## Week 3

## March 14, 2022

## 0.1 Linear Regression - for continuous values

```
[65]: #load the boston dataset
from sklearn.datasets import load_boston
```

```
[66]: boston = load_boston()
```

/home/andropov/anaconda3/envs/imp/lib/python3.7/sitepackages/sklearn/utils/deprecation.py:87: FutureWarning: Function load\_boston is deprecated; `load\_boston` is deprecated in 1.0 and will be removed in 1.2.

The Boston housing prices dataset has an ethical problem. You can refer to the documentation of this function for further details.

The scikit-learn maintainers therefore strongly discourage the use of this dataset unless the purpose of the code is to study and educate about ethical issues in data science and machine learning.

In this special case, you can fetch the dataset from the original source::

```
import pandas as pd
import numpy as np
```

```
data_url = "http://lib.stat.cmu.edu/datasets/boston"
raw_df = pd.read_csv(data_url, sep="\s+", skiprows=22, header=None)
data = np.hstack([raw_df.values[::2, :], raw_df.values[1::2, :2]])
target = raw_df.values[1::2, 2]
```

Alternative datasets include the California housing dataset (i.e. :func:`~sklearn.datasets.fetch\_california\_housing`) and the Ames housing dataset. You can load the datasets as follows::

```
from sklearn.datasets import fetch_california_housing
housing = fetch_california_housing()
```

for the California housing dataset and::

from sklearn.datasets import fetch\_openml
housing = fetch\_openml(name="house\_prices", as\_frame=True)

for the Ames housing dataset.

warnings.warn(msg, category=FutureWarning)

- [3]: #see description of dataset boston.DESCR
- [3]: ".. \_boston\_dataset:\n\nBoston house prices dataset\n-----\n\n\*\*Data Set Characteristics:\*\* \n\n :Number of Attributes: 13 numeric/categorical :Number of Instances: 506 \n\n predictive. Median Value (attribute 14) is usually the target.\n\n - CRIM Information (in order):\n per capita crime rate by town\n proportion of residential land zoned for lots over 25,000 sq.ft.\n proportion of non-retail business acres per town\n - INDUS Charles River dummy variable (= 1 if tract bounds river; 0 otherwise)\n nitric oxides concentration (parts per 10 million)\n - AGE average number of rooms per dwelling\n proportion of owneroccupied units built prior to 1940\n - DIS weighted distances to five Boston employment centres\n - RAD index of accessibility to radial highways\n full-value property-tax rate per \$10,000\n - TAX - PTRATIO pupil-teacher ratio by town\n - B  $1000(Bk - 0.63)^2$ where Bk is the proportion of black people by town\n - LSTAT status of the population\n - MEDV Median value of owner-occupied homes in  $1000's\n\$ :Missing Attribute Values: None\n\n Harrison, D. and Rubinfeld, D.L.\n\nThis is a copy of UCI ML housing dataset.\nhttps://archive.ics.uci.edu/ml/machine-learningdatabases/housing/\n\nThis dataset was taken from the StatLib library which is maintained at Carnegie Mellon University.\n\nThe Boston house-price data of Harrison, D. and Rubinfeld, D.L. 'Hedonic\nprices and the demand for clean air', J. Environ. Economics & Management,\nvol.5, 81-102, 1978. Used in Belsley, Kuh & Welsch, 'Regression diagnostics\n...', Wiley, 1980. N.B. Various transformations are used in the table on\npages 244-261 of the latter. $\n\$ Boston house-price data has been used in many machine learning papers that address regression\nproblems. \n \n.. topic:: References\n\n Kuh & Welsch, 'Regression diagnostics: Identifying Influential Data and Sources of Collinearity', Wiley, 1980. 244-261.\n - Quinlan, R. (1993). Combining Instance-Based and Model-Based Learning. In Proceedings on the Tenth International Conference of Machine Learning, 236-243, University of Massachusetts, Amherst. Morgan Kaufmann.\n"
- [67]: import pandas as pd
- [68]: data=pd.DataFrame(boston.data, columns=boston.feature\_names)

```
[69]: #see data in dataframe
      data
[69]:
               CRIM
                           INDUS
                                   CHAS
                                           NOX
                                                          AGE
                                                                  DIS
                                                                       RAD
                                                                               TAX \
                       ZN
                                                    RM
           0.00632
      0
                     18.0
                            2.31
                                    0.0
                                         0.538
                                                 6.575
                                                        65.2
                                                               4.0900
                                                                       1.0
                                                                             296.0
           0.02731
                            7.07
                                         0.469
                                                         78.9
                                                               4.9671
                                                                             242.0
      1
                      0.0
                                    0.0
                                                 6.421
                                                                       2.0
      2
           0.02729
                      0.0
                            7.07
                                    0.0
                                         0.469
                                                 7.185
                                                        61.1
                                                               4.9671
                                                                       2.0
                                                                             242.0
      3
           0.03237
                      0.0
                            2.18
                                    0.0
                                         0.458
                                                 6.998
                                                        45.8
                                                               6.0622
                                                                       3.0
                                                                             222.0
           0.06905
                                    0.0 0.458
                                                               6.0622
      4
                      0.0
                            2.18
                                                 7.147
                                                        54.2
                                                                       3.0
                                                                             222.0
      . .
           0.06263
                           11.93
      501
                      0.0
                                    0.0
                                         0.573
                                                 6.593
                                                        69.1
                                                               2.4786
                                                                             273.0
                                                                       1.0
                           11.93
                                    0.0
                                         0.573
      502
           0.04527
                      0.0
                                                 6.120
                                                        76.7
                                                               2.2875
                                                                       1.0
                                                                             273.0
      503
           0.06076
                      0.0
                           11.93
                                    0.0
                                         0.573
                                                 6.976
                                                        91.0
                                                               2.1675
                                                                             273.0
                                                                       1.0
      504
                           11.93
                                         0.573
           0.10959
                      0.0
                                    0.0
                                                 6.794
                                                        89.3
                                                               2.3889
                                                                       1.0
                                                                             273.0
                      0.0 11.93
                                    0.0 0.573
      505
          0.04741
                                                 6.030
                                                        80.8
                                                               2.5050
                                                                       1.0
                                                                             273.0
           PTRATIO
                          В
                            LSTAT
      0
               15.3
                     396.90
                               4.98
      1
               17.8
                     396.90
                               9.14
      2
               17.8
                     392.83
                               4.03
               18.7
                               2.94
      3
                     394.63
               18.7
      4
                     396.90
                               5.33
                               9.67
      501
               21.0
                     391.99
      502
              21.0
                    396.90
                               9.08
              21.0
      503
                     396.90
                               5.64
      504
              21.0
                     393.45
                               6.48
      505
              21.0
                     396.90
                               7.88
      [506 rows x 13 columns]
[70]: #column of Median Value is usually the target - to be predicted by regression_
       \rightarrowmodel
      data['MEDV'] = pd.DataFrame(boston.target)
[71]:
      data
                                                          AGE
[71]:
              CRIM
                       ZN
                           INDUS
                                   CHAS
                                           NOX
                                                    RM
                                                                  DIS
                                                                       RAD
                                                                               TAX \
                                                        65.2
           0.00632
      0
                     18.0
                            2.31
                                    0.0
                                        0.538
                                                 6.575
                                                               4.0900
                                                                       1.0
                                                                             296.0
      1
           0.02731
                      0.0
                            7.07
                                    0.0
                                         0.469
                                                 6.421
                                                         78.9
                                                               4.9671
                                                                       2.0
                                                                             242.0
      2
           0.02729
                            7.07
                                    0.0
                                         0.469
                                                 7.185
                                                        61.1
                                                                       2.0
                                                                             242.0
                      0.0
                                                               4.9671
      3
           0.03237
                      0.0
                            2.18
                                    0.0
                                         0.458
                                                 6.998
                                                        45.8
                                                               6.0622
                                                                       3.0
                                                                             222.0
      4
           0.06905
                      0.0
                            2.18
                                    0.0 0.458
                                                 7.147
                                                        54.2
                                                               6.0622
                                                                       3.0
                                                                             222.0
      501
          0.06263
                      0.0
                           11.93
                                    0.0
                                         0.573
                                                 6.593
                                                        69.1
                                                               2.4786
                                                                       1.0
                                                                             273.0
      502
           0.04527
                           11.93
                                         0.573
                                                        76.7
                                                                             273.0
                      0.0
                                    0.0
                                                 6.120
                                                               2.2875
                                                                       1.0
      503
           0.06076
                      0.0
                           11.93
                                    0.0 0.573
                                                 6.976
                                                        91.0
                                                               2.1675
                                                                       1.0
                                                                             273.0
```

```
504 0.10959
                  0.0 11.93
                              0.0 0.573 6.794 89.3 2.3889
                                                            1.0 273.0
     505 0.04741
                  0.0 11.93
                              0.0 0.573 6.030 80.8 2.5050
                                                                273.0
                                                           1.0
                      B LSTAT MEDV
         PTRATIO
     0
            15.3 396.90
                          4.98
                               24.0
            17.8
                 396.90
     1
                          9.14
                               21.6
     2
            17.8 392.83
                          4.03
                               34.7
     3
                          2.94 33.4
            18.7 394.63
     4
            18.7 396.90
                          5.33
                               36.2
             ...
     . .
                  •••
                          •••
     501
            21.0
                          9.67
                               22.4
                 391.99
     502
            21.0 396.90
                          9.08
                               20.6
     503
            21.0 396.90
                          5.64 23.9
     504
            21.0 393.45
                          6.48 22.0
     505
            21.0 396.90
                          7.88 11.9
     [506 rows x 14 columns]
[20]: #find all correlation values, RM has highest with target MEDV, so select RM for
      \hookrightarrow training
     pd.DataFrame(data.corr().round(2))
                    ZN
                        INDUS CHAS
                                                                   PTRATIO \
             CRIM
                                    NOX
                                          RM
                                               AGE
                                                    DIS
                                                          RAD
                                                               TAX
     CRIM
             1.00 -0.20
                        0.41 -0.06 0.42 -0.22 0.35 -0.38
                                                        0.63 0.58
                                                                      0.29
     ZN
            -0.20 1.00
                        -0.53 -0.04 -0.52 0.31 -0.57 0.66 -0.31 -0.31
                                                                      -0.39
     INDUS
             0.41 - 0.53
                        1.00 0.06 0.76 -0.39 0.64 -0.71 0.60 0.72
                                                                      0.38
     CHAS
            -0.06 -0.04
                        0.06 1.00 0.09 0.09 0.09 -0.10 -0.01 -0.04
                                                                      -0.12
     NOX
            0.42 - 0.52
                        0.76  0.09  1.00  -0.30  0.73  -0.77  0.61  0.67
                                                                      0.19
     RM
            -0.22 0.31 -0.39 0.09 -0.30 1.00 -0.24 0.21 -0.21 -0.29
                                                                      -0.36
     AGE
             0.35 - 0.57
                        0.64 0.09 0.73 -0.24 1.00 -0.75 0.46 0.51
                                                                      0.26
     DIS
                        -0.71 -0.10 -0.77 0.21 -0.75 1.00 -0.49 -0.53
            -0.38 0.66
                                                                      -0.23
                        0.60 -0.01  0.61 -0.21  0.46 -0.49  1.00  0.91
     RAD
             0.63 - 0.31
                                                                      0.46
     TAX
             0.58 - 0.31
                        0.72 -0.04 0.67 -0.29 0.51 -0.53 0.91
                                                              1.00
                                                                      0.46
     PTRATIO 0.29 -0.39
                        1.00
            -0.18
     В
     LSTAT
             0.46 - 0.41
                         0.60 -0.05 0.59 -0.61 0.60 -0.50 0.49 0.54
                                                                      0.37
            MEDV
                                                                      -0.51
                B LSTAT MEDV
     CRIM
            -0.39
                   0.46 - 0.39
     ZN
             0.18 -0.41 0.36
     INDUS
            -0.36
                   0.60 - 0.48
     CHAS
             0.05 -0.05 0.18
     NOX
            -0.38
                   0.59 - 0.43
     RM
             0.13 -0.61 0.70
            -0.27
     AGE
                   0.60 - 0.38
     DIS
             0.29 -0.50 0.25
```

[20]:

```
TAX
              -0.44 0.54 -0.47
     PTRATIO -0.18 0.37 -0.51
              1.00 -0.37 0.33
     LSTAT -0.37 1.00 -0.74
     MF.DV
              0.33 -0.74 1.00
[21]: # x corresponds to train data
      x=data['RM']
[22]: #y corresponds to labels
      y=data['MEDV']
[73]: #import module for linear regression
      from sklearn.linear_model import LinearRegression
[75]: #import train_test_split module
      from sklearn.model_selection import train_test_split
[74]: linearRegressionClassifier = LinearRegression()
[28]: #convert x and y to pandas Dataframes
      x=pd.DataFrame(x)
      y=pd.DataFrame(y)
[76]: #split the dataset using train_test_split function, pass train data, labels,
      \rightarrow and test data ratio
      x_train, x_test, y_train, y_test = train_test_split(x,y,test_size=0.2)
[77]: #check number of rows and columns
      print(x_train.shape)
     (404, 1)
[78]: #train the classifier by fitting to train data and corresponding labels
      linearRegressionClassifier.fit(x_train, y_train)
[78]: LinearRegression()
[34]: import numpy as np
[79]: #import the mean squared error module
      from sklearn.metrics import mean_squared_error
[80]: #determine the predicted values
      y_pred=linearRegressionClassifier.predict(x_test)
```

-0.44 0.49 -0.38

RAD

```
[82]: y_pred.shape
[82]: (102, 1)
[83]: #calculate root mean square error
      np.sqrt(mean_squared_error(y_test, y_pred))
[83]: 6.342458820150728
[84]: #determine R^2 scores (because regression)
      linearRegressionClassifier.score(x_test,y_test)
[84]: 0.47919078205973686
     0.2 working with Ridge
 []: #L2 Regularization: It adds an L2 penalty which is equal to the square of the
       → magnitude of coefficients.
[41]: #importing module to work with ridge regression model
      from sklearn.linear_model import Ridge
[85]: #setting parameter alpha for new ridge model
      ridge1=Ridge(alpha=1)
[86]: ridge1.fit(x_train,y_train)
[86]: Ridge(alpha=1)
[88]: y_pred1=ridge1.predict(x_test)
[89]: np.sqrt(mean_squared_error(y_test, y_pred1))
[89]: 6.341851705830557
[46]: ridge2=Ridge(alpha=100)
[47]: ridge2.fit(x_train,y_train)
[47]: Ridge(alpha=100)
[48]: y_pred2=ridge2.predict(x_test)
[97]: np.sqrt(mean_squared_error(y_test, y_pred2))
[97]: 9.28858567055522
```

```
[90]: ridge2.score(x_test,y_test)
[90]: 0.4264608073819258
          # Working with Lasso
  []: #L1 regularization: It adds an L1 penalty that is equal to the
       #absolute value of the magnitude of coefficient, or simply restricting the size_{\sf L}
        \hookrightarrow of coefficients.
[91]: from sklearn.linear_model import Lasso
[92]: Lasso1=Lasso(alpha=0.01)
[94]: Lasso1.fit(x_train,y_train)
[94]: Lasso(alpha=0.01)
[95]: y_predL1=Lasso1.predict(x_test)
[96]: np.sqrt(mean_squared_error(y_test, y_predL1))
[96]: 6.342170750650113
[98]: Lasso1.score(x_test,y_test)
[98]: 0.4792380904770168
  []: | #working with ElasticNet - combines feature elimination from lasso and feature
        → coefficient reduction from Ridge
[60]: from sklearn.linear_model import ElasticNet
[99]: en1=ElasticNet(alpha=0.1, l1_ratio=0.5)
[100]: en1.fit(x_train,y_train)
[100]: ElasticNet(alpha=0.1)
[101]: y_pred_en1=en1.predict(x_test)
[102]: np.sqrt(mean_squared_error(y_test, y_pred_en1))
[102]: 6.359665176837157
[103]: en1.score(x test, y test)
```

[103]: 0.4763611587818619

[]: