

# COT 5310: Theory of Computation I

## Homework 1

Due *in class* on Thursday, September 10, 2015

1. **[10 points]** Solve Sipser exercises 0.3, 0.4, 0.5, and problem 0.10
2. **[15 points]** For a DFA,  $M = (Q, \Sigma, \delta, q_0, F)$  in which the set of states is  $Q = \{q_1, q_2, q_3, q_4, q_5\}$ ,  $\Sigma = \{a, b\}$ ,  $q_0 = q_1$ ,  $F = \{q_2, q_3, q_4, q_5\}$ , and  $\delta$  is specified by the table :

$\delta$	$q_1$	$q_2$	$q_3$	$q_4$	$q_5$
a	$q_1$	$q_3$	$q_5$	$q_2$	$q_4$
b	$q_2$	$q_4$	$q_1$	$q_3$	$q_5$

Do the following:

- (a) Draw the state diagram of the DFA.
  - (b) For the strings below, give the corresponding computation of the automaton and say whether it accepts or rejects them. The definition of computation is given in page 40.  
 -baab  
 -abbb  
 -bbba
  - (c) Give a succinct English description of the strings accepted by  $M$
3. **[10 points]** For each of the following languages give a state diagram of a DFA that recognize it. The alphabet is  $\Sigma = \{0, 1\}$ 
  - a)  $\{w \mid w \text{ does not contain } 000 \text{ or } 11 \text{ as a substring}\}$
  - b)  $\{w \mid w \text{ contain at least two } 0\text{'s and at least two } 1\text{'s}\}$ . The 0's and 1's do not need to be consecutive.
4. **[15 points]** Solve Sipser exercises 1.6 b, 1.6 d, 1.5 c, 1.4 c