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METRICS FOR LINEAR REGRESSION

Mean Squared Error

Mean squared error, or MSE for short, is a popular error metric for regression problems.

It is also an important loss function for algorithms fit or optimized using the least squares framing of a regression problem. Here “*least squares*” refers to minimizing the mean squared error between predictions and expected values.

The MSE is calculated as the mean or average of the squared differences between predicted and expected target values in a dataset.

$$\text{MSE} = 1 / N * \sum \text{for } i \text{ to } N (y_i - \hat{y}_i)^2$$

Where y_i is the i 'th expected value in the dataset and \hat{y}_i is the i 'th predicted value. The difference between these two values is squared, which has the effect of removing the sign, resulting in a positive error value.

Root Mean Squared Error

The Root Mean Squared Error, or RMSE, is an extension of the mean squared error.

Importantly, the square root of the error is calculated, which means that the units of the RMSE are the same as the original units of the target value that is being predicted.

For example, if your target variable has the units “*dollars*,” then the RMSE error score will also have the unit “*dollars*” and not “*squared dollars*” like the MSE.

As such, it may be common to use MSE loss to train a regression predictive model, and to use RMSE to evaluate and report its performance.

The RMSE can be calculated as follows:

$$\text{RMSE} = \sqrt{1 / N * \sum \text{for } i \text{ to } N (y_i - \hat{y}_i)^2}$$

Where y_i is the i 'th expected value in the dataset, \hat{y}_i is the i 'th predicted value, and $\sqrt{()}$ is the square root function.

We can restate the RMSE in terms of the MSE as:

$$\text{RMSE} = \sqrt{\text{MSE}}$$

Note that the RMSE cannot be calculated as the average of the square root of the mean squared error values. This is a common error made by beginners and is an example of Jensen's inequality.

You may recall that the square root is the inverse of the square operation. MSE uses the square operation to remove the sign of each error value and to punish large errors. The square root reverses this operation, although it ensures that the result remains positive.

The root mean squared error between your expected and predicted values can be calculated using the `mean_squared_error()` function from the scikit-learn library.

By default, the function calculates the MSE, but we can configure it to calculate the square root of the MSE by setting the *“squared”* argument to *False*.

The function takes a one-dimensional array or list of expected values and predicted values and returns the mean squared error value.

Mean Absolute Error

Mean Absolute Error, or MAE, is a popular metric because, like RMSE, the units of the error score match the units of the target value that is being predicted.

Unlike the RMSE, the changes in MAE are linear and therefore intuitive.

That is, MSE and RMSE punish larger errors more than smaller errors, inflating or magnifying the mean error score. This is due to the square of the error value. The MAE does not give more or less weight to different types of errors and instead the scores increase linearly with increases in error.

As its name suggests, the MAE score is calculated as the average of the absolute error values. Absolute or *abs()* is a mathematical function that simply makes a number positive. Therefore, the difference between an expected and predicted value may be positive or negative and is forced to be positive when calculating the MAE.

The MAE can be calculated as follows:

$$\text{MAE} = 1 / N * \text{sum for } i \text{ to } N \text{ abs}(y_i - \hat{y}_i)$$

Where y_i is the i 'th expected value in the dataset, \hat{y}_i is the i 'th predicted value and *abs()* is the absolute function.

We can create a plot to get a feeling for how the change in prediction error impacts the MAE.