

lecture 25. Revision.

1- Eliminating Null Productions.

$$A \rightarrow \lambda.$$

$$S \rightarrow aA / b / bb / a.$$
~~$$A \rightarrow \lambda.$$~~

2- Removing UNIT Productions.

$$A \rightarrow B \rightarrow C \rightarrow D.$$

$$A \rightarrow \text{---}$$

$$A \rightarrow B$$

$$A \rightarrow a / bb / aA.$$

$$B \rightarrow a / bb / aC.$$

$$B \rightarrow a / bb / aA$$

$$D \rightarrow \text{---}$$

$$A \rightarrow B \rightarrow C \rightarrow \textcircled{A}.$$

Removing Useless Productions.

1- Non-Reachable:-

The production which can never take part in the derivation of any string.

Ex:- $A \rightarrow bc$

$$S \rightarrow a / B / aB.$$

$$B \rightarrow b$$

$$\boxed{A \rightarrow bc}.$$

→ Non Reachable.

2- Non-Terminating:-

A Variable (Non-Terminal) that can never take part in derivation of any string.

$$B \rightarrow bB.$$

$$bbB$$

$$bbbB$$

$$bbbbB$$

$$\vdots$$

$$\vdots$$

Ex: Remove all Useless Productions.

$$C \rightarrow aC / A / C$$

$$C \rightarrow a / b / C / \lambda.$$

Ex: Remove all useless productions.

$$S \rightarrow aS \mid A \mid \underline{C}$$

$$\begin{aligned} A &\rightarrow a \\ X B &\rightarrow aa \quad X. \\ * C &\rightarrow aCa * \end{aligned}$$

Step 1:- Non-Reachable.
X.

Step 2:- Non-Terminating.
*

$$\begin{aligned} S &\rightarrow C \rightarrow aCa \\ &\quad aaCa \\ &\quad aaaaCa \\ &\quad - \\ &\quad - \\ &\quad - \end{aligned}$$

$$\begin{aligned} S &\rightarrow aS \mid A \\ A &\rightarrow a \end{aligned}$$

CHOMSKY Normal Form (CNF).

A forms.

CFG is in CNF if every rule is ^{one} of the

1- $A \rightarrow BC.$

B & C are not starting Variables.

2- $A \rightarrow a$

3- $S \rightarrow \lambda.$

S is the starting Variable.

"How to Convert a CFG to CNF"

Step 1:- Introduce a New Rule $S_0 \rightarrow S.$

Step 2:- Remove all Null productions.

Step 3:- ϵ ϵ UNIT productions.

Step 4:- Add rules of the form $V_t \rightarrow t$
 $t \in \text{terminal}.$
 $V_t \in \text{Non-terminal}.$

$$\begin{aligned} B &\rightarrow a b a. \\ B &\rightarrow a \\ D &\rightarrow b. \\ B &\rightarrow C D C. \end{aligned}$$

Step 5:- Transform the remaining rules to the form
 $A \rightarrow BC.$

steps. Thus form the remaining rules to the form $A \rightarrow BC$.

$$\begin{aligned}
 V &\rightarrow A_1 A_2 A_3 A_4 A_5 \xrightarrow{X} B_1 A_3 A_4 A_5 \xrightarrow{X} B_2 A_4 A_5 \xrightarrow{V} B_3 A_5. \\
 B_1 &\rightarrow A_1 A_2 \checkmark \\
 B_2 &\rightarrow B_1 A_3 \checkmark \\
 B_3 &\rightarrow B_2 A_4 \checkmark.
 \end{aligned}$$

Ex:- $S \rightarrow CSC \mid B$ Terminals = $\{0, 1\}$.

$$\begin{aligned}
 C &\rightarrow 00 \mid \Lambda. \\
 B &\rightarrow 01B \mid 1.
 \end{aligned}$$

Step 1

$$\begin{aligned}
 S_0 &\rightarrow S. \\
 S &\rightarrow CSC \mid B \\
 C &\rightarrow 00 \mid \Lambda. \\
 B &\rightarrow 01B \mid 1.
 \end{aligned}$$

Step 2:-

$$\begin{aligned}
 S_0 &\rightarrow S. & C &\rightarrow \Lambda. \\
 S &\rightarrow CSC \mid B \mid SC \mid CS \mid S. \\
 C &\rightarrow 00 \mid \Lambda. \\
 B &\rightarrow 01B \mid 1.
 \end{aligned}$$

Step 3:-

$$\begin{aligned}
 S_0 &\rightarrow S. & S &\rightarrow B \\
 S &\rightarrow CSC \mid B \mid SC \mid CS \mid S. & B &\rightarrow \\
 C &\rightarrow 00 & A &\rightarrow B \rightarrow C \rightarrow A \\
 B &\rightarrow 01B \mid 1.
 \end{aligned}$$

$$\begin{aligned}
 S_0 &\rightarrow CSC \mid 01B \mid 1 \mid SC \mid CS \\
 S &\rightarrow CSC \mid 01B \mid 1 \mid SC \mid CS \\
 C &\rightarrow 00 \\
 B &\rightarrow 01B \mid 1.
 \end{aligned}$$

Step 4:- Create $V_t \rightarrow t$ for every t .

$$\begin{aligned}
 S_0 &\rightarrow CSC \mid 01B \mid 1 \mid SC \mid CS \\
 S &\rightarrow CSC \mid 01B \mid 1 \mid SC \mid CS
 \end{aligned}$$

$$\begin{aligned}
 C &\rightarrow \cancel{z} \cancel{z} \\
 B &\rightarrow z \cancel{0} 1 B \mid 1. \\
 z &\rightarrow 0
 \end{aligned}$$

$$A \rightarrow a.$$

$$\begin{aligned}
 S_0 &\rightarrow CSC \mid ZAB \mid 1 \mid SC \mid CS \\
 S &\rightarrow CSC \mid ZAB \mid 1 \mid SC \mid CS \\
 C &\rightarrow ZZ \\
 B &\rightarrow ZAB \mid 1. \\
 z &\rightarrow 0 \\
 A &\rightarrow 1.
 \end{aligned}$$

Steps:- Take care of the long Rules.

$$\begin{aligned}
 S_0 &\rightarrow \overset{D}{\circlearrowleft} CSC \mid \overset{E}{\circlearrowleft} ZAB \mid 1 \mid SC \mid CS \\
 S &\rightarrow D \overset{D}{\circlearrowleft} CSC \mid \overset{E}{\circlearrowleft} ZAB \mid 1 \mid SC \mid CS \\
 C &\rightarrow ZZ \\
 B &\rightarrow \overset{E}{\circlearrowleft} ZAB \mid 1. \\
 z &\rightarrow 0 \\
 A &\rightarrow 1. \\
 D &\rightarrow CS. \\
 E &\rightarrow ZA.
 \end{aligned}$$

$$\begin{aligned}
 S_0 &\rightarrow DC \mid EB \mid 1 \mid SC \mid CS \\
 S &\rightarrow DC \mid EB \mid 1 \mid SC \mid CS. \\
 C &\rightarrow ZZ \\
 B &\rightarrow EB \mid 1 \\
 z &\rightarrow 0 \\
 A &\rightarrow 1 \\
 D &\rightarrow CS \\
 E &\rightarrow ZA.
 \end{aligned}$$

Ex:-

$$\begin{aligned}
 A &\rightarrow BAB \mid B \mid \Lambda \\
 B &\rightarrow 00 \mid \Lambda.
 \end{aligned}$$

As Start.
Terminal $z \in \{0\}$.

Ques:-

C. - A

Step 1: $S_0 \rightarrow A$
 $A \rightarrow BAB (B) \Lambda$
 $B \rightarrow \emptyset \Lambda$

Step 2: $S_0 \rightarrow A/\Lambda$ $\begin{matrix} X. \\ B \end{matrix}$ Next lecture
 $A \rightarrow BAB (B) \Lambda$ $\overline{AB|BA|A/\Lambda.BB.}$ $\begin{matrix} A \rightarrow \Lambda \\ B \rightarrow \Lambda \end{matrix}$
 $B \rightarrow \emptyset \Lambda$