

# Universidad de las Fuerzas Armadas ESPE-L

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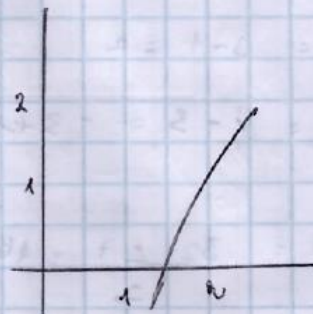
Fecha: 30-11-2021

En las siguientes ejercicios realizar 5 iteraciones con los métodos de la búsqueda Regla Falsa, Newton Raphson, la secante y Muller, tabular los resultados en cada caso y realizar una comparativa del comportamiento de error

1. Determine la raíz real de  $\ln(x^2) = 0.7$

Método Bisección

Iteración	$X_p$	$X_s$	$X_r$	Error
1	1	2	1.5	100%
2	1	1.5	1.25	20%
3	1.25	1.5	1.375	9.09%
4	1.375	1.5	1.4375	4.35%
5	1.375	1.4375	1.40625	2.27%
6	1.40625	1.4375	1.421875	1.09%
7	1.40625	1.421875	1.414062	0.55%
8	1.414062	1.421875	1.417969	0.27%



Intervalo  $[1, 2]$

$$f(1) = \ln(1) - 0.7 = -0.7$$

$$f(2) = \ln(2^2) - 0.7 = 0.686294$$

$l_b = 1$

$r_b = 2$

$$X_r = \frac{X_l + X_r}{2} = \frac{1 + 2}{2} = \frac{3}{2} = 1.5$$

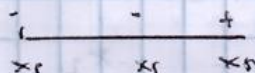
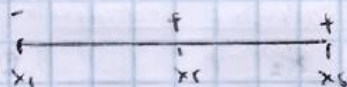
$$X_r = \frac{1.25 + 1.5}{2} = 1.25$$

$$e = \left| \frac{1.5 - 0}{1.5} \right| \cdot 100\% = 100\%$$

$$e = \left| \frac{1.25 - 1.5}{1.25} \right| \cdot 100\% = 20\%$$

$$f(1.5) = \ln(1.5^2) - 0.7 = 0.1109302$$

$$f(1.25) = \ln(1.25^2) - 0.7 = -0.258713$$



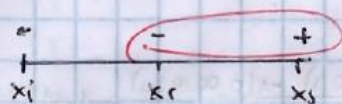


it=3

$$x_r = \frac{1,25 + 1,5}{2} = 1,375$$

$$e = \left| \frac{1,375 - 1,25}{1,375} \right| \cdot 100 = 9,09\%$$

$$f(1,375) = \ln(1,375) - 0,7 = -0,06309$$

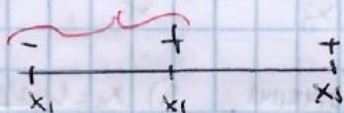


it=4

$$x_r = \frac{1,375 + 1,5}{2} = 1,4375$$

$$e = \left| \frac{1,4375 - 1,375}{1,4375} \right| \cdot 100 = 4,35\%$$

$$f(1,4375) = \ln(1,4375) - 0,7 = 0,026$$

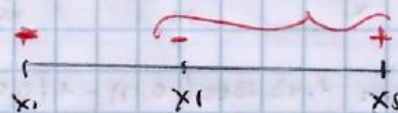


it=5

$$x_r = \frac{1,375 + 1,4375}{2} = 1,40625$$

$$e = \left| \frac{1,40625 - 1,4375}{1,40625} \right| \cdot 100 = 2,17\%$$

$$f(1,40625) = \ln(1,40625) - 0,7 = -0,018$$

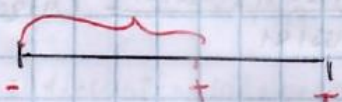


it=6

$$x_r = \frac{1,40625 + 1,4375}{2} = 1,421875$$

$$e = \left| \frac{1,421875 - 1,40625}{1,421875} \right| \cdot 100 = 1,09\%$$

$$f(1,421875) = 0,0039528$$

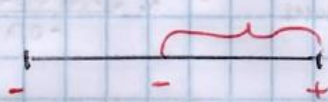


it=7

$$x_r = \frac{1,40625 + 1,421875}{2} = 1,4140625$$

$$e = \left| \frac{1,4140625 - 1,421875}{1,4140625} \right| \cdot 100 = 0,55\%$$

$$f(1,4140625) = -0,007066$$



$$x_r = \frac{1,4140625 + 1,421875}{2} = 1,41796875$$

$$e = \left| \frac{1,41796875 - 1,4140625}{1,41796875} \right| \cdot 100 = 0,27\%$$

$$f(1,41796875) = 0,001349$$

2 Regla Falsa

Iteración	$x_1$	$x_2$	$x_r$	Error %
1	1	2	1,504943	100%
2	1	1,502943	1,432312	5,07%
3	1	1,432362	1,421142	0,79%
4	1	1,421142	1,41922	0,12%
5	1	1,419292	1,41919	0,019%
6	1	1,419118	1,419071	0,003%
7	1	1,419071	1,419064	0,0004%
8	1	1,419064	1,419063	0,000033%

Intervalo [1,2]

$$f(x) = -0,7$$

$$f(2) = 0,686244$$



$$1) x_r = \frac{x_s(f(x_0) - x_0 f(x_s))}{f(x_0) - f(x_s)}$$

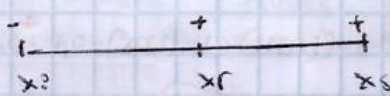
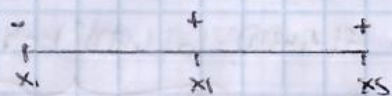
$$2) x_r = \frac{1,504443(-0,7) - (1)(0,1)(0,117510)}{(-0,17) - (0,117510)} = 1,432362$$

$$e = \left| \frac{1,504443 - 0}{1,504443} \right| \cdot 100 = 100\%$$

$$e = \left| \frac{1,432362 - 1,504443}{1,432362} \right| \cdot 100 = 5,06\%$$

$$f(x_i) = 0,117510$$

$$f(x_r) = 0,01865$$



$$3) x_r = \frac{1,432362(-0,17) - 1(0,01865)}{-0,7 - 0,01865} = 1,421141$$

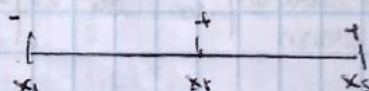
$$4) x_r = \frac{1,421141(-0,7) - 1(0,002920)}{-0,7 - 0,002920} = 1,419342$$

$$e = \left| \frac{1,421141 - 1,432362}{1,421141} \right| \cdot 100 = 0,78\%$$

$$e = \left| \frac{1,419342 - 1,421141}{1,419342} \right| \cdot 100 = 0,12\%$$

$$f(x_i) = 0,002920$$

$$f(x_r) = 0,000457$$



$$5) x_r = \frac{1,41932(-0,17) - 1(0,000457)}{-0,7 - 0,000457} = 1,419118$$

$$6) x_r = \frac{1,419118(-0,7) - 1(7,135191)}{-0,7 - 7,135191} = 1,419007$$

$$e = \left| \frac{1,419118 - 1,41932}{1,419118} \right| \cdot 100 = 0,014\%$$

$$e = \left| \frac{1,419074 - 1,419118}{1,419074} \right| \cdot 100 = 0,003\%$$

$$f(x_i) = 0,0000711$$

$$7) x_r = \frac{1,419075(0,7) - (1)(1,14869)}{-0,7 - 1,14869} = 1,419068$$

$$8) x_r = \frac{1,419068(-0,7) - 1(1,740040)}{-0,7 - 1,740040} = 1,419067$$

$$e = \frac{1,419068 - 1,419075}{1,419068} = 0,0004\%$$

$$e = \frac{1,419067 - 1,419069}{1,419067} = 0,000015\%$$



## Método Newton-Raphson

Iteración	$x_i$	$x_{i+1}$	Error	$f(x) = \ln(x^2) - 0.7$ $f'(x) = \frac{2x}{x^2} = \frac{2}{x}$
1	2	1.313706	52.24%	Punto = $x_0 = 2$
2	1.313706	1.415056	7.16%	
3	1.415056	1.419062	0.282%	
4	1.419062	1.419068	0.0004%	
5	1.419068	1.419068	0.000035%	
6	1.419068	1.419068	0%	
7	1.419068	1.419068	0%	
8	1.419068	1.419068	0%	

- 1)  $x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)}$   
 $x_2 = 2 - \frac{\ln(2^2) - 0.7}{2/2} = 1.313706$   
 $e = \left| \frac{1.313706 - 2}{1.313706} \right| \cdot 100 = 52.24\%$
- 2)  $x_3 = 1.313706 - \frac{\ln(1.313706^2) - 0.7}{2/1.313706} = 1.415056$   
 $e = \left| \frac{1.415056 - 1.313706}{1.415056} \right| \cdot 100 = 7.16\%$
- 3)  $x_4 = 1.415056 - \frac{\ln(1.415056^2) - 0.7}{2/1.415056} = 1.419062$   
 $e = \left| \frac{1.419062 - 1.415056}{1.419062} \right| \cdot 100 = 0.282\%$
- 4)  $x_5 = 1.419062 - \frac{\ln(1.419062^2) - 0.7}{2/1.419062} = 1.419068$   
 $e = \left| \frac{1.419068 - 1.419062}{1.419068} \right| \cdot 100 = 0.0004\%$
- 5)  $x_6 = 1.419068 - \frac{\ln(1.419068^2) - 0.7}{2/1.419068} = 1.419068$   
 $e = \left| \frac{1.419068 - 1.419068}{1.419068} \right| \cdot 100 = 0.000035\%$
- 6)  $x_7 = 1.419068 - \frac{\ln(1.419068^2) - 0.7}{2/1.419068} = 1.419068$   
 $e = \left| \frac{1.419068 - 1.419068}{1.419068} \right| \cdot 100 = 0\%$
- 7)  $x_8 = 1.419068 - \frac{\ln(1.419068^2) - 0.7}{2/1.419068} = 1.419068$   
 $e = \left| \frac{1.419068 - 1.419068}{1.419068} \right| \cdot 100 = 0\%$
- 8)  $x_9 = 1.419068 - \frac{\ln(1.419068^2) - 0.7}{2/1.419068} = 1.419068$   
 $e = \left| \frac{1.419068 - 1.419068}{1.419068} \right| \cdot 100 = 0\%$

## Método de la Secante

Iteración	$x_i$	$x_{i-1}$	$x_{i+1}$	Error	Intervalo [1, 2]
1	2	1	1.504443	52.40%	
2	1.504443	2	1.402663	7.29%	
3	1.402663	1.504443	1.419560	1.19%	
4	1.419560	1.402663	1.419070	0.051%	
5	1.419070	1.419560	1.419068	0.00018%	
6	1.419068	1.419070	1.419068	3.48 $\times 10^{-8}$	
7	1.419068	1.419068	1.419068	4.64 $\times 10^{-14}$	



8                      1,419063                      1,419663                      1,41463                      0%

$$1) \quad x_{i+1} = \frac{x_i f(x_i) - x_{i-1} f(x_i)}{f(x_{i+1}) - f(x_i)} = \frac{2(\ln(1) - 0,7) - 1(\ln(0,4) - 0,7)}{\ln(1) - 0,7 - (\ln(0,4) - 0,7)} = 1,504443$$

$$e = \left| \frac{1,504443 - 2}{1,504443} \right| \cdot 100 = 32,90\%$$

$$2) \quad x_3 = \frac{1,504443(\ln(\frac{1}{2}) - 0,7) - 2(\ln(1,504443^2) - 0,7)}{\ln(\frac{1}{2}) - 0,7 - (\ln(1,504443^2) - 0,7)} = 1,402665$$

$$e = \left| \frac{1,402665 - 1,504443}{1,402665} \right| \cdot 100 = 7,29\%$$

$$3) \quad x_4 = \frac{1,402665(\ln(1,504443^2) - 0,7) - 1,504443(\ln(1,402665^2) - 0,7)}{\ln(1,504443^2) - 0,7 - (\ln(1,402665^2) - 0,7)} = 1,419560$$

$$e = \left| \frac{1,419560 - 1,402665}{1,419560} \right| \cdot 100 = 1,19\%$$

$$4) \quad x_5 = \frac{1,419560(\ln(1,402665) - 0,7) - 1,402665(\ln(1,419560^2) - 0,7)}{\ln(1,402665) - 0,7 - (\ln(1,419560^2) - 0,7)}$$

$$e = \left| \frac{1,419670 - 1,419560}{1,419670} \right| \cdot 100 = 0,05\%$$

$$5) \quad x_6 = \frac{1,419670(\ln(1,419560^2) - 0,7) - 1,419560(\ln(1,419670^2) - 0,7)}{\ln(1,419560^2) - 0,7 - \ln(1,419670^2) - 0,7} = 1,419063$$

$$e = \left| \frac{1,419063 - 1,419670}{1,419063} \right| \cdot 100 = 0,0043\%$$

$$6) \quad x_7 = \frac{1,419063(4,07338) \times 10^{-6} - 1,419070(-6,971425)}{4,073380 \times 10^{-6} - (-6,971425 \times 10^{-10})} = 1,419067$$

$$e = \frac{-6,661338 \times 10^{-14} - 4,694163}{-6,661338 \times 10^{-14}} = 0\%$$

$$7) \quad x_8 = \frac{1,419067(-6,971425 \times 10^{-10}) - 1,419067(7,771561 \times 10^{-10})}{-6,971425 \times 10^{-10} - 7,771561 \times 10^{-10}} = 1,419067$$

$$e = \frac{-6,661338 \times 10^{-14} - 4,694163 \times 10^{-14}}{-6,661338 \times 10^{-14}} = 0\%$$



$$8) \quad x_1 = \frac{1,419067 (2.771561 \times 10^{-16}) - 1,419067 (-1,110223 \times 10^{-16})}{2.771561 \times 10^{-16} - (-1,110223 \times 10^{-16})} = 1,419067$$

$$e = \left| \frac{1,41967 - 1,419067}{1,41967} \right| \times 100 = 0\%$$

Miller

iteration	$x_0$	$x_1$	$x_2$	$x_3$	Error %
1	1	1,5	2	1,422084	40,64%
2	1,5	2	1,422084	1,419610	0,2142%
3	2	1,422084	1,419610	1,419068	0,0027%
4	1,422084	1,419068	1,419068	1,419068	0%
5					
6					
7					
8					

$$1) \quad h_0 = x_1 - x_0 = 1,5 - 1 = 0,5$$

$$h_1 = x_2 - x_1 = 2 - 1,5 = 0,5$$

$$f(x_0) = m(1)^2 - 0,7 = -0,7$$

$$f(x_1) = m(1,5)^2 - 0,7 = 0,110430$$

$$f(x_2) = m(2)^2 - 0,7 = 0,686294$$

$$d_0 = \frac{f(x_1) - f(x_0)}{h_0} = \frac{0,110430 - (-0,7)}{0,5} = 1,62186$$

$$d_1 = \frac{f(x_2) - f(x_1)}{h_1} = \frac{0,686294 - 0,110430}{0,5} = 1,150728$$

$$a = \frac{d_1 - d_0}{h_1 - h_0} = \frac{1,150728 - 1,62186}{0,5 - 0,5} = -0,471132$$

$$b = ah_1 + d_1 = (-0,471132)(0,5) + 1,150728 = 0,913622$$

$$c = 0,686294$$

$$x_3 = x_2 - \frac{2c}{b^2 (0,999999) \sqrt{b^2 - 4ac}} = 2 - \frac{2(0,686294)}{0,913622^2 \sqrt{0,913622^2 - 4(-0,471132)(0,686294)}}$$

$$x_3 = 1,422084$$

$$x_0 = 1,5$$

$$x_1 = 2$$

$$x_2 = 1,422084$$

$$e = \left| \frac{x_3 - x_2}{x_3} \right| = \left| \frac{1,422084 - 2}{1,422084} \right| \times 100 = 40,64\%$$



$$2) \quad h_0 = 2 - 1.5 = 0.5$$

$$h_1 = 1.422084 - 2 = -0.577911$$

$$f(x_0) = 0.110430$$

$$f(x_1) = 0.686294$$

$$f(x_2) = \ln(1.422084^2) - 0.7 = 0.004234$$

$$d_0 = \frac{0.686294 - 0.110430}{0.5} = 1.00728$$

$$a = \frac{1.80182 - 1.10728}{-0.577911 + 0.5} = -0.578047$$

$$d_1 = \frac{0.004234 - 0.686294}{-0.577911} = 1.180182$$

$$b = -0.578047(-0.577911) + 1.180182 = 1.34866$$

$$c = 0.004234$$

$$x_3 = 1.422084 - \frac{2(0.004234)}{1.34866 + \sqrt{1.34866^2 - 4(-0.578047)(0.004234)}}$$

$$x_3 = 1.419030$$

$$x_0 = 2$$

$$x_1 = 1.422084$$

$$x_2 = 1.419050$$

$$e = \left| \frac{1.419030 - 1.422084}{1.4190} \right| \cdot 100 = 0.2142\%$$

$$3) \quad h_0 = 1.422084 - 2 = -0.577911$$

$$h_1 = 1.419030 - 1.422084 = -0.003054$$

$$f(x_0) = 0.686294$$

$$f(x_1) = f(1.422) = 0.604230$$

$$f(x_2) = f(1.4144) = \ln(1.4144030^2) - 0.7 = -0.000025$$

$$d_0 = \frac{0.604234 - 0.686294}{-0.577911} = 1.180182$$

$$a = \frac{1.408029 - 1.180182}{-0.003054 - 0.577911} = -0.312128$$

$$d_1 = \frac{-0.000025 - 0.604234}{-0.003054} = 1.408029$$

$$b = -0.312128(-0.003054) + 1.408029 = 1.409221$$

$$c = -0.000025$$

$$x_3 = 1.419030 - \frac{2(-0.000025)}{1.409221 + \sqrt{1.409221^2 - 4(-0.312128)(-0.000025)}}$$

$$x_3 = 1.419068$$

$$e = \left| \frac{1.419068 - 1.419030}{1.419068} \right| \cdot 100 = 0.00127\%$$



$$\begin{aligned} 4) \quad h_0 &= 1,419050 - 1,419084 = -0,000034 & f(x_0) &= f(1,412) = 0,004254 \\ h_1 &= 1,419068 - 1,419050 = 0,000018 & f(x_1) &= f(1,414) = 0,000025 \\ & & f(x_2) &= f(1,419068) = 0,000006 \end{aligned}$$

$$d_0 = \frac{-0,000025 - 0,004254}{-0,000034} = 1,408024$$

$$d_1 = \frac{0,00000006 + 0,000025}{0,000018} = 1,422222$$

$$a = \frac{1,422222 - 1,408024}{0,000018 - 0,000034} = -4,648113$$

$$b = -4,648113(0,000018) + 1,422222 = 1,442137$$

$$c = 0,0000006$$

$$x_2 = 1,419068 - \frac{2(0,0000006)}{1,422137 + \sqrt{1,422137^2 - 4(-4,648113)(0,0000006)}}$$

$$x_3 = 1,419068$$

$$e = \left| \frac{1,419068 - 1,419068}{1,419068} \right|, \text{ wo } = 0,$$



2) La velocidad  $v$  de un paracaidista que cae esta dada por:  $N = \frac{g}{c} (1 - e^{-\frac{c}{m}t})$

donde  $g = 9.8 \text{ m/s}^2$ , Era un paracaidista con coeficiente de arrastre de  $c = 15 \text{ kg/s}$

calcular la masa  $m$  de modo que la velocidad sea  $v = 35 \text{ m/s}$  en  $t = 9 \text{ s}$

$$35 = \frac{9.8}{15} m (1 - e^{-15 \cdot 9 / m})$$

$$f(m) = \frac{9.8}{15} m (1 - e^{-135/m}) - 35$$

### • Método Bisección

Iteración	$x_i$	$x_s$	$x_r$	Error %
1	50	60	55	100%
2	55	60	57.5	4.35%
3	57.5	60	58.75	2.13%
4	58.75	60	59.375	1.05%
5	59.375	60	59.6875	0.52%

$$f(50) = \frac{9.8(50)}{15} (1 - e^{-\frac{135}{50}}) - 35$$

$$f(50) = -4.528113$$

$$f(60) = \frac{9.8(60)}{15} (1 - e^{-\frac{135}{60}}) - 35$$

$$f(60) = 0.062350$$

$$① x_r = \frac{50+60}{2} = 55$$

$$e = \left| \frac{55-50}{55} \right| \cdot 100 = 9.09\%$$

$$f(55) = \frac{9.8(55)}{15} (1 - e^{-\frac{135}{55}}) - 35 = -2.153420$$



$$② x_r = \frac{55+60}{2} = 57.5$$

$$e = \left| \frac{57.5-55}{57.5} \right| \cdot 100 = 4.35\%$$

$$f(57.5) = \frac{9.8(57.5)}{15} (1 - e^{-\frac{135}{57.5}}) - 35 = -1.023832$$



$$③ x_r = \frac{57.5+60}{2} = 58.75$$

$$e = \left| \frac{58.75-57.5}{58.75} \right| \cdot 100 = 2.13\%$$

$$f(58.75) = \frac{9.8(58.75)}{15} (1 - e^{-\frac{135}{58.75}}) - 35 = -0.475132$$



$$④ x_r = \frac{58.75+60}{2} = 59.375$$

$$e = \left| \frac{59.375-58.75}{59.375} \right| \cdot 100 = 1.05\%$$

$$f(59.375) = \frac{9.8(59.375)}{15} (1 - e^{-\frac{135}{59.375}}) - 35 = -0.201247$$



$$⑤ x_r = \frac{59.375+60}{2} = 59.6875$$

$$e = \left| \frac{59.6875-59.375}{59.6875} \right| \cdot 100 = 0.52\%$$



# Método de la Regla Falsa

Iteración	$x_1$	$x_2$	$x_r$	$f(x_1)$	$f(x_2)$	$f(x_r)$	Error %
1	50	60	59,851317	-4,528713	0,062350	0,004422	100 %
2	50	59,851317	59,841708	-4,528713	0,004422	0,000286	0,016 %
3	50	59,841708	59,841087	-4,528713	0,000286	0,000018	0,001 %
4	50	59,841087	59,841047	-4,528713	0,000018	0,0000012	0,00006 %
5	50	59,841047	59,841045	-4,528713	0,0000012	0,00000008	0,000004 %

$$f(x_1) = f(50) = -4,528713$$

$$f(x_2) = f(60) = 0,062350$$

$$(1) x_r = \frac{60(-4,528713) - 50(0,062350)}{-4,528713 - 0,062350} = 59,851317$$

$$e = \left| \frac{59,851317 - 0}{59,851317} \right| \cdot 100 = 100\%$$

$$f(59,851317) = 0,004422$$



$$(2) x_r = \frac{59,851317(-4,528713) - 50(0,004422)}{-4,528713 - 0,004422} = 59,841708$$

$$e = \left| \frac{59,841708 - 59,851317}{59,841708} \right| \cdot 100 = 0,016\%$$

$$f(59,841708) = 0,000286$$



$$(3) x_r = \frac{59,841708(-4,528713) - 50(0,000286)}{-4,528713 - 0,000286} = 59,841087$$

$$e = \left| \frac{59,841087 - 59,841708}{59,841087} \right| \cdot 100 = 0,001\%$$

$$f(59,841087) = 0,000018$$



$$(4) x_r = \frac{59,841087(-4,528713) - 50(0,000018)}{-4,528713 - 0,000018} = 59,841047$$

$$e = \left| \frac{59,841047 - 59,841087}{59,841047} \right| \cdot 100 = 0,00006\%$$

$$f(59,841047) = 0,0000012$$



$$(5) x_r = \frac{59,841047(-4,528713) - 50(0,0000012)}{-4,528713 - 0,0000012} = 59,841045$$

$$e = \left| \frac{59,841045 - 59,841047}{59,841045} \right| \cdot 100 = 0,000004\%$$

$$f(59,841045) = 0,00000008$$





# Método Newton Raphson

iteración	$x_i$	$x_{i+1}$	Error %	$f(m) = \frac{9.8}{15} m (1 - e^{-\frac{135}{m}}) - 35$	
1	50	59,225803	15,58%		1
2	59,225803	59,838495	1,02%		2
3	59,838495	59,841046	0,0043%		3
4	59,841046	59,841045	0,000002%		4
5	59,841045	59,841044	0,0000017%		5

①  $i=1$

$$f(50) = \frac{9.8}{15} (50) \left(1 - e^{-\frac{135}{50}}\right) - 35 = -0,490875$$

$$f'(50) = \frac{9.8}{15} \left( \frac{49(50) + 6615}{75(50)} \right) e^{-\frac{135}{50}} = 0,434055$$

$$x_2 = 50 - \frac{-0,490875}{0,434055} = 59,225803$$

$$e = \left| \frac{59,225803 - 50}{59,225803} \right| = 15,58\%$$

②  $i=2$

$$f(59,225803) = \frac{9.8}{15} (59,225803) \left(1 - e^{-\frac{135}{59,225803}}\right) - 35 = -0,265942$$

$$f'(59,225803) = \frac{9.8}{15} \left( \frac{49(59,225803) + 6615}{75(59,225803)} \right) e^{-\frac{135}{59,225803}} = 0,434055$$

$$x_3 = 59,225803 - \frac{-0,265942}{0,434055} = 59,838495$$

$$e = \left| \frac{59,838495 - 59,225803}{59,838495} \right| = 1,02\%$$

③  $i=3$

$$f(59,838495) = \frac{9.8}{15} (59,838495) \left(1 - e^{-\frac{135}{59,838495}}\right) - 35 = -0,001098$$

$$f'(59,838495) = \frac{9.8}{15} \left( \frac{49(59,838495) + 6615}{75(59,838495)} \right) e^{-\frac{135}{59,838495}} = 0,430475$$

$$x_4 = 59,838495 - \frac{-0,001098}{0,430475} = 59,841046$$

$$e = \left| \frac{59,841046 - 59,838495}{59,841046} \right| = 0,0043\%$$

④  $i=4$

$$f(59,841046) = \frac{9.8}{15} (59,841046) \left(1 - e^{-\frac{135}{59,841046}}\right) - 35 = 0,0000005$$

$$f'(59,841046) = \frac{9.8}{15} \left( \frac{49(59,841046) + 6615}{75(59,841046)} \right) e^{-\frac{135}{59,841046}} = 0,430460$$

$$x_5 = 59,841046 - \frac{0,0000005}{0,430460} = 59,841045$$

$$e = \left| \frac{59,841045 - 59,841046}{59,841045} \right| = 0,000002\%$$

⑤  $i=5$

$$f(59,841045) = \frac{9.8}{15} (59,841045) \left(1 - e^{-\frac{135}{59,841045}}\right) - 35 = 0,000000108$$

$$f'(59,841045) = \frac{9.8}{15} \left( \frac{49(59,841045) + 6615}{75(59,841045)} \right) e^{-\frac{135}{59,841045}} = -0,134923$$

$$x_6 = 59,841045 - \frac{0,000000108}{-0,134923} = 59,841044$$

$$e = \left| \frac{59,841044 - 59,841045}{59,841044} \right| = 0,0000017\%$$



## ◉ Método de la Secante

Iteración	$x_i$	$x_{i-1}$	$x_{i+1}$	Error %
1	60	50	59,85318	0,24%
2	59,85318	60	59,837100	0,024%
3	59,837100	59,85318	59,84025	0,005%
4	59,840250	59,837100	59,841045	0,001%
5	59,841045	59,840250	59,841045	0

$$f(50) = -4,528713$$

$$f(60) = 0,068350$$

①

$$x_2 = \frac{60(-4,528713) - 50(0,06835)}{-4,528713 - 0,06835} = 59,85318$$

$$e = \left| \frac{59,85318 - 60}{59,85318} \right| = 0,24\%$$

$$\textcircled{2} f(x_{i+1}) = f(59,85318) = \frac{9,8(59,85318)}{15} \left( 1 - e^{-\frac{135}{59,85318}} \right) - 35 = 0,005966$$

$$x_3 = \frac{59,85318(0,068350) - 60(0,005966)}{0,068350 - 0,005966} = 59,837100$$

$$e = \left| \frac{59,837100 - 59,85318}{59,837100} \right| \cdot 100 = 0,024\%$$

$$\textcircled{3} f(x_{i+1}) = f(59,837100) = \frac{9,8(59,837100)}{15} \left( 1 - e^{-\frac{135}{59,837100}} \right) - 35 = -0,001698$$

$$x_4 = \frac{59,837100(0,005966) - 59,85318(-0,001698)}{0,005966 + 0,001698} = 59,840250$$

$$e = \left| \frac{59,840250 - 59,837100}{59,840250} \right| \cdot 100 = 0,005\%$$

$$\textcircled{4} f(x_{i+1}) = f(59,840250) = \frac{9,8(59,840250)}{15} \left( 1 - e^{-\frac{135}{59,840250}} \right) - 35 = -0,000342$$

$$x_5 = \frac{59,840250(-0,001698) - 59,837100(-0,000342)}{-0,001698 + 0,000342} = 59,841045$$

$$e = \left| \frac{59,841045 - 59,840250}{59,841045} \right| = 0,001\%$$

$$\textcircled{5} f(x_{i+1}) = f(59,841045) = \frac{9,8(59,840250)}{15} \left( 1 - e^{-\frac{135}{59,841045}} \right) - 35 = -0,000000108$$

$$x_6 = \frac{59,841045(-0,000342) - 59,840250(-0,000000108)}{-0,000342 + 0,000000108} = 59,841045$$

$$e = \left| \frac{59,841045 - 59,841045}{59,841045} \right| \cdot 100 = 0$$



# Método de Möller

$$f(m) = \frac{9.8}{15} m (1 - e^{-\frac{135}{m}}) - 35$$

$$x_0 = 20$$

$$x_1 = 30$$

$$x_2 = 60$$

Iterac	$x_0$	$x_1$	$x_2$	$x_3$	Error %
1	20	30	60	59,844881	0,259%
2	30	60	59,844881	59,841045	0,0064%
3	60	59,844881	59,841045	59,841045	0%

$$\textcircled{1} h_0 = x_1 - x_0 = 30 - 20 = 10$$

$$h_1 = x_2 - x_1 = 60 - 30 = 30$$

$$f(20) = \frac{9.8}{15} (20) (1 - e^{-\frac{135}{20}}) - 35 = -21,948632$$

$$f(30) = \frac{9.8}{15} (30) (1 - e^{-\frac{135}{30}}) - 35 = -15,617736$$

$$f(60) = \frac{9.8}{15} (60) (1 - e^{-\frac{135}{60}}) - 35 = 0,068350$$

$$d_0 = \frac{f(x_1) - f(x_0)}{h_0} = \frac{-15,617736 - (-21,948632)}{10} = 0,630896$$

$$d_1 = \frac{f(x_2) - f(x_1)}{h_1} = \frac{0,068350 - (-15,617736)}{30} = 0,522869$$

$$a = \frac{d_1 - d_0}{h_1 - h_0} = \frac{0,522869 - 0,630896}{30 - 10} = -0,0027555$$

$$c = 0,068350$$

$$b = ah_1 + d_1 = -0,0027555(30) + 0,522869 = 0,440204$$

$$x_3 = x_2 - \frac{2c}{b \pm \sqrt{b^2 - 4ac}} = 60 - \frac{2(0,068350)}{0,440204 + \sqrt{0,440204^2 - 4(-0,0027555)(0,068350)}} = 59,844881$$

$$e = \left| \frac{59,844881 - 60}{59,844881} \right| \cdot 100 = 0,259\%$$

$$\textcircled{2} h_0 = 60 - 30 = 30$$

$$h_1 = 59,844881 - 60 = -0,155119$$

$$f(x_0) = f(30) = -15,617736$$

$$f(x_1) = f(60) = 0,068350$$

$$f(x_2) = f(59,844881) = \frac{9.8}{15} (59,844881) (1 - e^{-\frac{135}{59,844881}}) - 35 = 0,001651$$

$$d_0 = \frac{0,068350 - (-15,617736)}{30} = 0,522869$$

$$d_1 = \frac{0,001651 - 0,068350}{-0,155119} = 0,429986$$

$$a = \frac{0,429986 - 0,522869}{-0,155119 - 30} = -0,003112$$

$$c = 0,001651$$

$$b = -0,003112(-0,155119) + 0,429986 = 0,430469$$

$$x_3 = 59,844881 - \frac{2(0,001651)}{0,430469 + \sqrt{0,430469^2 - 4(-0,003112)(0,001651)}} = 59,841045$$

$$e = \left| \frac{59,841045 - 59,844881}{59,841045} \right| \cdot 100 = 0,0064\%$$



$$③ h_0 = -0,155119$$

$$h_1 = 59,844881 - 60 = -0,003836$$

$$d_0 = \frac{0,001651 - 0,068350}{-0,155119} = 0,429987$$

$$d_1 = \frac{1,239776 - 0,001651}{-0,003836} = 0,430449$$

$$a = \frac{0,430449 - 0,429987}{-0,003836 + 0,155119} = -0,002909$$

$$b = -0,002909(-0,003836) + 0,430449 = 0,430460$$

$$x_3 = 59,841045 - \frac{2(1,239776)}{0,430460 + \sqrt{0,430460^2 - 4(-0,002909)(1,239776)}} = 59,841045$$

$$e = \left| \frac{59,841045 - 59,841045}{59,841045} \right| \cdot 100 = 0 \quad \checkmark$$

$$f(x_0) = f(60) = 0,068350$$

$$f(x_1) = f(59,844881) = 0,001651$$

$$f(x_2) = f(59,841045) = \frac{9,8(59,841045)}{15} \left( 1 - e^{-\frac{13,5}{59,841045}} \right) - 35 = 1,239776$$

$$c = 1,239776$$