Introduction to Social Network Analysis

SICSS Norrköping 2023

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Purpose/content

Introduction to social(-scientific) network analysis

Seeing and thinking in terms of relational data

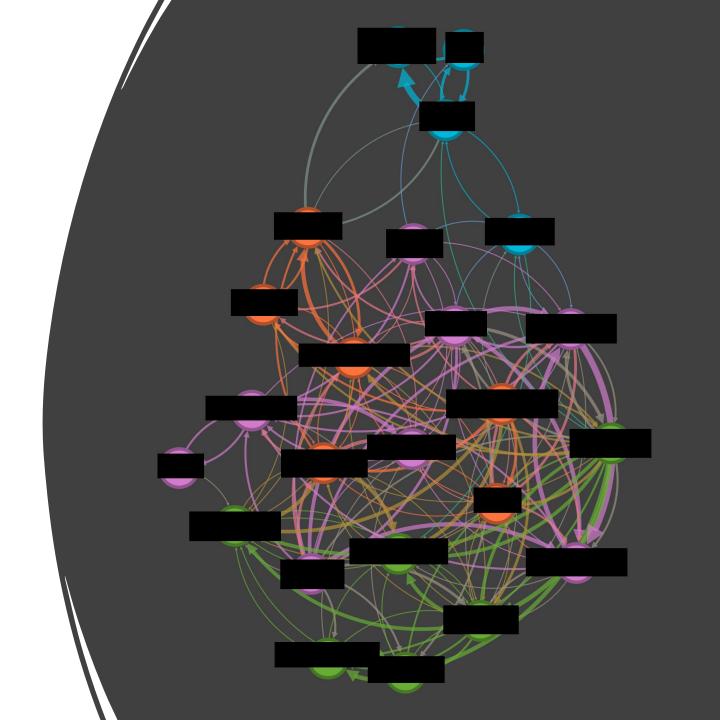
Basic toolkit of (descriptive) methods

Hands-on workshop/lab (R)



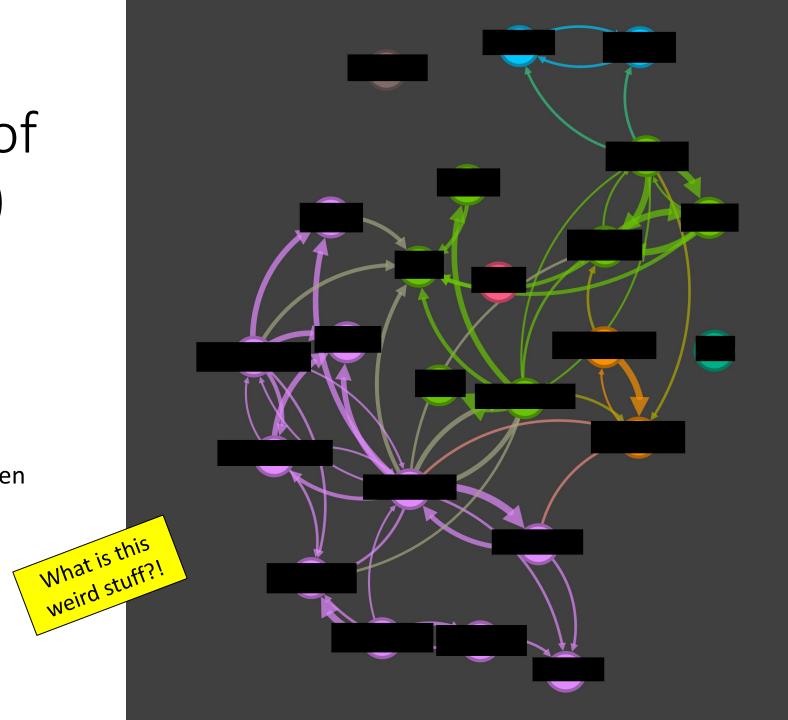
# The SICSS class of 2023 (version A)

- Directional, valued (normalized) network
- Often reciprocal (full self-ties)
- Four communities (Girvan-Newman)
- Valued blockmodeling: ambiguous findings



# The SICSS class of 2023 (version B)

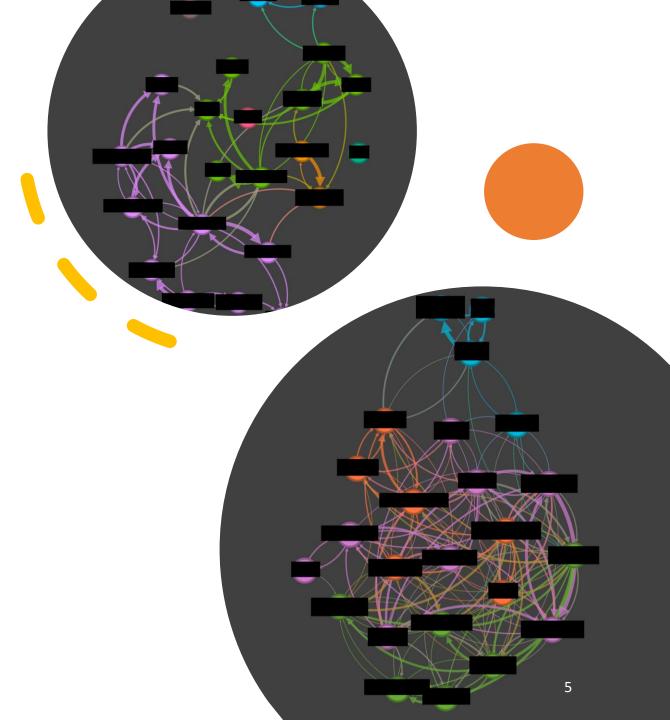
- Different data than version A
- Less dense (singleton positions)
- Previously connected: now disconnected
- Chain structures in purple and green communities
- Complete self-ties

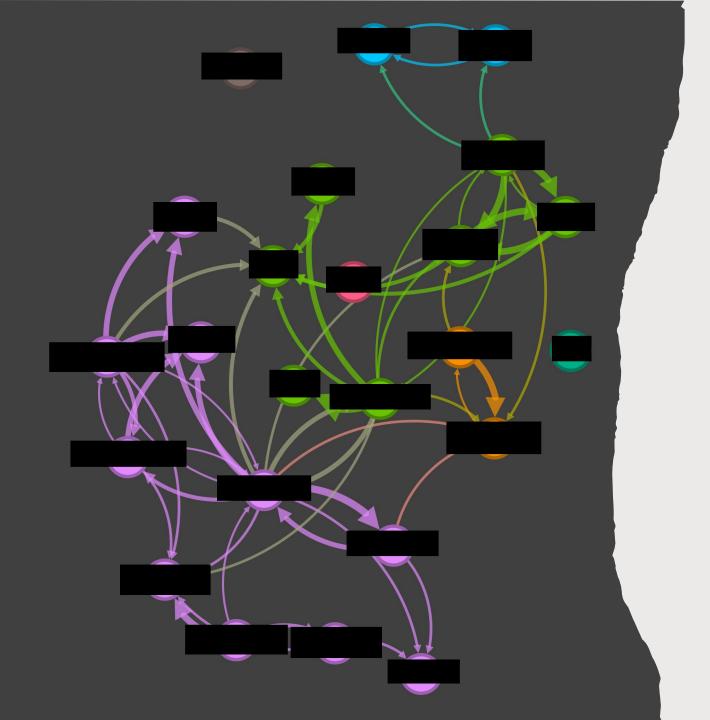


#### Peter networks

- Captures the share of shared letters in your first (A) and last (B) names
- Edge weight(A->B): how much of B's name that can be reconstructed given the letters in A's name
- Prune away all edges with weights < 0.5

 'Relations' solely derived from letters as found in class roster!





# Usefulness of Peter networks?

- None
- A fantastic example of generated pseudo-relational data with zero social-scientific use
- ...that still can be generated, visualized, and analyzed in various ways

...which paves the way to...

Robins (2015), Doing Social Network Research: Network-based Research Design for Social Scientists

# Reasons for network analysis

- To understand how individuals in certain social position have different individual outcome
- To understand how individuals affect social structure
- To facilitate this: (as always) intricate interplay between:
  - Research question
  - Data
  - Methods
  - Theory
- Peter networks: perhaps for visualization methods

#### **Traditional panel data**



Age: 35 Income: 40k Education: BSc Gender: Male



Age: 21 Income: 34k Education: MA Gender: Male



Age: 20 Income: 30k Education: MA Gender: Female



**D**Age: 52
Income: 53k
Education: n/a
Gender: Male



Age: 56 Income: 28k Education: PhD Gender: Female



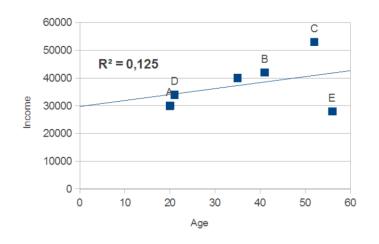
Age: 41 Income: 42k Education: n/a Gender: Female Properties (attributes)
of individual entities

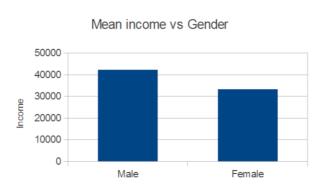
Label	Age	Income	Education	Gender
Α	35	40k	BSc	Male
В	20	30k	MA	Female
С	41	42k	n/a	Female
D	52	53k	n/a	Male
E	21	34k	MA	Male
F	56	28k	PhD	Female

#### **Traditional panel data**

- Comparing two or more 'attributes' among entities
- Identifying would-be associations between variables
- Methods typically assume independence between entities and their attributes
- Sampling possible

#### **Examining statistical associations**











Education: MA



Income: 28k Education: PhD Gender: Female

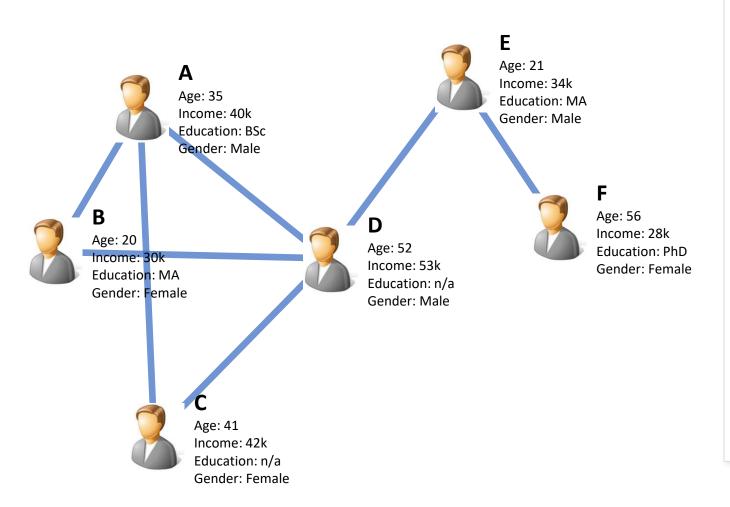


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D	52	53k	n/a	Male
E	21	34k	MA	Male
F	56	28k	PhD	Female

#### **Relational data**

- Entities: actors / nodes / vertices (here: social ones, e.g. individuals)
- Data: sets of relations between entities (e.g. friendship)



#### Friendship (reciprocated) [matrix-format]

	Α	В	С	D	E	F
Α	ı	1	1	1	0	0
В	1	-	0	1	0	0
С	1	0	-	1	0	0
D	1	1	1	-	1	0
E	0	0	0	1	-	1
F	0	0	0	0	1	-

#### **Relational data**

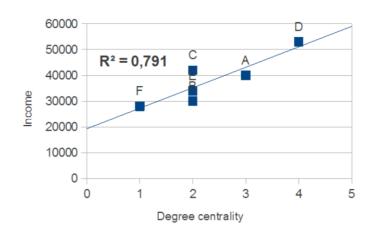
- Entities: actors / nodes / vertices
- Data: sets of relations between entities (e.g. friendship)

#### **Measuring relations**

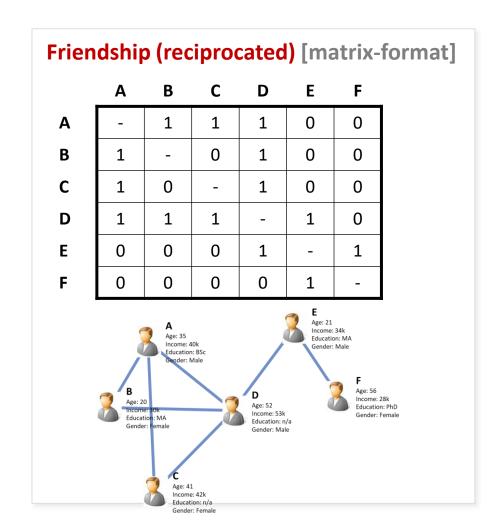
#### **Degree centrality**

Rudimentary individual (micro-level) measure of centrality: Number of ties that a node has

Degree centrality vs Income



- Linking to attributional data
- Likely needs proper null model (rewiring)
- Mere associations



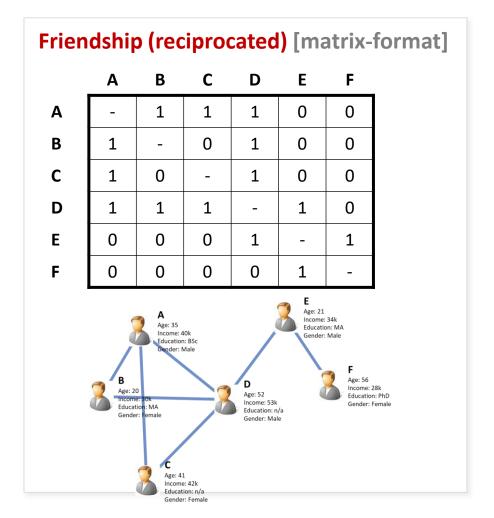
#### **Relational data**

- Capturing the in-between
- Inter-dependence of observations
  - Removing a 'data point' can have grand implications
- Sampling typically problematic
  - System boundaries for full populations important
- Supplementing 'conventional' (attributional) data

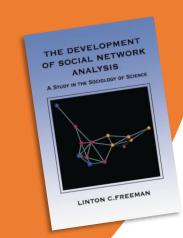
Ethical considerations!

#### The Robins reminders

- Incorporating network data and metrics far more than a mere methodological extension
- Explicit theoretical commitments about structure and dependence: that the in-between matters!
- Going beyond *Hobbesession* with individual, assumedly independent entities to understand social world



# Historical roots and precedents



Behavioural sciences and sociology

- Moreno/Jenning 1930's sociometry
- Classical reference on history of SNA

Earlier precedents (1920s)

• John Almack's (1922), Beth Wellman (1926): homophilic choices in schools



Anthropology

 The bipartite Deep South networks of Davis, Gardner, Gardner (1941)

Human geography

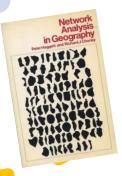
- Kansky (1963)
- Haggett/Chorley (1969)

Relational sociology of 1970's

• (Harrison) White, Burt, Breiger, Wellman, Arabie etc.

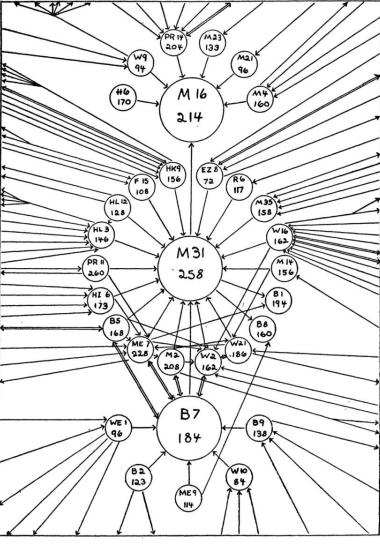
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Freeman, L. (2000). Visualizing Social Networks, Journal of Social Structure, 1(1) Freeman, L. (2004). The Development of Social Network Analysis. Empirical Press.

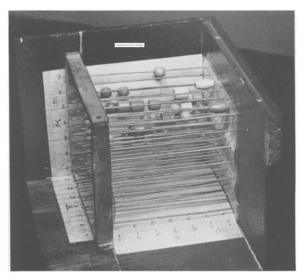


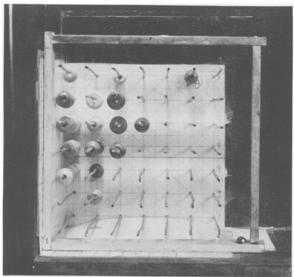


# Historical roots and precedents



Lundberg & Steele (1938), Social Attraction-Patterns in a Village, *Sociometry*, 1 (3/4), p. 387





Chapin (1950), Sociometric Stars as Isolates, American Journal of Sociology, 56(3), p. 265ff



## Network terminology

#### Actor / Node / Vertex

**Entities of interest** 

Often individuals, but also organizations, groups, cities/countries, words etc.

Often have properties/attributes (e.g. age, income, gender etc)

#### Relations / Edges / Links / Dyads

Connecting pairs of actors/nodes

Each set of relations represent different contextual relational types (e.g. friendship, kinship, working relation, road connection, amount of bilateral trade)

#### Network

Collection of (at least) one set of nodes and (at least) one set of edges connecting pairs of nodes



## Types of relations



#### **Directional vs. Symmetric**

- Directional
   Likes, dislikes, trade flow, calls, supervises, talks to, friendship nomination
- Symmetric
  Dialogue, kinship, friendship (reciprocal), road connection, co-presence, co-affiliation

#### **Binary vs. Valued**

- **Binary** Likes, dialogue, alliance, cited in, kinship
- Valued / weighted
   Number of phone calls, degree of friendship (Likert-scaled), number of citations, value of trade flows

## Types and Basic transformations



**Symmetrical** 



**Directional** 

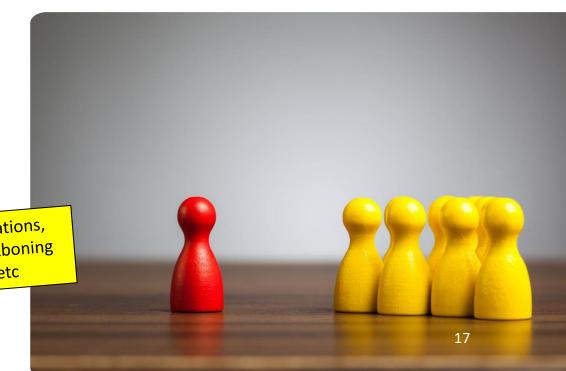
John and Sue are friends
USA and Canada has a treaty
NGO A and B share resources

John and Sue met 4 times
Distance Malmö-Lund is 10 km
Politicians A and B has 5 collabs

Sven dislikes John
Denmark invaded Sweden
John likes Sven

John gave Sue 8 appples
Denmark invaded Sweden twice
Five politicians left party A to B

...and various kinds of normalizations, null models (CM, rewiring, backboning etc), dichotomization, pruning etc



#### Data formats

- Keep tabs on directionality, edge values etc.
- Supplement with actor attributes

#### **Edgelist**

from	to	value
1	9	1
2	6	1
2	7	1
2	9	1
3	5	1
3	8	1
4	7	1
4	11	1
4	15	1
5	3	1

For large (sparse) networks Unclear directionality Optional value columns

#### (Socio)matrix

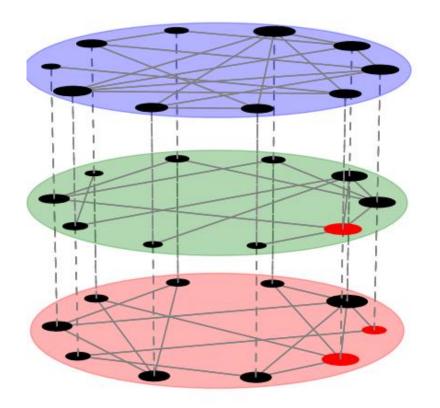
	c1	c2	с3	с4	p11	p12	p21	p22	p31	p32	p33	p41	p42
c1		1	0	1	1	1	0	0	0	0	0	0	0
c2	1		1	0	0	0	1	1	0	0	0	0	0
c3	0	1		1	0	0	0	0	1	1	1	0	0
c4	1	0	1		0	0	0	0	0	0	0	1	1
p11	1	0	0	0		0	0	0	0	0	0	0	0
p12	1	0	0	0	0		0	0	0	0	0	0	0
p21	0	1	0	0	0	0		0	0	0	0	0	0
p22	0	1	0	0	0	0	0		0	0	0	0	0
p31	0	0	1	0	0	0	0	0		0	0	0	0
p32	0	0	1	0	0	0	0	0	0		0	0	0
p33	0	0	1	0	0	0	0	0	0	0		0	0
p41	0	0	0	1	0	0	0	0	0	0	0		0
p42	0	0	0	1	0	0	0	0	0	0	0	0	

For (relatively) small, dense networks All relational types (but takes space) Useful for blockmodeling methods

#### Nodelist (1)

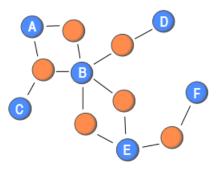
c1	c2	c4	p11	p12	
c2	c1	с3	p21	p22	
c3	c2	c4	p31	p32	p33
c4	c1	c3	p41	p42	
p11	c1				
p12	c1				
p21	c2				
p22	c2				
p31	c3				
p32	c3				
p33	c3				
p41	c4				
p42	c4				

For large binary networks **Unclear directionality** 

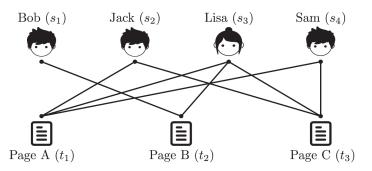


## Multilayer networks

- Same set of nodes
  - Individuals, countries, organizations etc
- Multiple/different sets of relations
  - Different types of relations among individuals (e.g. Breiger, Boorman, Arabie 1974)
  - Bilateral trade between countries, different commodities (e.g. Snyder & Kick 1979)
- Multiplex, Multi-relational, "tofts"
  - Attempt at generalization/formalization (Kivelä et al 2014)



(from Opsahl 2011)



(from Zhang et al 2023)

Type of	Меж-					Eve	NTS	IND I	PART	CIPA	TION	s			
MEMBERSHIP	BERS	1	2	3	4	5	6	7	8	9	10	11	12	13	14
Clique I:	(1	C	С	С	С	С	С	_	С	С					
-	2	llc	C	С	_	С	С	С	С	-					
Core	13	11-	C	C	C	C	C	C	C	С					
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.	1 75	Ш		P	P	P	_	P	_	-					
Primary 6	Ш		P	_	P	P	_	P	-						
	7	П				P	P	P	P	-					
Secondary .	8	П				_	S	-	S	S					
Clique II:	(o	Ш				S		S	S	S	_				
Secondary .	10	-	_	_	_	_		S	s	s	1		s		
	110							3	P	P	P	_	P		
Primary	112	1			1			_	P	P	P	_	P	P	P
-	13	1						_	ć	ć	c	_	ć	ć	c
Core		1			1		C	c c c	_	č	č	c	č	č	č
Cole	15	1					·	č	C	_	č	č	č	č	č
	16	1			1			-	š	s	Š	_	š	•	_
Secondary .	117	i							3	Š	_	S			
occonduity.	18									Š	_	Š			

Fig. 5.—Types of members of, and relationships between, two overlapping

(from Davis et al 1941)

#### Bipartite networks

#### A.k.a. 2-mode networks, affiliation networks

•Also N-mode and N-partite networks

#### Two sets of nodes / actors

- •Society ladies and social events (Davis et al 1941)
- •Interlocking directorates (directors on corporate boards)
- Authors and scientific papers
- •Company branches and cities (Taylor et al; GaWC papers)
- Hashtags and tweets

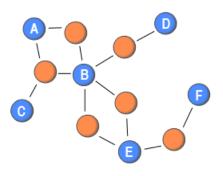
#### Relations only between these two sets

- •No relations within each set
- Possibility for many-to-many relations

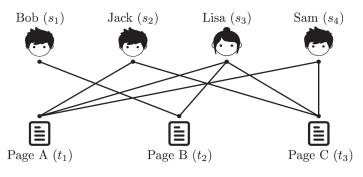
#### Ties typically binary and symmetric

#### Relations or a set of attributes (indicator variables)?

- •A paper has a set of authors
- •A social event is visited by a set of women
- •A woman attends a set of social events



(from Opsahl 2011)



(from Zhang et al 2023)

Type or	Меж-					Eve	NTS	und l	PART	CIPA	TION	s			
MEMBERSHIP	BERS	1	2	3	4	5	6	7	8	9	10	11	12	13	14
Clique I:	(1	С	С	С	С	С	С	_	С	С					
Core	2 3 4	c c	c c	CCC	cc	C C	CCC	CCC	CCC	c -					
Primary	5 6 7			P P	P -	P P P	P P	P - P	P P	-					
Secondary .	8	Ш				-	S		S	S					
Clique II: Secondary.	{9 10	L		_	_	S	=	S	S	S	_	_	s		
Primary	{11 12							-	P	P	P	-	P	P	P
Core	13 14 15						c	CCC	- C	c	CCC	c	CCC	CCC	CCC
Secondary.	16 17 18								S	S S	s - -	s s	S P C C C S		

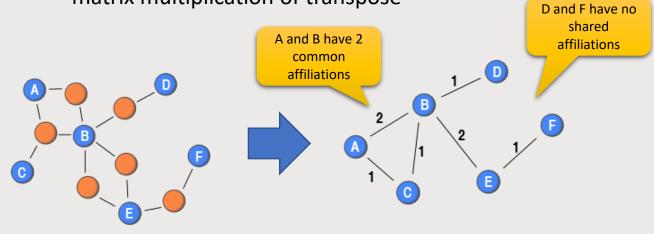
FIG. 5.—Types of members of, and relationships between, two overlapping cliques.

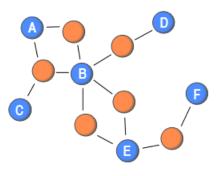
(from Davis et al 1941)

# Bipartite networks: methods and projections

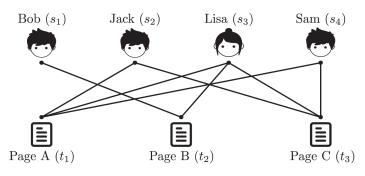
- Few methods for analyzing 2-mode networks
  - (though Borgatti & Everett 1997; Doreian et al 2004)
- Often projected: converted into 1-mode (unipartite) network

 Different projection method: classical approach by matrix multiplication of transpose





(from Opsahl 2011)



(from Zhang et al 2023)

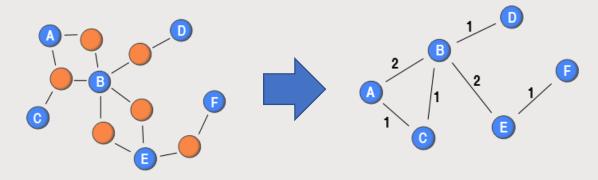
TYPE OF	Мем-					Eve	NTS /	IND I	ART	CIPA	TION	s			
MEMBERSHIP	BERS	1	2	3	4	5	6	7	8	9	10	11	12	13	14
Clique I:	(1	С	С	С	С	С	C	-	С	С					
Core	2 3	C -	C	C	c	C	C C	c c	C	- C					
	5	С	-	C P	C P	C P	С -	C P	С -	_					
Primary	67			P	-	P P	P P	- Р	P P	-					
Secondary .	8	Ш				-	S	-	S	S					
Clique II:	(o	11				S	_	S	S	S					
Secondary .	10	-		_	_	_		S	S	S	<u>'</u> -	-	s		
Primary	111							_	P P	P P	P P	_	P P	P	P
	13	l						C	C	C	C	-	С	С	C
Core							С	c	-	С	c	c	c	C	Č
	15							С	c	s	C	c	CCCS	С	С
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Fig. 5.—Types of members of, and relationships between, two overlappin diques.

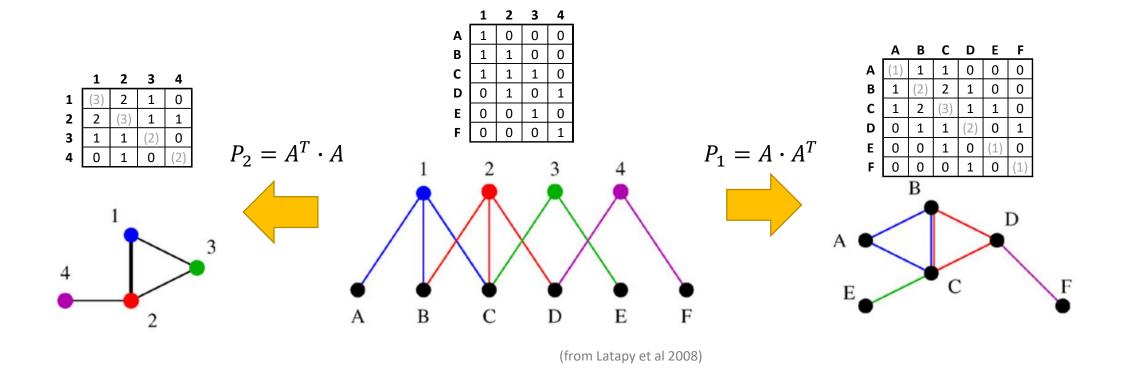
(from Davis et al 1941)

# • Edge inflation phenomena • Null models recommended (simulation)

# Bipartite networks: methods and projections



- Projections must make theoretical sense!
  - Peter networks (slightly different projection) does not
- Ladies at social events (Davis et al 1941)
  - Assumption of social exposure at events: feasible
  - Projected network: valued symmetrical number of shared affiliations
  - We are not observing that individuals interact, but we can identify which individuals that are (and are not) exposed to each other
  - Could be dichotomized as deemed fit (minimum number of shared events/exposure to infer a social tie/exposure)



# Bipartite networks: methods and projections

- Bipartite projections have directionality!
  - How actors A-F affiliates with 1-4: network of relations between A-F
  - How affiliations 1-4 share actors: a network of relations between 1-4
- Southern ladies-event data:
  - Network between ladies, capturing number of shared events
  - Network between events, capturing number of shared ladies

# Getting network data

#### Sociometric surveys

- Collect ego networks of each individual (name generators)
- Merge all ego networks into larger network



#### Snowball sampling

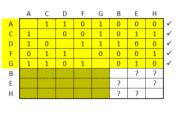
- Initial study population (zone 1)
- New actors mentioned (next zone)
- Query new actors
- Prune outer layer (no info about their ties)



- Interactions within individual school classes feasible
- Assuming inter-class relations can be ignored
- Full-population typically needed

#### Databases and digital trace data

- Email log files
- Social media ties (1- and 2-mode)
- Employment roster
- Transportation networks



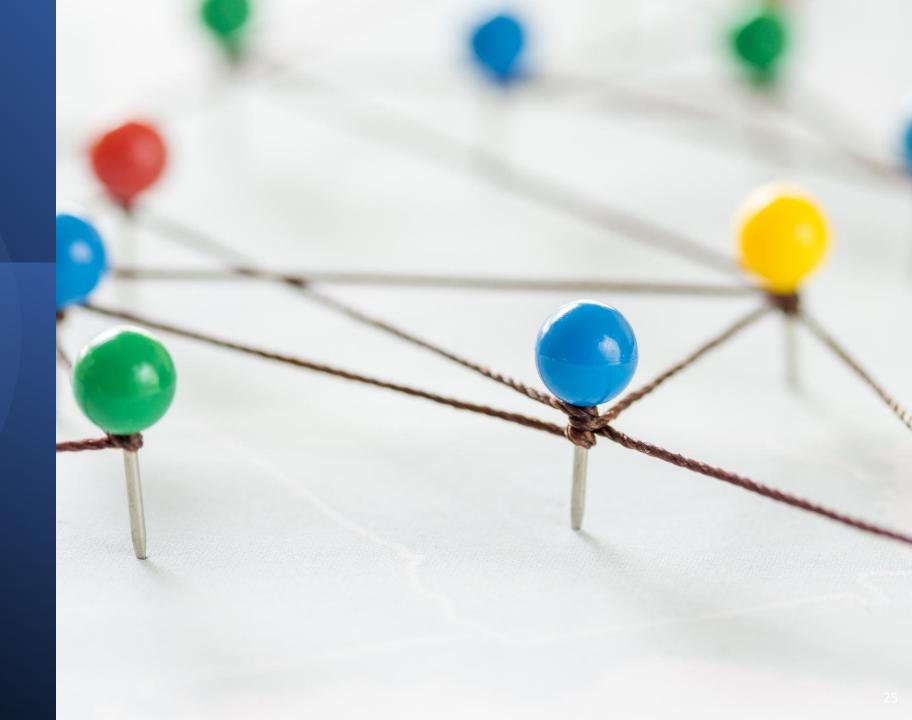
(Grandjean 2015)



(Kelly & Etling 2008)

Network metrics and methods

(Descriptive only)



#### Network metrics and methods





#### Micro-level

• Structural properties of individual actors



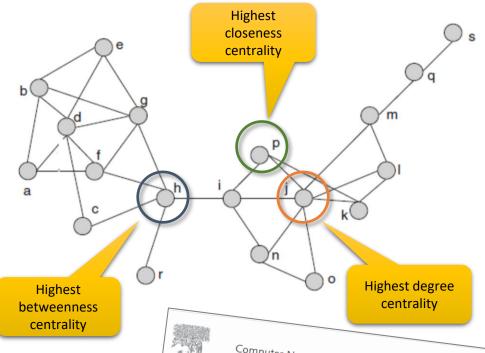
#### Meso-level

 Properties and similarities of actor subsets



#### Macro-level

• Properties of the network as a whole



Katz centrality
 Extension of degree

centrality (taking nonnearest neighbors into account)

PageRank

Extension of Katz centrality (adjusting an inflationary aspect of Katz)

# Computer Networks and ISDN Systems Volume 30, Issues 1-7, April 1998, Pages 107-117 The anatomy of a large-scale hypertextual Web Sergey Brin S., Lawrence Page R S B Show more In this paper, we present Google, a prototype of a large-scale search engine which anakes heavy use of the structure present in hypertext. Google is designed to crawl existing systems. The prototype with a full text and hyperlink database of at least 24

## Centrality

#### Degree centrality

• Number of ties that an actor is connected to

#### Betweenness centrality

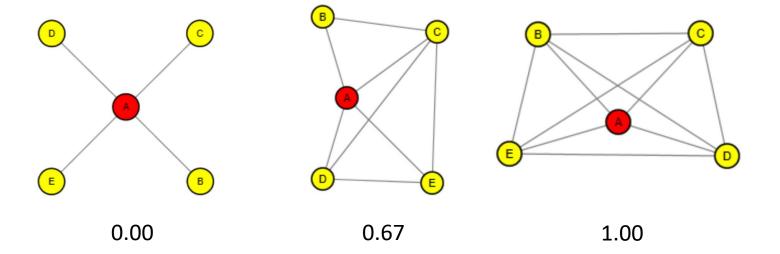
- How "between" an actor is
- Number of shortest paths between all pairs of actors that passes through an actor

#### Closeness centrality

- How "close" an actor is to all others
- Sum of shortest path from an actor to all other actors

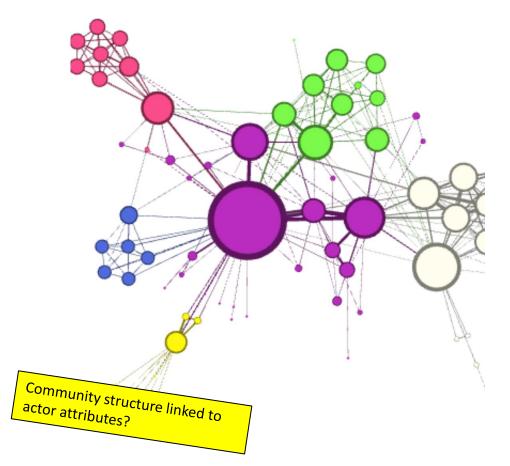
# Clustering coefficient

- How connected are my alters?
- Density of alter-alter ties in an ego-network



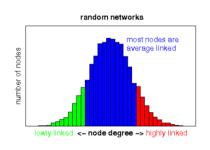
## Cohesive Subgroups (communities)

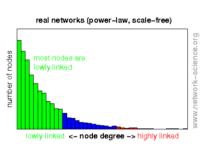
- Group actors in a network based on these having relatively more ties with each other than with other non-group actors
- Multiple different heuristics
  - Girvan-Newman
  - Clique overlap
  - Cores / k-Cores / k-Plex / Factions etc (see, e.g., Wasserman & Faust 1994)
- Girvan-Newman algorithm (2002)
  - Identify highest 'edge-betweenness'
  - Remove that edge
  - Calculate modularity (goodness-of-fit measure of community structures)
  - Repeat (recalculate edge betweenness)

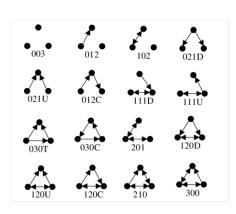


# Macro-level metrics

- Properties of the network as a whole
  - Nbr of (disconnected) components
  - Density (existing/possible ties)
  - Diameter (longest shortest-path)
  - Reciprocity
- Centralization
  - Average and distribution of nodal centralities
- Triad census







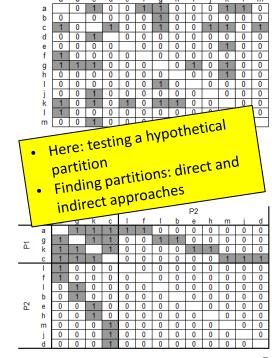
## Role-analysis (blockmodeling)

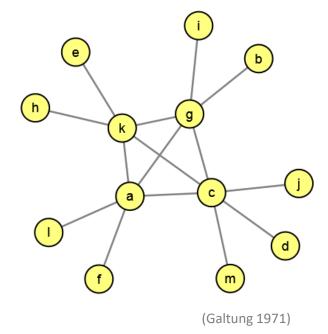
- Given a rich, complex network of (social) relations:
- Identifying roles in networks
  - Partition actors based on relational similarities
  - Formal way to capture notion of "social role" (Harrison White 1970s)
- Hospital example: patients, doctors, nurses, admin
  - Doctors interact with other doctors, and patients
  - Nurses interact with doctors, patients and admin
  - Admin interact with patients
  - Patients interact with all, except other patients
- More complex relational patterns
  - Beyond community detection
  - Core-periphery, transitive, hierarchy
  - "Custom" roles and structures

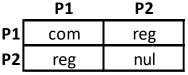


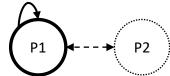
## Role-analysis (blockmodeling)

- Classical core-periphery structure
  - Seemingly two types of actors
- Core actors
  - Connected with several other core actors
  - Connected with a subset of peripheral actors
- Peripheral actors
  - NOT connected with other peripheral actors
  - Connected to singular core actors
- Re-shuffling original sociomatrix
  - According to our hypothetical separation
- Identifying blocks
  - Representing relational patterns within and between equivalent actors



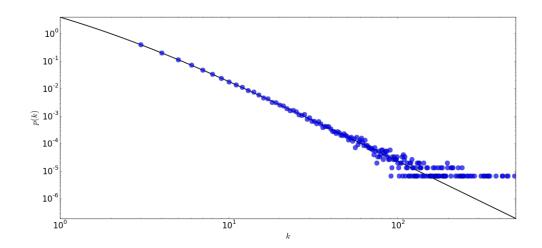






## Ideas about network dynamics

- Assortativity/homophily
  - Actors with similar attributes more likely to form connections (e.g. McPherson 2001)
  - Typically yields community structures
- Preferential attachment
  - High-degree actors more likely to connect with new actors
  - Associated with degree distribution following a power law
- Grand Unifying Network Theory
  - Certain dynamics and mechanisms that exist in all (or most) types of networks (cf. Brandes et al 2013)



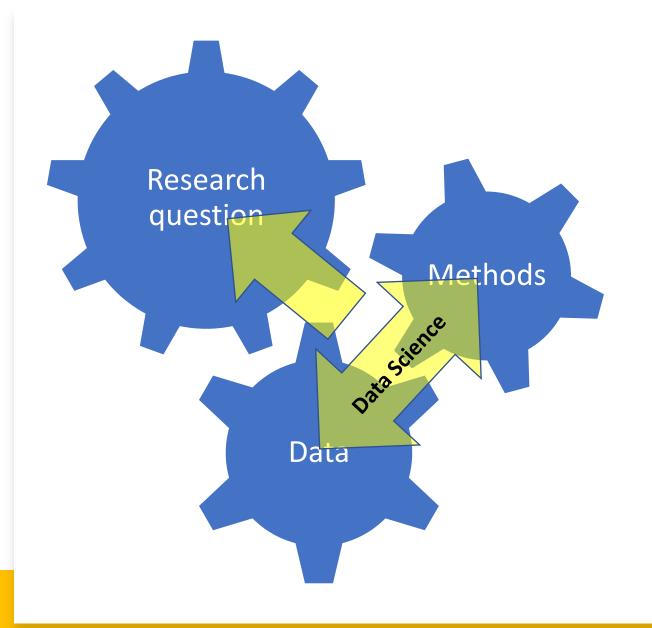
- Plethora of ways to describe/define what CSS is and how it relates to
  - Quantitative social-science at large
  - Data science
- This conceptual pluralism likely good for now
  - Emerging field
- Possible distinction between CSS and Data Science concerning the triad between
  - Research question (including theory)
  - Data
  - Methods



- In CSS, we tend to start off with the RQ cog
- Building on previous research, we formulate RQs of social-scientific and/or societal relevance
  - Is GDP growth linked to positionality in trade networks?
  - Are private schools better than public?
  - Are inter-ethnic families happier than endogamic ones?
- To address these: pair up methods with data
- Circling back to RQ at the end



- Postulating that data science is more exploratory
- Given (typically large and complex) datasets
  - More exploratory, open-minded approach
  - Apply methods to prune out insights data
- Although general topic area given by the data
  - Perhaps more open to *finding* signals
  - Seed to an interesting research question
- Formulating question (or topic)
- Connecting with previous research



- Ethnographic cycle (Gladwin 1989)
  - 1. Ask ethnographic questions
  - 2. Collect data
  - 3. Analyze data
  - Discover better question (repeat from 1)
- In context of CSS (and SNA)
  - 1. Research question
  - 2. Database, scraping, wrangling
  - 3. Methods and analysis
  - Discover better questions (repeat from 1)

