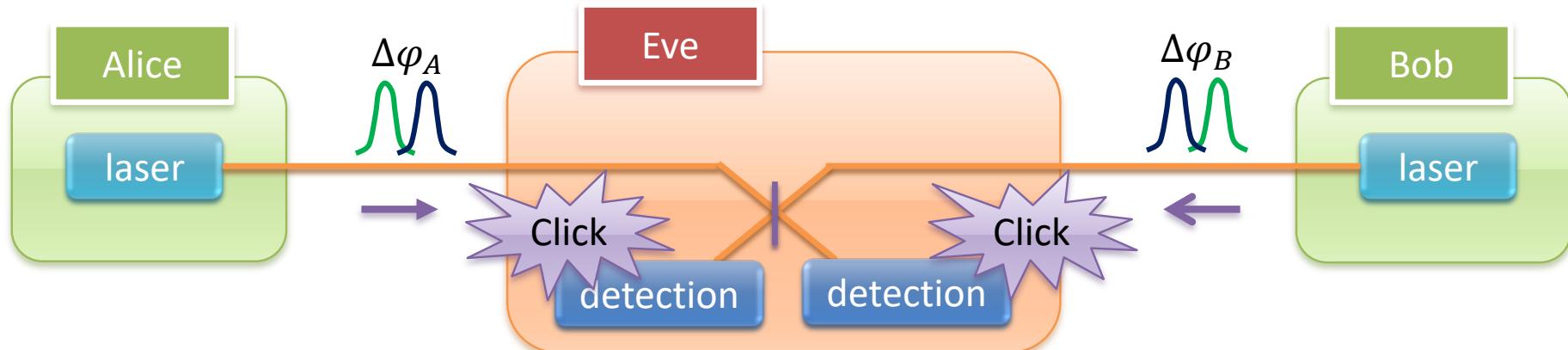
TF-QKD Protocol

To be more specific...

1) General "Sending–Receiving" QKD (e.g., BB84)

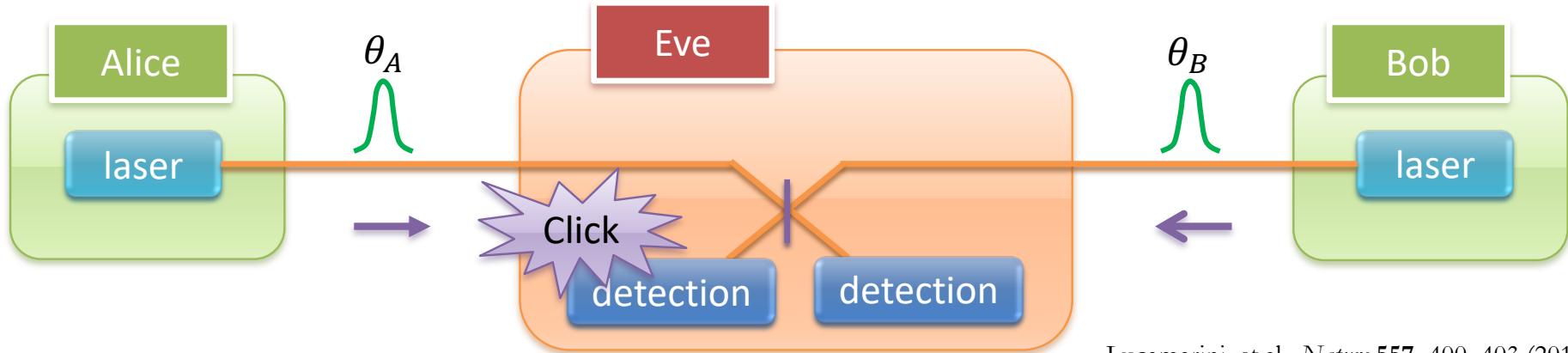


2) Measurement device independent (MDI–QKD)



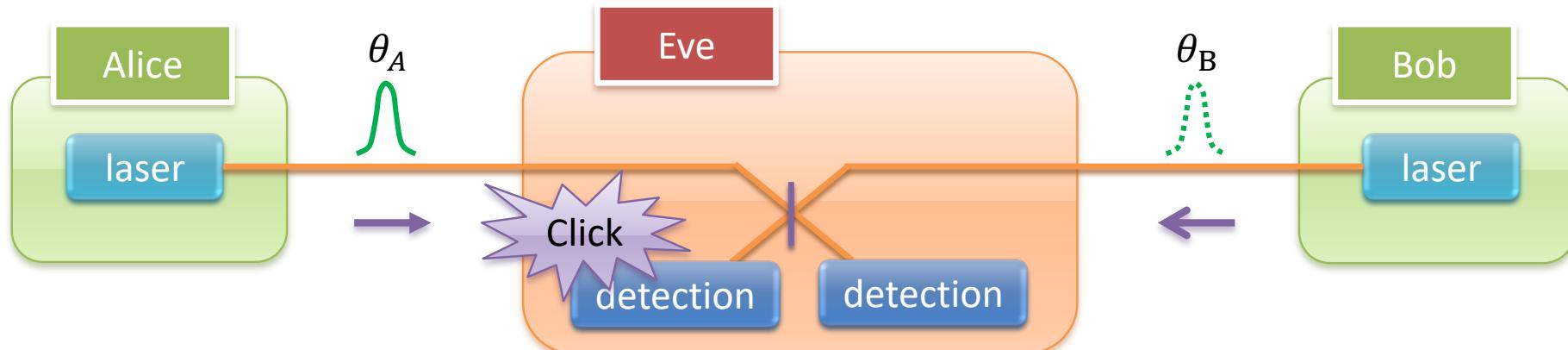
TF-QKD Schemes

3) Twin-Field QKD (QKD)



Lucamarini, et.al., *Nature* **557**, 400–403 (2018).

4) Sending-or-Not-Sending (SNS-TF-QKD)



Wang, X.-B., et.al., *Physical Review A* **98**, 062323 (2018).

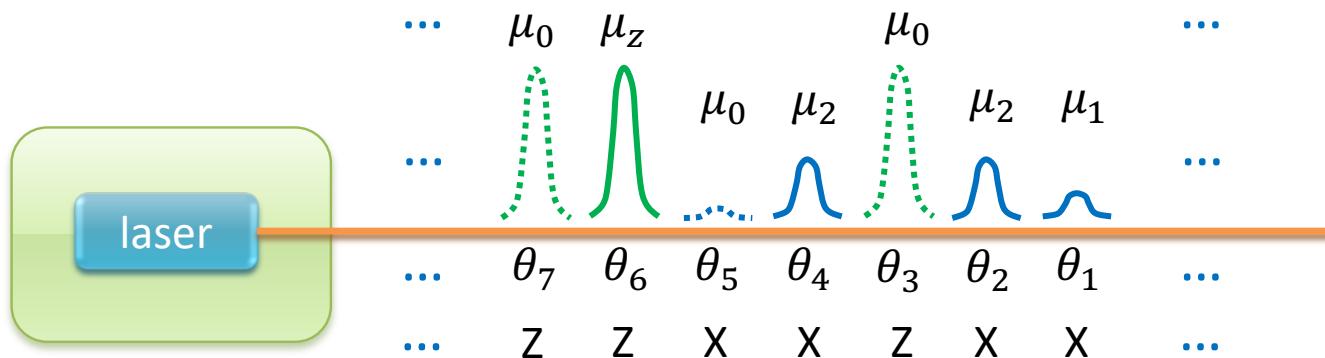
SNS-TF-QKD Introduction: Encoding

Alice/Bob Encoding (Example)

| Basis | Phase (Alice / Bob) | Intensity | S/NS | Probability |
|-------|-----------------------|-------------|-------------|-------------------|
| Z | θ_A / θ_B | μ_z | Not Sending | $p_z * (1 - p_a)$ |
| Z | θ_A / θ_B | μ_z | Sending | $p_z * p_a$ |
| X | θ_A / θ_B | $\mu_0 = 0$ | Sending | $p_X * p_0$ |
| X | θ_A / θ_B | μ_1 | Sending | $p_X * p_1$ |
| X | θ_A / θ_B | μ_2 | Sending | $p_X * p_2$ |

Wang, X.-B., et.al., *Physical Review A* **98**, 062323 (2018).

Z basis: encoding 0/1 with “Send”/“Not Sending” e.g., $|\sqrt{\mu_z} e^{i\theta_A}\rangle |\sqrt{\mu_z} e^{i\theta_B}\rangle$
X basis: encoding with 16 different phases θ_A/θ_B

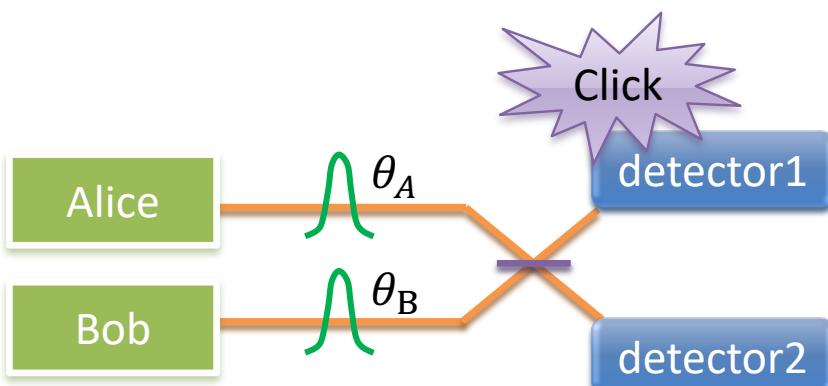


SNS-TF-QKD Introduction: Decoding

Charlie measures all interference, and announces effect event with:
One detector counting if A/B both determined signal/decoy window

Z-Window (A/B choose Z basis)

| | Alice | Bob |
|---------|-------|-----|
| Correct | S | N |
| | N | S |
| Error | S | S |
| | N | N |



X-Window (A/B choose X basis)

Only keep the events satisfy:

$$|\theta_A - \theta_B + \Delta\varphi_T| \leq D_s$$

$$|\theta_A - \theta_B + \Delta\varphi_T| \leq D_s + \pi$$

where $\Delta\varphi_T$ is the path phase,
 D_s is the allowed deviation.

| Range | D_s | $D_s + \pi$ |
|---------|-------|-------------|
| Correct | Det 1 | Det 2 |
| Error | Det 2 | Det 1 |

The phase and bit information are not announced. Detections for different bases are record for analysis.

ZZ00, ZZ03, ZZ30, ZZ33, ZX00, ZX01, ZX02, ZX30, XZ00, XZ10, XZ20, XZ03, XX00, XX01, XX02, XX20, XX11, XX22

SNS-TF-QKD Introduction: Security

Estimate flipping rate in X1-window $e_1^{\mathcal{X}_1} \leq \bar{e}_1^{\mathcal{X}_1} = \frac{S_\mu E_\mu^X - e^{-2\mu} s_0 / 2}{2\mu e^{-2\mu} s_1}$

Asymptotically: $e_1^{ph} = e_1^{\chi_1}$

Final secure key rate: $N_f = n_1 - n_1 H(e_1^{ph}) - n_t f H(E^Z)$

Security is proofed with Virtual protocols and reduction:

Consider virtual ancillary state $\mathcal{A}n$, phase randomized coherent state, extended state is

$$\Omega = \sum_r q_r \Omega_r \quad , \text{with} \quad \Omega_1 = (1/2)(|01\rangle\langle 01| \otimes |01\rangle\langle 01| + |10\rangle\langle 10| \otimes |10\rangle\langle 10|),$$

(for 1-photon/vac/multi-photon)

$$\begin{aligned}\Omega_2 &= (1/2)[(|0\rangle\langle 0| \tilde{\otimes} \bar{\rho}) \otimes |01\rangle\langle 01| + (\bar{\rho} \tilde{\otimes} |0\rangle\langle 0|) \otimes |10\rangle\langle 10|], \\ \Omega_3 &= |00\rangle\langle 00| \otimes |00\rangle\langle 00|, \\ \Omega_4 &= (\rho_{\mu'} \tilde{\otimes} \rho_{\mu'}) \otimes |11\rangle\langle 11|.\end{aligned}$$

Consider 1-photon component, $\Omega_{0i} = |\Psi_{1i}\rangle\langle\Psi_{1i}|$,

$$|\Psi_{1i}\rangle = \frac{1}{\sqrt{2}}(e^{i\gamma_{B_i}}|01\rangle\otimes|01\rangle + e^{i\gamma_{A_i}}|10\rangle\otimes|10\rangle)$$

After Charlie's measuring, and purification ancillary state becomes $|\Phi^0\rangle = |01\rangle + |10\rangle$,
 A/B measure locally to obtain final key k_f or $|\Phi^1\rangle = |01\rangle - |10\rangle$

SNS-TF-QKD Introduction: Conclusion

❖ TF-QKD

- MDI-type QKD protocol
- Key rate scales with square root of loss: $R \propto \sqrt{\eta}$
 - Longer distribution distance and higher key rate

❖ SNS-TF-QKD

- Does not announce phase information
 - So decoy state method can apply
- Phase interference only in X basis
 - QBER in Z basis can be negligibly small
 - Allow high (e.g., 20%) X basis QBER due to interference
 - Still possible to achieve long distribution distance

Challenges in TF-QKD experiment

Experimental TF-QKD is not easy

❖ Single photon interference

- Requires same wavelength independent laser
- Requires ultra narrow laser bandwidth (10 kHz)
- Requires precise fiber phase stabilization

❖ Low dark count noise

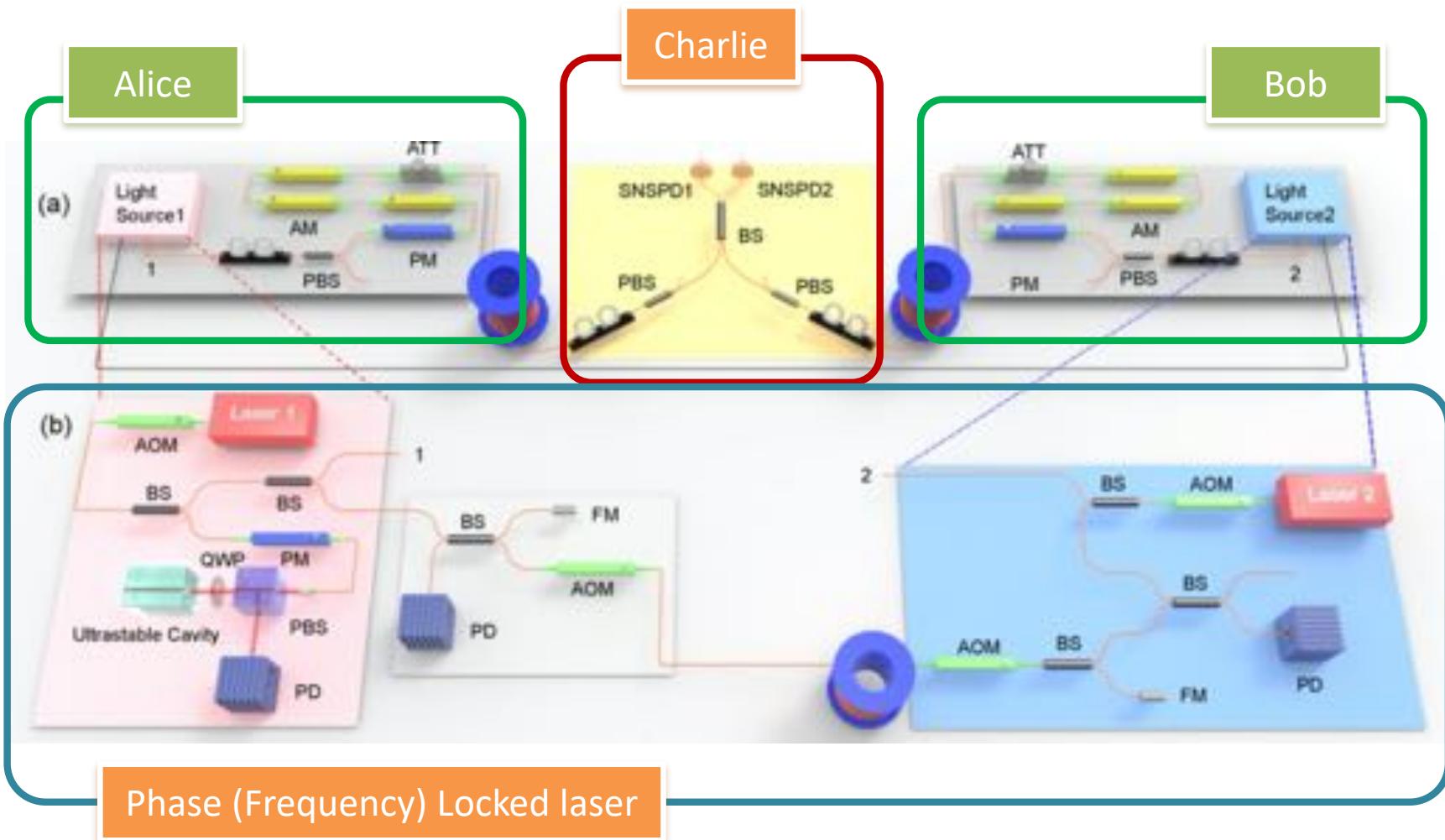
- SNS-TF-QKD requires ultra-low dark count in SPD
- Understanding and controlling fiber noise

❖ Phase stabilization

- Reference pulses requires deep modulation
- Stabilizing/recover phase in short time

SNS-TF-QKD experimental setup

SNS-TF-QKD Setup



SNS-TF-QKD: Phase Stabilization

- Phase interference with Independent lasers

$$\delta_{ba} = \frac{2\pi}{s}(\Delta\nu L + \nu\Delta L)$$

Wavelength
difference (A/B)

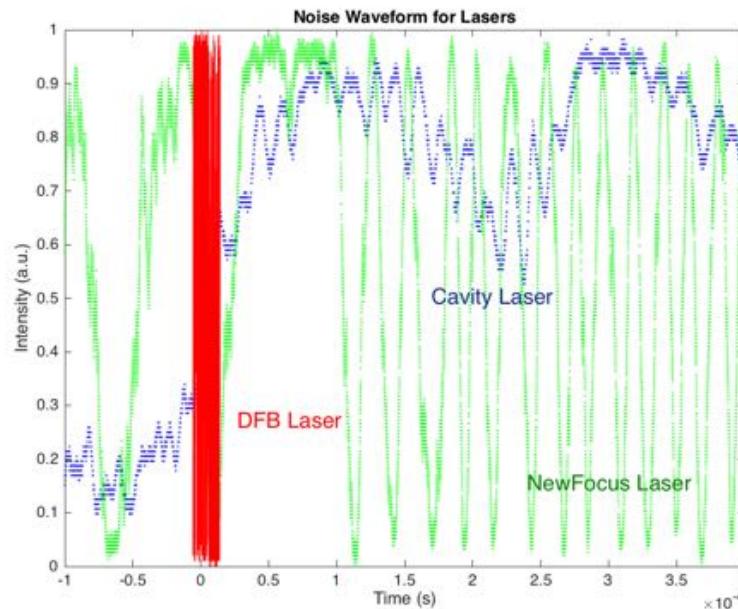
Fiber length
difference (A/B)

MDI-QKD (as comparison)
Two photon interference,
do not require phase
interference, only
requires time coincidence
and wavelengths from the
sources are the same.

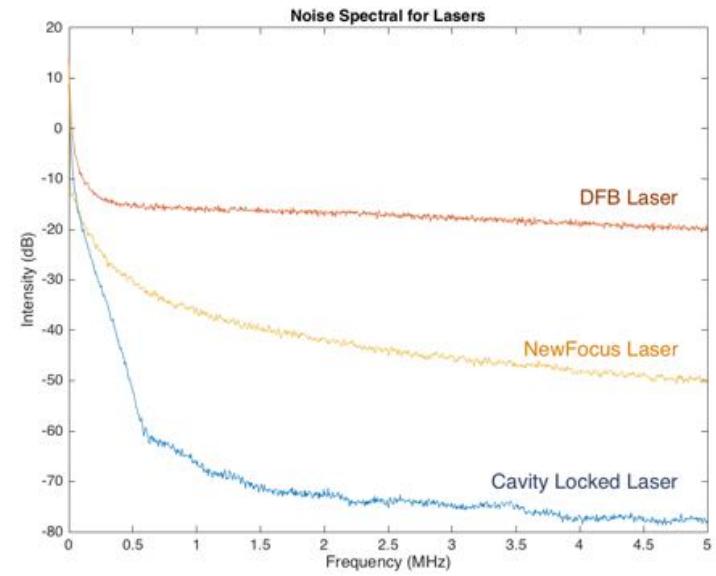
- Stabilizing source wavelength
 - A/B uses narrow bandwidth lasers (<kHz)
 - A/B locks the laser wavelength with each other
- Stabilizing fiber phase fluctuation
 - A/B Stabilize the phase within the statistical period

Laser source stability

- The interference result of single laser source
 - The wavelength stability compared with different lasers
 - With one single source passes a 20 km arm unbalanced interferometer
 - Limits the time period phase is stable



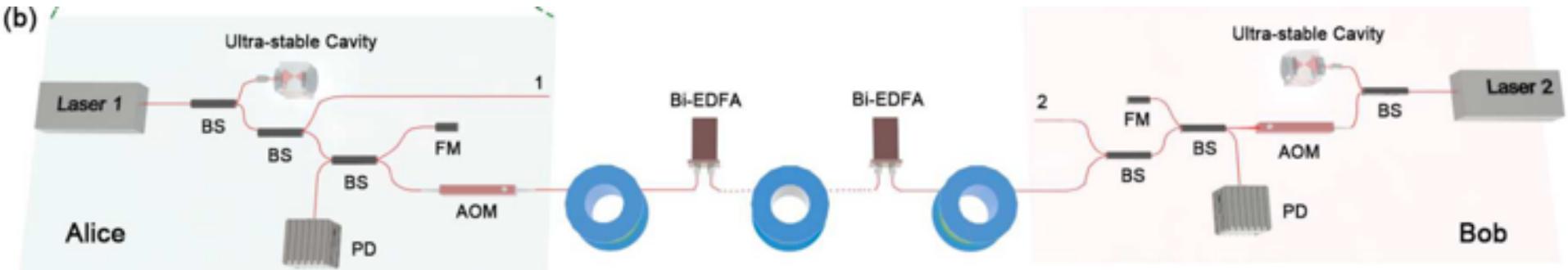
Interference result



Noise spectrom

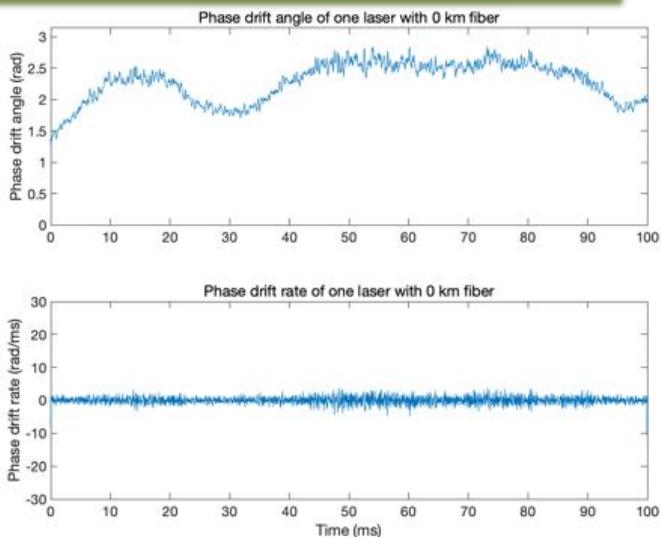
Laser sources

- Continuous wave laser sources (< 1 Hz linewidth)
 - Alice internally locks to her cavity at 1550.0465 nm
 - Bob locks to his cavity at 1550.0474 nm with PDH
 - Relative frequency drift ~ 0.1 Hz/s (freq. diff. ~ 112 MHz)
- Wavelength locking through 500 km fiber (9 EDFAs)
 - B compensate source phase difference with AOM (~ 100 Hz)
 - A compensate fiber phase fluctuation with AOM (~ 50 Hz)
 - Bi-EDFA gain is set to ~ 11 dB to control the signal intensity below the threshold for Stimulated Brillouin Scattering (SBS)

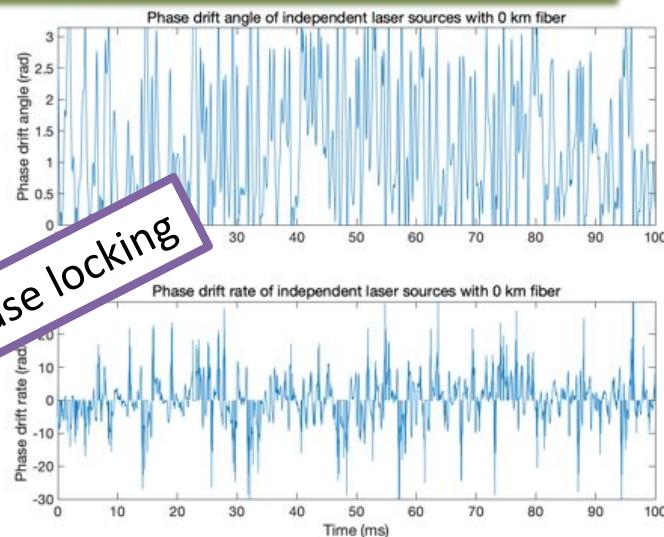


Phase fluctuation by fiber fluctuation

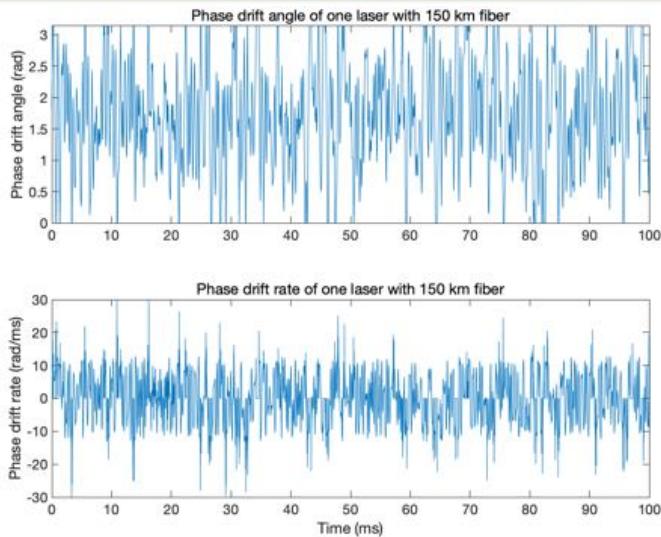
Single source, 0 km: 1.0 rad/ms



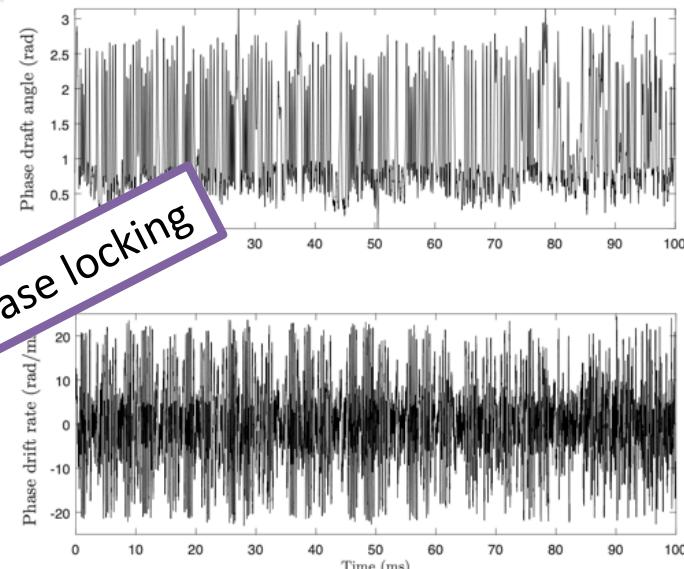
Two sources, 0 km: 5.8 rad/ms



Single source, 75 km x 2: 7.1 rad/ms



Independent lasers, 509 km: 9.6 rad/ms



Compensating fiber phase drift

Estimate fiber phase with reference pulse

Assume phase is stable within $10 \mu\text{s}$

(Based on measure rate 7.5 rad/ms)

- Interference relates to phase difference:

$$I(\phi) = 4 \cos^2(\phi/2)$$

- By sending phase sequences in ref:

$$\theta_A - \theta_B = \{0, \pi/2, \pi, 3\pi/2\}$$

- Consider the relative phase in fiber:

$$\phi = \theta_A - \theta_B + \Delta\varphi_T$$

- We establish error model:

$$Err(\Delta\varphi_T) = \sum_i [p_i - p_{Ti}(\Delta\varphi_T)]^2$$

- Minimizing error to get relative phase $\Delta\varphi_T$

Requirements of Reference Pulse

1. Wavelength: $\lambda_{Ref} = \lambda_{Sig}$
2. Reference travel the same path as signal
3. Reference intensity should be high (~2MHz detection) for quick estimation

$$\theta_A - \theta_B =$$

$$0$$

$$\frac{\pi}{2}$$

$$\pi$$

$$\frac{3\pi}{2}$$

$$4$$

$$3$$

$$2$$

$$1$$

$$0$$

$$-1$$

$$-2$$

$$-3$$

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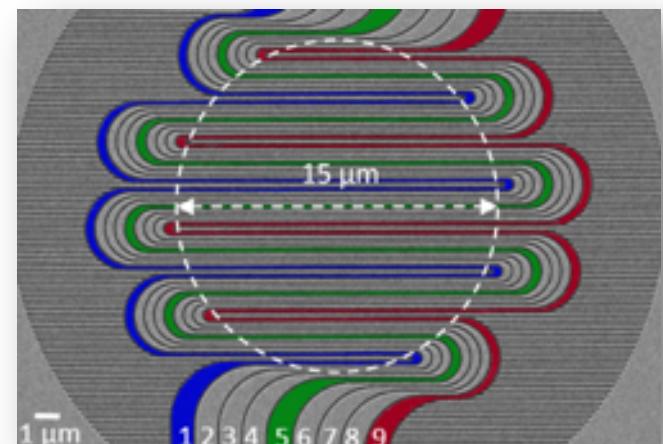
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superconducting nanowire SPD (SNSPD)

- Higher Counting rate
 - For fast phase compensation with reference pulses
 - Parallel configuration → reduces kinetic inductance → reduce recovery time
 - 50 Ohm shunt resistor → prevent the detector latching at high count rates
 - Achieves 10 Mhz with continuous light test (>3MHz that is required)
- Lower Dark count for Signal
 - For long distance distribution. QBER-Z is ultra-sensitive to noise.
 - Integrating a filter onto the end face of the coupling fiber
→ reduce dark count and the insertion loss
 - active area of 16 μm in diameter
 - System efficiency 56% and 58%
 - Dark count \sim 3.5 Hz



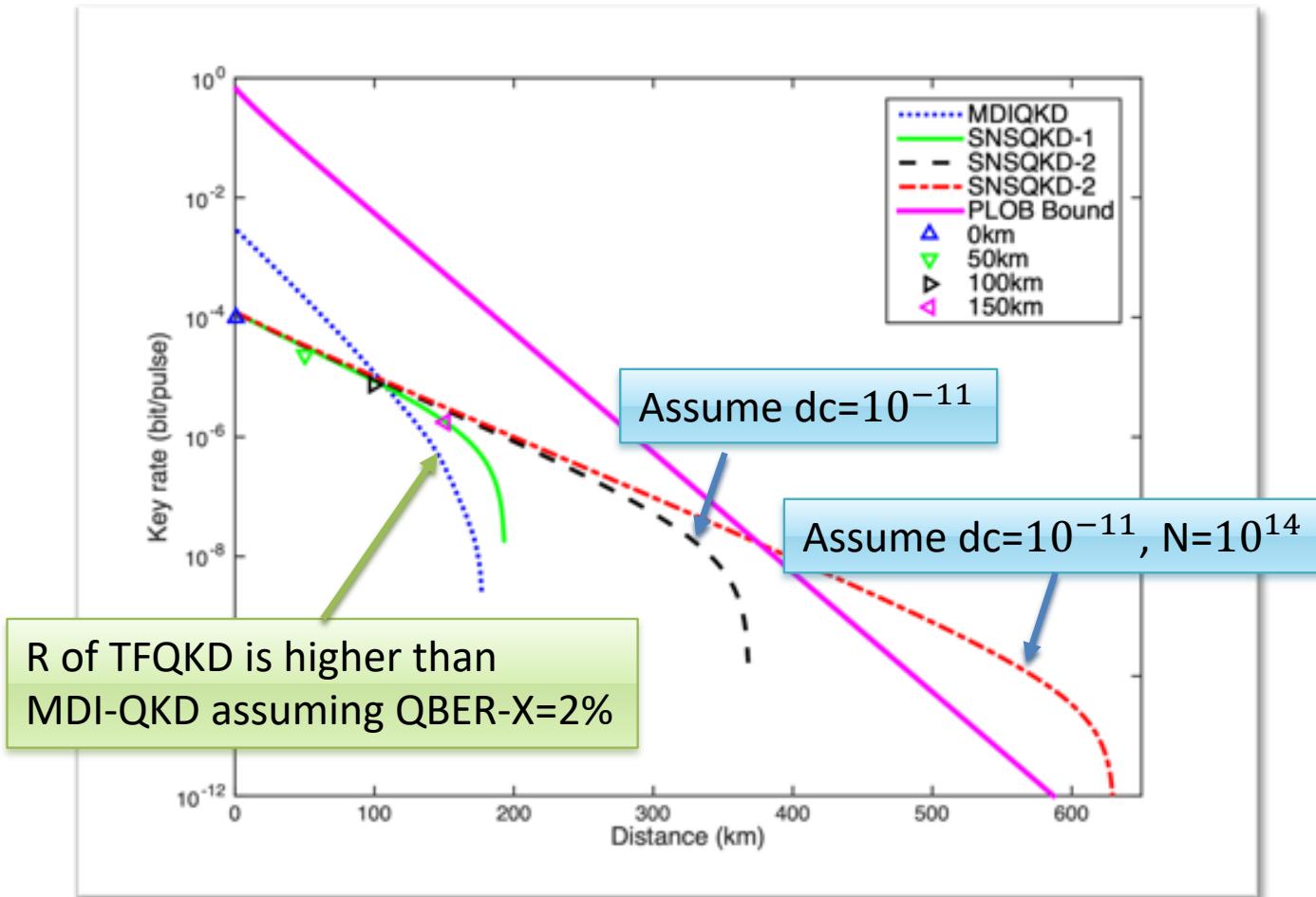
SNS-TF-QKD experimental results

Parameters (that in common)

| | |
|---------------------|--|
| Fiber (Signal) | Fiber spools without stabilization |
| Fiber (locking) | Same or longer than signal fiber |
| System frequency | 30 ns signal interval 3 μ s for signal, 2 μ s for phase estimation |
| Phase estimation | Collect phase estimation data in 10 μ s |
| Fiber drift | <10 rad/ms (up to 509 km) |
| Failure probability | $\epsilon = 10^{-10}$ (considering finite size effect and statistical fluctuation) |

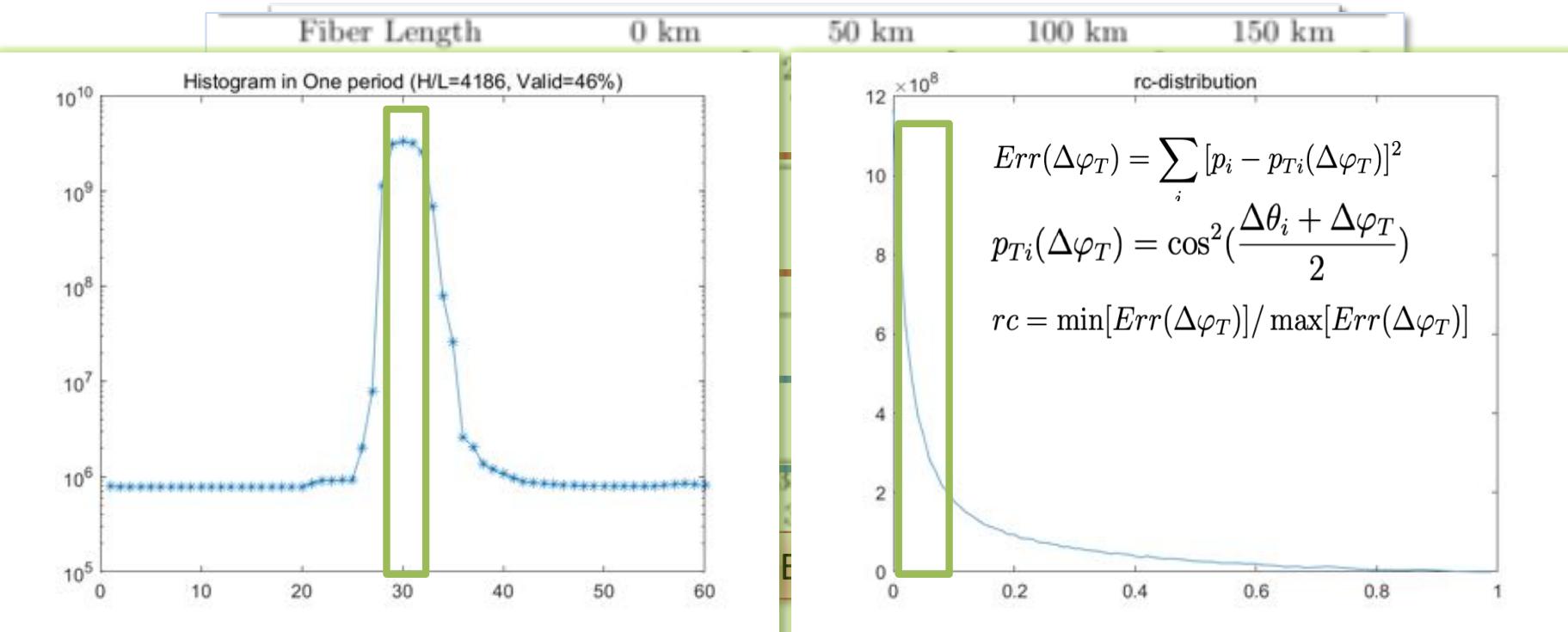
Experiment I: proof of principle

- SNSPD efficiency: 75.3%/76.6%, dark count: ~ 1000 Hz (10^{-6} per ns)
- Total pulses sent = 7.2×10^{11} (about 10 hours)
- Valid detections are:
 $0\text{ km}: 6.5 \times 10^9, 50\text{ km}: 2.3 \times 10^9, 100\text{ km}: 7.6 \times 10^8, 150\text{ km}: 2.5 \times 10^8$



Experiment I: proof of principle

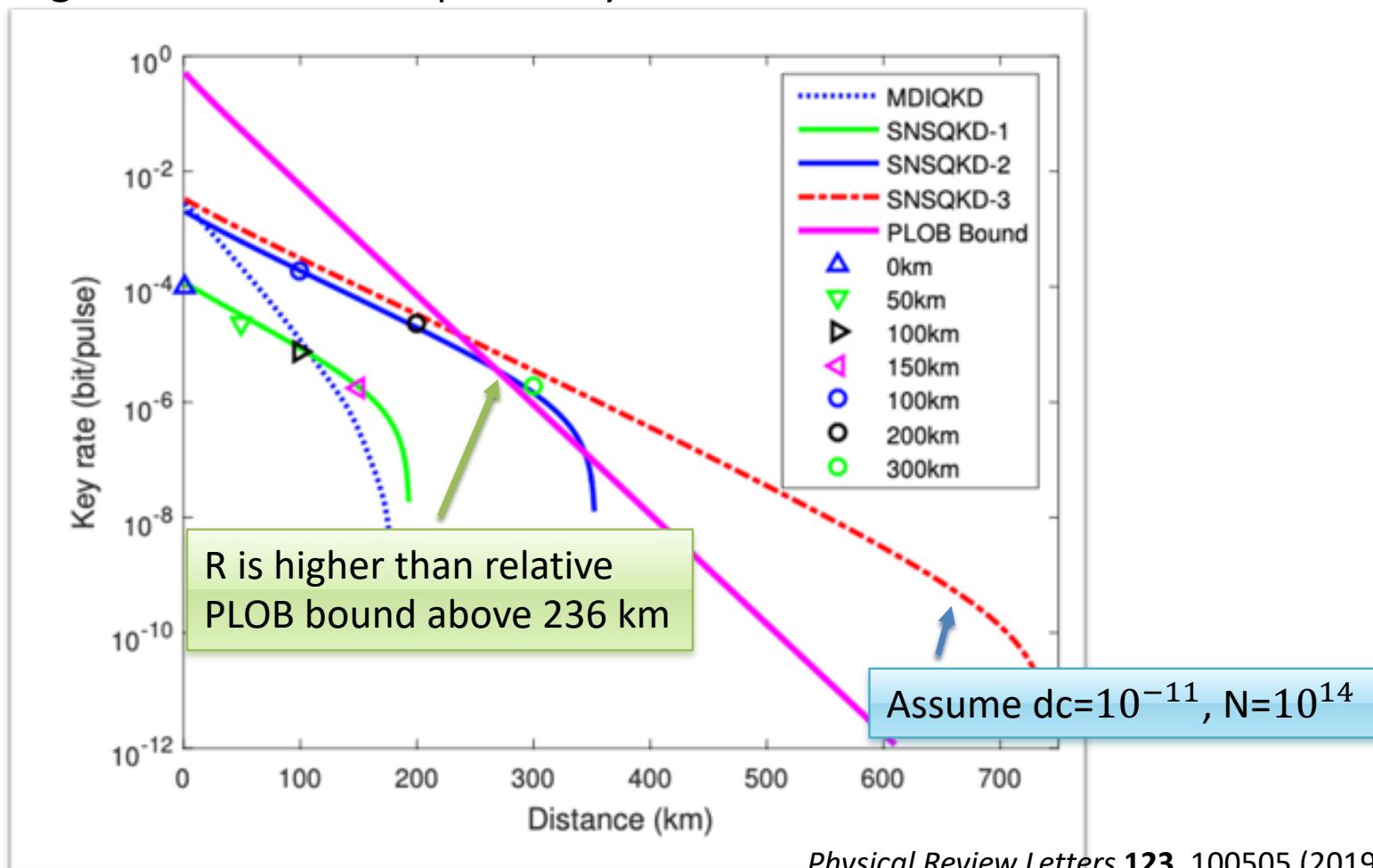
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Sen Sent Filtering pulses and phase help to decrease errors. 74400000
Sent-XZ20 369252000000 369586000000 369860000000 369988000000
Sent-XZ03 8268000000 8330000000 8642000000 8388000000
Sent-XX00 4034200000 4059800000 4006800000 4003000000
Sent-XX01 8159800000 8127400000 8009600000 8139000000

Experiment II: higher than relative PLOB

- SNSPD efficiency: 58%/38%, dark count: ~ 100 Hz (10^{-7} per ns)
- Total pulses sent = 7.2×10^{11} (about 10 hours)
- Valid detections 100 km: 1.7×10^9 , 200 km: 1.9×10^8 , 300 km: 2.4×10^7
- Decreasing QBER-X with the updated system



Experiment II: higher than relative PLOB

- SNSPD efficiency: 58%/38%, dark count: ~ 100 Hz (10^{-7} per ns)
- Total pulses sent = 7.2×10^{11} (about 10 hours)
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Phase error can be controlled under realistic condition

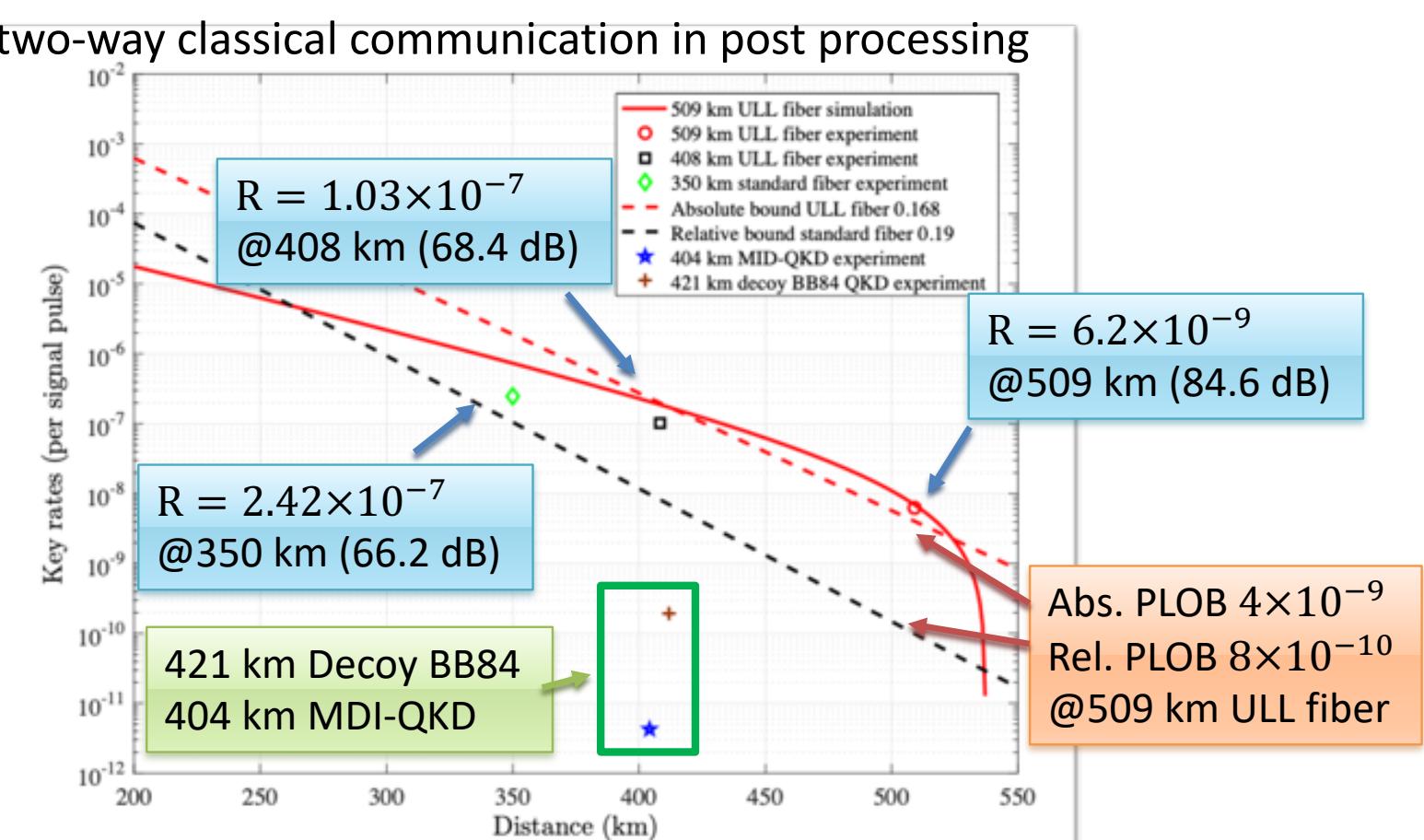
| Length | 100 km* | 200 km* | 300 km* |
|-------------|------------------------|------------------------|------------------------|
| R | 1.841×10^{-4} | 2.405×10^{-5} | 1.957×10^{-6} |
| s_1 | 3.26×10^{-2} | 3.96×10^{-3} | 4.99×10^{-4} |
| e_1^{ph} | 2.09% | 2.07% | 3.58% |
| QBER(Z) | 4.15% | 4.25% | 5.29% |
| QBER(X11) | 1.49% | 1.43% | 1.40% |
| QBER(X22) | 1.44% | 1.33% | 1.30% |
| rc | 1 | 1 | 0.3 |
| D_s | 5° | 5° | 8° |
| r_{rc} | 1 | 1 | 0.99985 |
| r_{gate} | 0.87 | 0.85 | 0.82 |
| N_{total} | 7.20×10^{11} | | |
| Syst. ZZ | 460668400000 | 460820400000 | 460688800000 |

QBER-Z is optimized
QBER v.s. detections

Phase estimation is good enough in experiment

Experiment III: higher than absolute PLOB

- SNSPD efficiency: 58%/56%, dark count: ~ 3.5 Hz (3.5×10^{-9} per ns)
- Total pulses sent 350 km: 2.1×10^{11} , 408 km: 3.5×10^{11} , 509 km: 1.1×10^{12}
- Valid detections 350 km: 2.0×10^6 , 408 km: 2.6×10^6 , 509 km: 9.0×10^5
- Using Ultra-Low-Loss fiber in 509 km (84.6 dB) experiment
- Using two-way classical communication in post processing



Re-Rayleigh Scattering Noise in Fiber

- Rayleigh scattering (elastic scattering) in fiber
 - The intensity is proportional to the input power $P_L = P_0 e^{-\alpha L}$

$$dP_B = dP_{B'} e^{-\alpha L} = P_L S e^{-\alpha L} dL = P_0 S e^{-2\alpha L} dL$$

$$\text{– Total reflected power } P_B = \int_0^L dP_B = \frac{P_0 S}{2\alpha} (1 - e^{-2\alpha L})$$

- Back Scattered light is again back scattered (Re-Rayleigh Scattering)

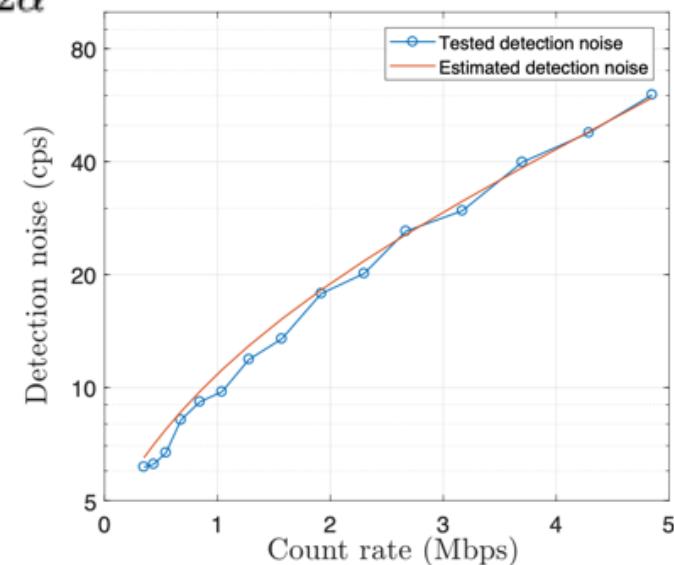
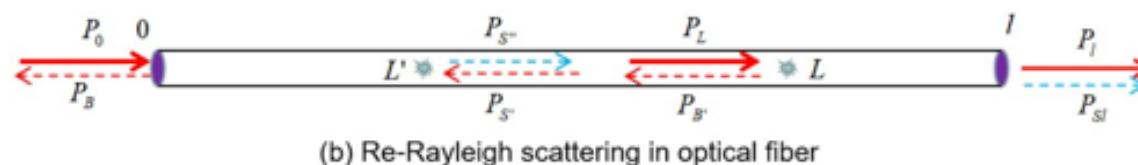
$$dP_{Sl} = P_0 S^2 e^{-\alpha L} e^{-\alpha(L-L')} e^{-\alpha(l-L')} dL dL'$$

- With random polarization, the total power is

$$P_{srs} = \frac{1}{2} P_{Sl} = \frac{P_0 S^2}{4\alpha} e^{-\alpha l} \left[l + \frac{e^{-2\alpha l}}{2\alpha} - \frac{1}{2\alpha} \right]$$

In all time period

$\alpha = -0.168 \text{dB/km}$
 $S = 3.919 \times 10^{-5}$
 Ref = 2MHz (12.65 nW)
 Noise $\approx 8.6 \text{cps}$ (@500km)



Experiment III: higher than absolute PLOB

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- Total pulses sent 350 km: 2.1×10^{11} , 408 km: 3.5×10^{11} , 509 km: 1.1×10^{12}
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- Using Ultra-Low-Loss fiber in 509 km (84.6 dB) experiment
- Using two-way classical communication in post processing

| Fiber Length | 350 km | 408 km | 509 km |
|---|------------------------|------------------------|------------------------|
| N_{total} | 2.046×10^{11} | 3.542×10^{11} | 1.093×10^{12} |
| R | 2.42×10^{-7} | 1.03×10^{-7} | 6.19×10^{-9} |
| n_1 (Before standard two-way classical communication) | 585406 | 562378 | 160781 |
| n_1 (After standard two-way classical communication) | 158767 | 135844 | 43664 |
| e_1^{ph} (Before standard t | 5.89% | 6.95% | 6.88% |
| e_1^{ph} (After standard t | 11.26% | 13.18% | 13.20% |
| QBER($Z - Before$) | 8.44% | 6.99% | 9.87% |
| Odd pairs in raw keys | 230957 | 258911 | 62427 |
| Even Pairs | 113156 | 121455 | 28638 |
| Even Pairs | 122138 | 140446 | 34263 |
| Error pairs in raw keys | 3944 | 2864 | 1486 |
| QBER($Z - After$) | 0.846% | 0.550% | 1.186% |
| QBER(X11) | 3.2% | 3.0% | 3.7% |
| QBER(X22) | 1.4% | 2.7% | 1.5% |
| r_c | 0.5 | 0.3 | 0.3 |
| D_s | 15° | 12° | 12° |
| r_{rc} | 0.9999 | 0.9991 | 0.9988 |
| r_{gate} | 0.51 | 0.48 | 0.35 |
| Sent-ZZ | 143067040000 | 261059700000 | 586934380000 |
| Sent-ZX00 | 912200000 | 1136400000 | 15419600000 |
| Sent_ZX01 | 230688000000 | 351504000000 | 168177400000 |

Two-way communication

| Type | C0 | C1 | D | V |
|-------|----|----|---|---|
| Alice | 0 | 1 | 1 | 0 |
| Bob | 1 | 0 | 1 | 0 |

| e.g. 2 bits | VV | C0C1 | C1D | DV | ... |
|-------------|----|------|-----|----|-----|
| Alice | 00 | 01 | 11 | 10 | ... |
| Bob | 00 | 10 | 01 | 10 | ... |

| Type | CC | VV | DD | CV | VC | CD | DC | VD | DV |
|----------|----|----|----|---------------|---------------|---------------|---------------|----|----|
| Parity A | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 |
| Parity B | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 |

PRA 66, 060302 (2002).
arXiv:1904.06331 (2019).
PRA 101, 042330 (2020).

Assume C=C0, parity checking
(A=B?) is the same for other C

| Type | coco | coc1 | c1c0 | c1c1 | VV | DD | VD | DV |
|----------|------|------|------|------|----|----|----|----|
| Parity B | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 |
| Correct | ○ | ○ | ○ | ○ | ✗ | ✗ | ✗ | ✗ |

bit-flip error rate reduced
dramatically after BFER

Standard two-way classical communication (for phase error) $\tilde{e}_1^{ph} = 2e_1^{ph}(1 - e_1^{ph})$

$$N_f = \tilde{n}_1 [1 - H(\tilde{e}_1^{ph})] - f[n_{t1}H(E_1) + n_{t2}H(E_2) + n_{t3}H(E_3)].$$

Odd Parity Sifting

Actively Odd Parity Sifting (AOPP)

Bit-flip error is concentrated on even-parity pairs:
Sifting or actively make odd parity pairing in
groups, will further reduce the bit flip error.

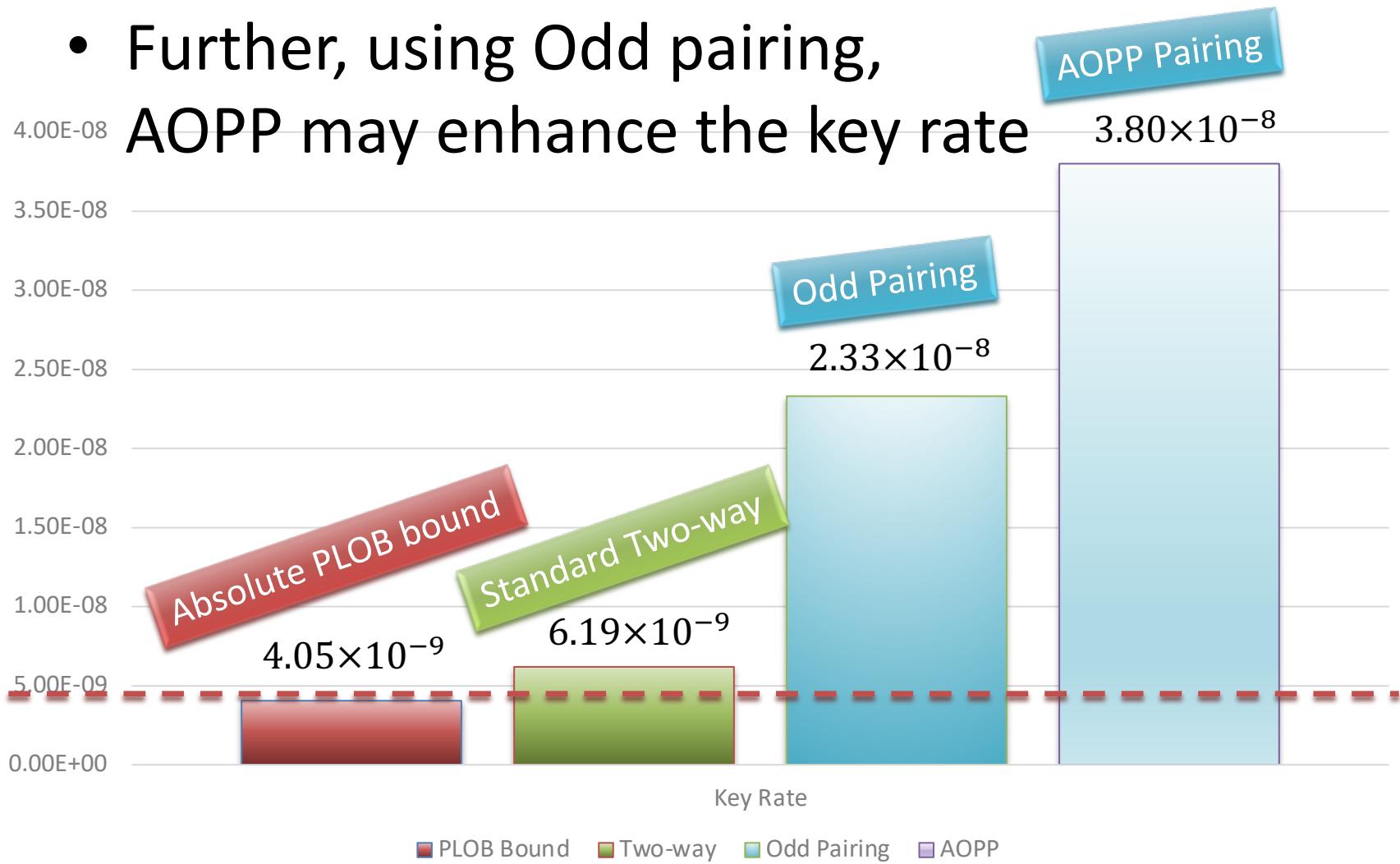
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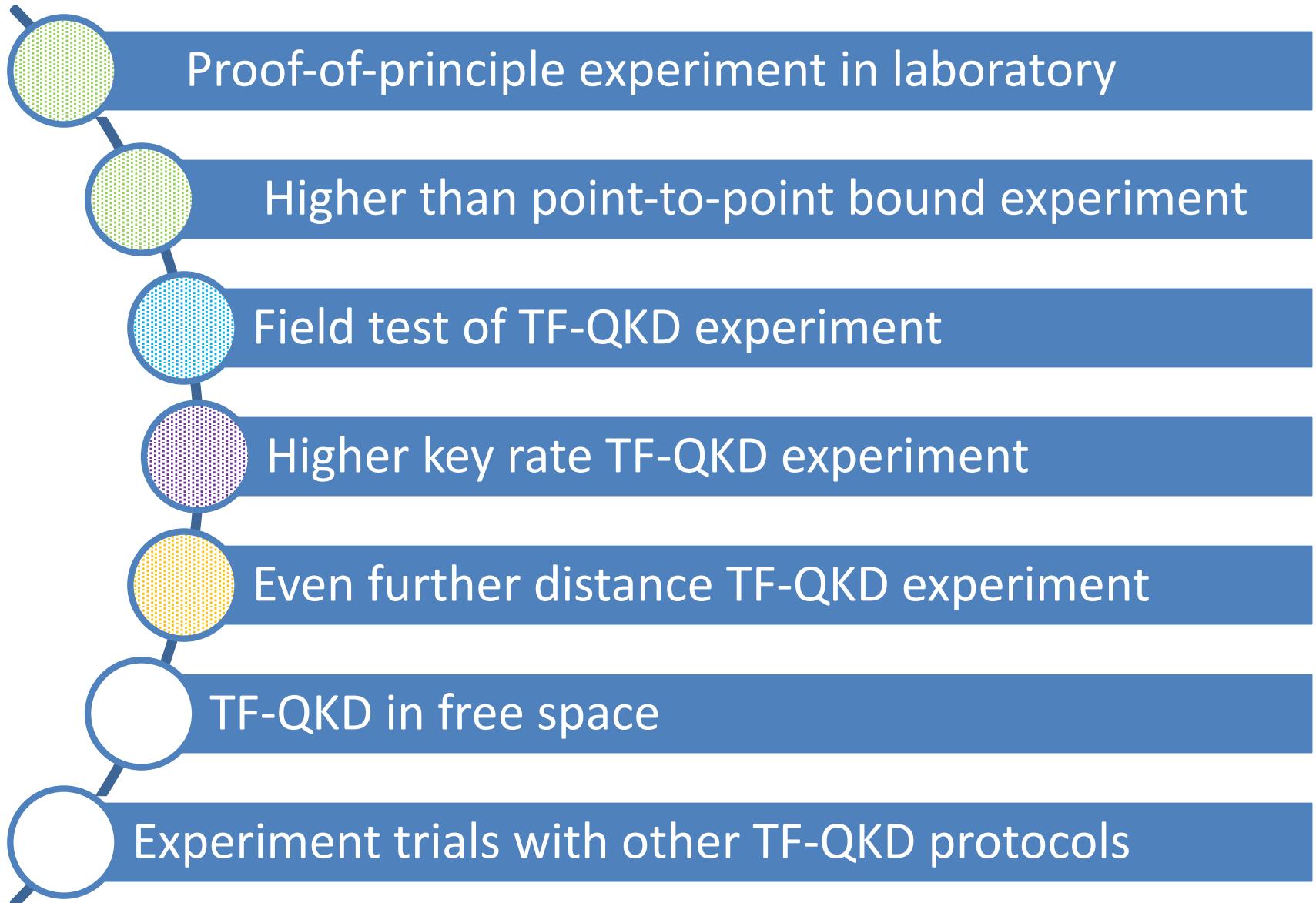
Experiment III: higher than absolute PLOB

- Further, using Odd pairing,
AOPP may enhance the key rate



That is what we have for now, and next...

Outlook

- 
- Proof-of-principle experiment in laboratory
 - Higher than point-to-point bound experiment
 - Field test of TF-QKD experiment
 - Higher key rate TF-QKD experiment
 - Even further distance TF-QKD experiment
 - TF-QKD in free space
 - Experiment trials with other TF-QKD protocols



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**National Key R&D
Program of China**

Corning Inc.
Ming-Jun Li, Hao Chen

**Anhui Initiative in
Quantum Information
Technologies**



Thank you for listening!