Solve Sipser exercises 0.3, 0.4, 0.5, and problem 0.10.

0.3

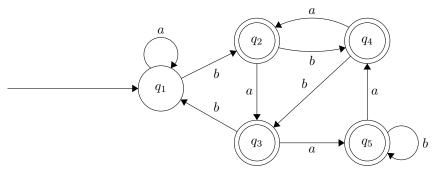
- a. No.
- b. Yes.
- c. x, y, z
- d. x, y
- e. xx, xy, yx, yy, zx, zy, xz, yz
- f. x, y, x, y
- 0.4 The cartesian product has a \* b elements. Since the cartesian product is b ordered pairs for each of the m elements.
- 0.5 There are  $2^c$  elements in the power set of C. Since the subsets in the power set either include an element of C or they do not then it holds that there are  $2^{|C|}$  elements in the power set.
- 0.10 In the step where we divide both sides by (a b) if a = b then (a b) = 0. This leads to a divide by zero error.

For a DFA,  $M = (Q, \sum, \delta, q_0, F)$  in which the set of states is  $Q = \{q_1, q_2, q_3, q_4, q_5\}$ ,  $\sum = \{a, b\}$ ,  $q_0 = q_1$ ,  $F = \{q_2, q_3, q_4, q_5\}$ , and  $\delta$  is specified by the table:

δ	$q_1$	$q_2$	$q_3$	$q_4$	$q_5$
a	$q_1$	$q_3$	$q_5$	$q_2$	$q_4$
b	$q_2$	$q_4$	$q_1$	$q_3$	$q_5$

Do the following:

- (a) Draw the state diagram of the DFA.
- (b) For the strings below, give the corresponding computation of the automaton and say whether it accepts or rejects them. The definition of computation is given in page 40.
  - (a) baab
  - (b) abbb
  - (c) bbba
- (c) Give a succinct English description of the string accepted by M.



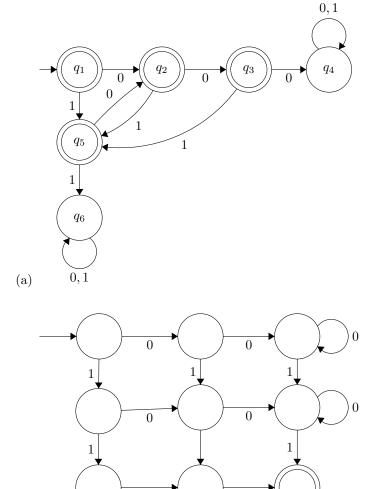
a.

- b. baab is accepted. abbb is accepted. bbba is accepted.
- c. It accepted strings that do not have four consecutive b's.

(b)

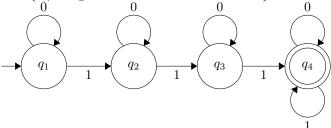
For each of the following languages give a state diagram of a DFA that recognize it. The alphabet is  $\sum = \{0,1\}$ 

- (a)  $\{w|w \text{ does not contain } 000 \text{ or } 11 \text{ as a substring}\}$
- (b)  $\{w|w \text{ contain at least two 0's and at least two 1's}\}$ . The 0's and 1's do not need to be consecutive.

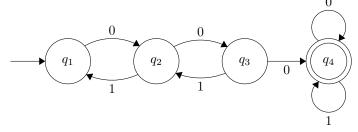


Solve Sipser exercises 1.6b, 1.6d, 1.5c, 1.4c.

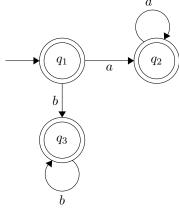
• 1.6b  $\{w|w \text{ begins with a 1 and ends with a 0}\}$ 



• 1.6d  $\{w|w \text{ has length at least 3 and its third symbol is 0}\}$ 



• 1.5c  $\{w|w$  contains neither the substrings ab nor  $ba\}$ 



• 1.4c  $\{w|w \text{ has an even number of } a$ 's and one or two b's $\}$ 

