

$$x^4 = -1$$

$$x^4 = \rho^4 (\cos 4\alpha + i \sin 4\alpha)$$

$$-1 = 1(-1 + 0i) = 1(\cos \pi + i \sin \pi)$$

$$x = \sqrt[4]{1} \left(\cos \frac{\pi + 2K\pi}{4} + i \sin \frac{\pi + 2K\pi}{4} \right) \quad \boxed{0 \leq K \leq 3}$$

$$\boxed{K=0} \quad x = \left(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4} \right) = \frac{\sqrt{2}}{2} + i \frac{\sqrt{2}}{2} = \boxed{\frac{\sqrt{2}}{2} (1+i)}$$

$$\boxed{K=1} \quad x = \left(\cos \frac{3}{4}\pi + i \sin \frac{3}{4}\pi \right) = -\frac{\sqrt{2}}{2} + i \frac{\sqrt{2}}{2} = \boxed{\frac{\sqrt{2}}{2} (i-1)}$$

$$\boxed{K=2} \quad x = \left(\cos \frac{5}{4}\pi + i \sin \frac{5}{4}\pi \right) = -\frac{\sqrt{2}}{2} - i \frac{\sqrt{2}}{2} = \boxed{-\frac{\sqrt{2}}{2} (1+i)}$$

$$\boxed{K=3} \quad x = \left(\cos \frac{7}{4}\pi + i \sin \frac{7}{4}\pi \right) = \frac{\sqrt{2}}{2} - i \frac{\sqrt{2}}{2} = \boxed{\frac{\sqrt{2}}{2} (1-i)}$$

4 soluzioni complesse

$$x^2 = 2$$

$$x^2 = \rho^2 (\cos 2\alpha + i \sin 2\alpha)$$

$$2 = 2(1 + 0i) = 2(\cos 0 + i \sin 0)$$

$$x = \sqrt{2} \left(\cos \frac{2K\pi}{2} + i \sin \frac{2K\pi}{2} \right) \quad \boxed{0 \leq K \leq 1}$$

$$\boxed{K=0} \quad x = \sqrt{2} (\cos 0 + i \sin 0) = \sqrt{2} \cdot (1 + i0) = \boxed{\sqrt{2}}$$

$$\boxed{K=1} \quad x = \sqrt{2} (\cos \pi + i \sin \pi) = \sqrt{2} \cdot (-1 + i0) = \boxed{-\sqrt{2}}$$

2 soluzioni reali

(Infatti si poteva risolvere anche senza utilizzare numeri complessi)

$$x^3 = 2$$

$$x^3 = r^3 (\cos 3\alpha + i \sin 3\alpha)$$

$$2 = 2(1 + 0i) = 2(\cos 0 + i \sin 0)$$

$$x = \sqrt[3]{2} \left(\cos \frac{2K\pi}{3} + i \sin \frac{2K\pi}{3} \right) \quad \boxed{0 \leq K \leq 2}$$

$$\boxed{K=0} \quad x = \sqrt[3]{2} (\cos 0 + i \sin 0) = \sqrt[3]{2} (1 + 0) = \boxed{\sqrt[3]{2}}$$

$$\boxed{K=1} \quad x = \sqrt[3]{2} \left(\cos \frac{2}{3}\pi + i \sin \frac{2}{3}\pi \right) = \boxed{\sqrt[3]{2} \left(-\frac{1}{2} + i \frac{\sqrt{3}}{2} \right)}$$

$$\boxed{K=2} \quad x = \sqrt[3]{2} \left(\cos \frac{4}{3}\pi + i \sin \frac{4}{3}\pi \right) = \boxed{\sqrt[3]{2} \left(-\frac{1}{2} - i \frac{\sqrt{3}}{2} \right)}$$

1 soluzione reale e 2 soluzioni complesse

$$x^6 = -64$$

$$x^6 = r^6 (\cos 6\alpha + i \sin 6\alpha)$$

$$-64 = 64(-1 + 0i) = 64(\cos \pi + i \sin \pi)$$

$$x = \sqrt[6]{64} \left(\cos \frac{\pi + 2K\pi}{6} + i \sin \frac{\pi + 2K\pi}{6} \right) \quad \boxed{0 \leq K \leq 5}$$

$$\boxed{K=0} \quad x = 2 \left(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6} \right) = 2 \left(\frac{\sqrt{3}}{2} + i \frac{1}{2} \right) = 2 \left(\frac{\sqrt{3} + i}{2} \right) = \boxed{\sqrt{3} + i}$$

$$\boxed{K=1} \quad x = 2 \left(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2} \right) = 2(0 + i) = \boxed{2i}$$

$$\boxed{K=2} \quad x = 2 \left(\cos \frac{5}{6}\pi + i \sin \frac{5}{6}\pi \right) = 2 \left(-\frac{\sqrt{3}}{2} + i \frac{1}{2} \right) = 2 \left(\frac{-\sqrt{3} + i}{2} \right) = \boxed{-\sqrt{3} + i}$$

$$\boxed{K=3} \quad x = 2 \left(\cos \frac{7}{6}\pi + i \sin \frac{7}{6}\pi \right) = 2 \left(-\frac{\sqrt{3}}{2} - i \frac{1}{2} \right) = 2 \left(\frac{-\sqrt{3} - i}{2} \right) = \boxed{-\sqrt{3} - i}$$

$$\boxed{K=4} \quad x = 2 \left(\cos \frac{3}{2}\pi + i \sin \frac{3}{2}\pi \right) = 2(0 - i) = \boxed{-2i}$$

$$\boxed{K=5} \quad x = 2 \left(\cos \frac{11}{6}\pi + i \sin \frac{11}{6}\pi \right) = 2 \left(\frac{\sqrt{3}}{2} - i \frac{1}{2} \right) = 2 \left(\frac{\sqrt{3} - i}{2} \right) = \boxed{\sqrt{3} - i}$$

6 soluzioni complesse