# Assignment-4 Python Programming

Date	11 October 2022
Team ID	PNT2022TMID40200
Project Name	Project - Traffic and Capacity
	Analytics for Major Ports.

In [1]:

import pandas as pd import numpy as np import matplotlib.pyplot as plt import seaborn as sns

# Loading the dataset

In [ ]:

df = pd.read\_csv('Mall\_Customers.csv') df

Out[]:

CustomerID Gender Age Annual Income (k\$) Spending Score (1-100)

0	1	Male	19	15	39		
1	2	Male	21	15	81		
2	3	Female	20	16	6		
3	4	Female	23	16	77		
4	5	Female	31	17	40		
195	196	Female	35	120	79		
196	197	Female	45	126	28		
197	198	Male	32	126	74		
198	199	Male	32	137	18		
199	200	Male	30	137	83		
200	rows	× 5 colu	mns				

# **Encoding Categorical Columns**

```
from sklearn.preprocessing import LabelEncoder le
In [ ]:
            LabelEncoder()
            df['Gender'] = le.fit\_transform(df['Gender'])
             df
In [ ]:
Out[]:
                  CustomerID
                                 Gender
                                                                         Spending Score (1-100)
                                           Age
                                                 Annual Income (k$)
0
                         1
              1
                                  19
                                           15
                                                    39
1
              2
                         1
                                  21
                                           15
                                                    81
2
              3
                                  20
                                           16
                                                    6
3
              4
                                  23
                                           16
                                                    77
                         0
                                  31
                                           17
                                                    40
                         •••
        195
                       196
                                  0
                                           35
                                                    120
                                                             79
        196
                       197
                                           45
                                                    126
                                                             28
        197
                       198
                                           32
                                                    126
                                                             74
        198
                       199
                                  1
                                           32
                                                    137
                                                             18
        199
                       200
                                  1
                                           30
                                                    137
                                                             83
                       rows \times 5 \ columns
        200
```

#### Visualizations

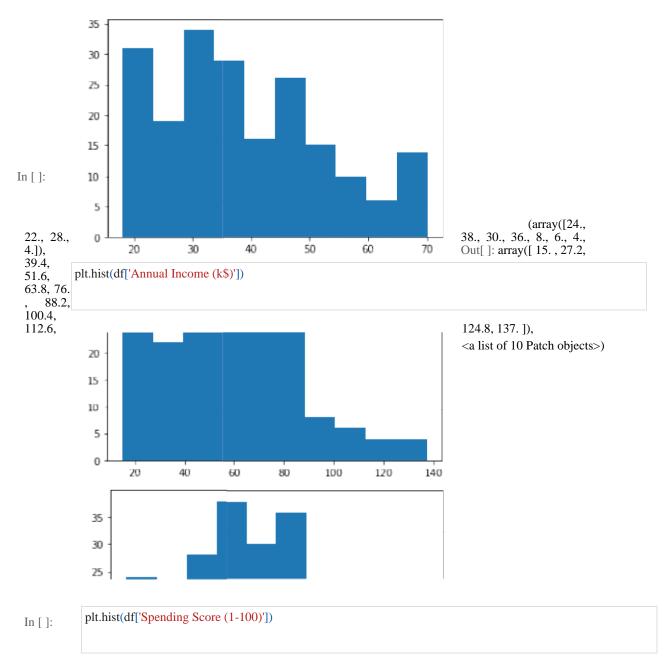
## Univariate Analysis

array([18., 23.2, 28.4, 33.6, 38.8, 44., 49.2, 54.4, 59.6, 64.8, 70.]),

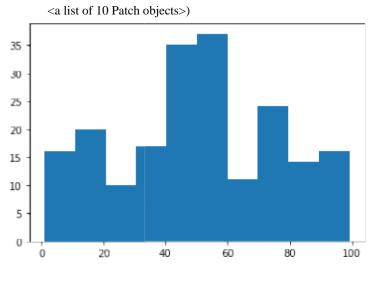
```
In []: plt.hist(df['Age'])

(array([31., 19., 34., 29., 16., 26., 15., 10., 6., 14.]), Out[]:
```

<a list of 10 Patch objects>)



 $\begin{array}{ll} \mathrm{Out}[\ ]: (array([16., 20., 10., 17., 35., 37., 11., 24., 14., 16.]), & array([\ 1.\ , 10.8, 20.6, 30.4, 40.2, 50.\ , 59.8, 69.6, 79.4, 89.2, 99.\ ]), \end{array}$ 

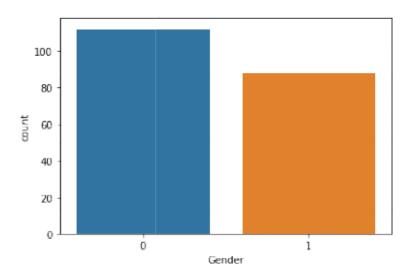


In []:

/usr/local/lib/python3.7/dist-packages/seaborn/\_decorators.py:43: FutureWarnin g: Pass the following variable as a keyword arg: x. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without a n explicit keyword will result in an error or misinterpretation.

FutureWarning <matplotlib.axes.\_subplots.AxesSubplot at 0x7fdb93a2d490>

Out[]:



## Bi-Variate Analysis

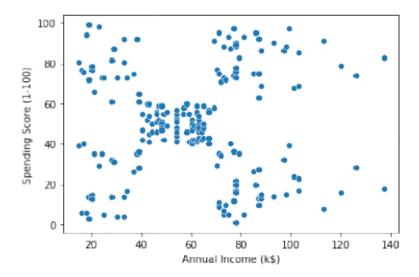
In []:

sns.scatterplot(df['Annual Income (k\$)'], df['Spending Score (1-100)'])

/usr/local/lib/python3.7/dist-packages/seaborn/\_decorators.py:43: FutureWarnin g: Pass the following variables as keyword args: x, y. From version 0.12, the o nly valid positional argument will be `data`, and passing other arguments witho ut an explicit keyword will result in an error or misinterpretation.

FutureWarning <matplotlib.axes.\_subplots.AxesSubplot at 0x7fdb93a1f1d0>

Out[]:

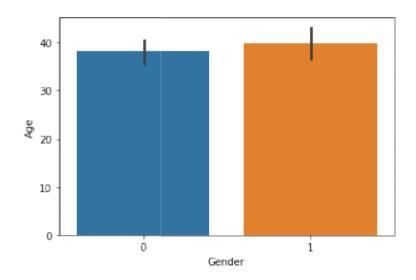


```
n
[
]
:
sns.barplot(df['Gender'], df['Age'])
```

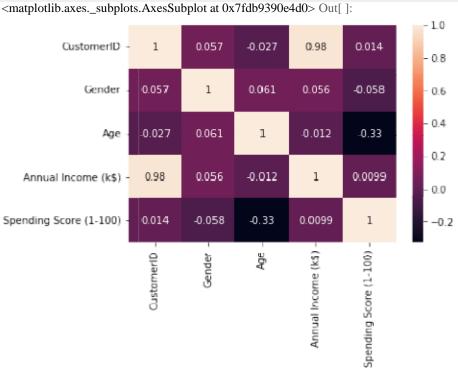
/usr/local/lib/python3.7/dist-packages/seaborn/\_decorators.py:43: FutureWarnin g: Pass the following variables as keyword args: x, y. From version 0.12, the o nly valid positional argument will be `data`, and passing other arguments witho ut an explicit keyword will result in an error or misinterpretation.

# FutureWarning <matplotlib.axes.\_subplots.AxesSubplot at 0x7fdb93931b90>

Out[]:



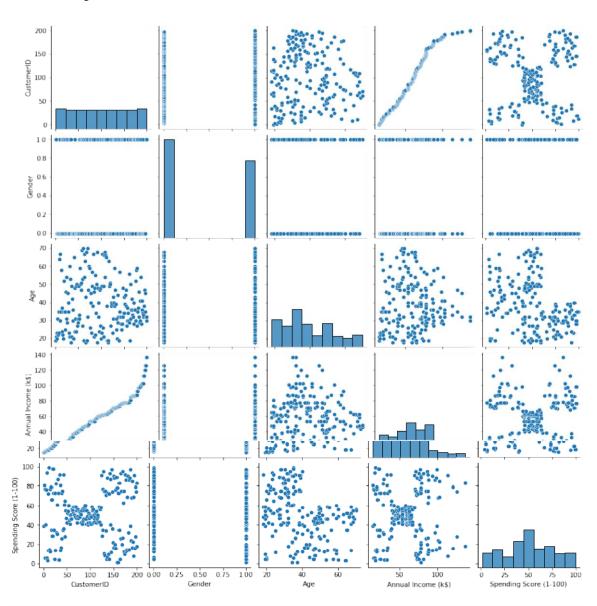
In [ ]: sns.heatmap(df.corr(), annot = True)



# Multi-variate Analysis



<seaborn.axisgrid.PairGrid at 0x7fdb91011e50> Out[]:



In [ ]:

## **Descriptive Statistics**

In []: df.info()

<class 'pandas.core.frame.DataFrame'> RangeIndex: 200 entries, 0 to 199 Data columns

(total 5 columns):

# Column Non-Null Count Dtype

.\_\_ \_\_\_\_\_

0 CustomerID 200 non-null int64

Gender 200 non-null int64 2 Age 200 non-null int64

3 Annual Income (k\$) 200 non-null int64 4 Spending Score (1-100) 200 non-null int64 dtypes: int64(5) memory usage: 7.9 KB

In []:

In []:

df.describe()

Out[]: CustomerID Gender Age Annual Income (k\$) Spending Score (1-100)

	df.skew()							
			200.000000 200.000000 200.000000			200.000000	200.000000	
	mean					60.560000	50.200000	
		std	100.500000	0.440000	38.850000	26.264721	25.823522	
min	min		57.879185	0.497633	13.969007	15.000000	1.000000	
		25%	1.000000	0.000000	18.000000	41.500000	34.750000	
		50%	50.750000	0.000000	28.750000	61.500000	50.000000	
		750/	100.500000	0.000000	36.000000	78.000000	73.000000	
		75%	150.250000	1.000000	49.000000	137.000000	99.000000	
In [].		max	200.000000	1.000000	70.000000			
In [ ]:								
Out[]: Cus	stomerID			0.000000				
	Gender			0.243578				
	Age		(1. ft)	0.485569 0.32184	2			
	Annual Income (k\$)							
Spending Score (1-100) -0.047220 dtype: float64								

df.kurt()

In []: df.corr() -1.200000 Gender -1.960375 Age -0.671573 Annual Income (k\$) -0.098487 Annual Income Out[]: Spending Score (1-100)CustomerID Gender (k\$) Age CustomerID CustomerID 1.000000 0.057400 -0.026763 0.977548 0.013835 0.057400 0.056410 -0.058109 1.000000 0.060867 Gender Age -0.026763 -0.012398 -0.327227 0.060867 1.000000 0.977548 1.000000 0.009903 0.056410 -0.012398 Annual Income (k\$) 1.000000 0.009903 Spending Score (1-100) 0.013835 -0.058109 -0.327227 df.var() In []: CustomerID 3350.000000 Out[]: Gender 0.247638 Age 195.133166 Annual Income (k\$) 689.835578 Spending Score (1-100) dtype: 666.854271 float64 In []: df.std() Out[]: CustomerID 57.879185 Gender 0.497633 Age 13.969007 Annual Income (k\$) 26.264721 Spending Score (1-100) 25.823522 dtype: float64 Checking for missing values In []: df.isna().sum() Out[]: CustomerID

Gender 0 Age 0 Spending Score (1-100)

# Finding & Handling Ouliers

```
In [ ]: quantile = df.quantile(q = [0.25, \\ 0.75]) \quad quantile
```

ıt[]:	CustomerID		Gender	Age Annu	Age Annual Income (k\$) Spending Score (1-100)				
	0.25	50.75	0.0	28.75	41.5	34.75			
	0.75	150.25	1.0	49.00	78.0	73.00			
n [ ]:	IQR = q $IQR$	uantile.iloc[	.]-	quantil e.	iloc[0]				
	Customer	rID		99.50					
Out[ ]:	Gender			1.00					
	Age			20.25					
	Annual I	ncome (k\$)		36.50					
n [ ]:	Spending float64	Score (1	-100) dt	ype: 38.25					
	upper = q	uantile.iloc[	] upper	+ (1.5 *	IQR)				
Out[ ]:									
	Customer	rID		299.500					
	Gender			2.500					
	Age			79.375					
[]:		ncome (k\$)		132.750					
	Spending float64	Score (1	-100) dt	ype: 130.375					
Out[ ]:	1 Custonia	unntile.iloc[(	)] lower	-98.500IQF	2)				
~ ~·[ ].	Gender			-1.500					
	Age			-1.625					

Annual Income (k\$) -13.250 Spending Score (1-100) -22.625 dtype: float64

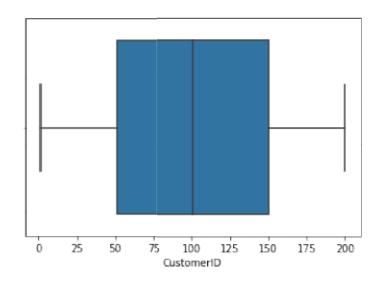
```
In []:
                 df.mean()
 Out[]:
                                              100.50
             CustomerID
                                                 0.44
                                               38.85 60.56
            Gender
                                               50.20
             Age
             Annual Income (k$) Spending
In []:
            Score (1-100) dtype: float64
            df['Annual Income (k$)'].max()
            sns.boxplot(df['CustomerID'])
            137 Out[]:
```

In []:

/usr/local/lib/python3.7/dist-packages/seaborn/\_decorators.py:43: FutureWarnin g: Pass the following variable as a keyword arg: x. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without a n explicit keyword will result in an error or misinterpretation.

FutureWarning <matplotlib.axes.\_subplots.AxesSubplot at 0x7fdb904c1290>

Out[]:



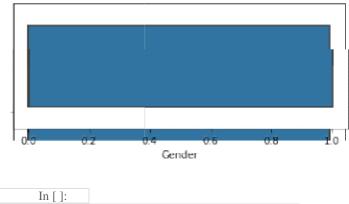


/usr/local/lib/python3.7/dist-packages/seaborn/\_decorators.py:43: FutureWarnin g: Pass the following variable as a keyword arg: x. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without a n explicit keyword will result in an error or misinterpretation.

**FutureWarning** 

<matplotlib.axes.\_subplots.AxesSubplot at 0x7fdb8ebea250>

Out[]:

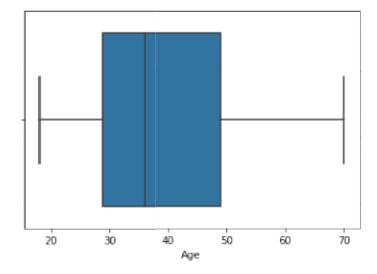


In []:
sns.boxplot(df['Age'])

/usr/local/lib/python3.7/dist-packages/seaborn/\_decorators.py:43: FutureWarnin g: Pass the following variable as a keyword arg: x. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without a  $\,$ n explicit keyword will result in an error or misinterpretation.

FutureWarning <matplotlib.axes.\_subplots.AxesSubplot at 0x7fdb93b3ee50>

Out[]:



I n [ ]:

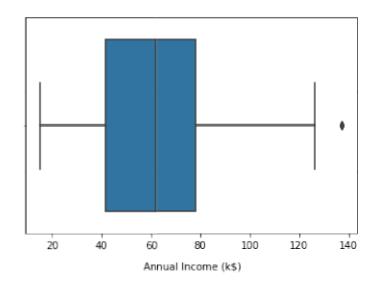
```
sns.boxplot(df['Annual Income (k$)'])
```

/usr/local/lib/python3.7/dist-packages/seaborn/\_decorators.py:43: FutureWarnin g: Pass the following variable as a keyword arg: x. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without a n explicit keyword will result in an error or misinterpretation.

#### **FutureWarning**

<matplotlib.axes.\_subplots.AxesSubplot at 0x7fdb8eb28450>

Out[]:



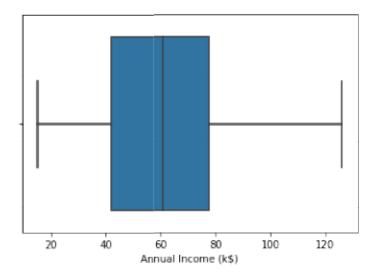
In []: df['Annual Income (k\$)'] = np.where(df['Annual Income (k\$)'] > 132.750, 60.55,

In []: sns.boxplot(df['Annual Income (k\$)'])

/usr/local/lib/python3.7/dist-packages/seaborn/\_decorators.py:43: FutureWarnin g: Pass the following variable as a keyword arg: x. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without a n explicit keyword will result in an error or misinterpretation.

**FutureWarning** 

 $<\!matplotlib.axes.\_subplots.AxesSubplot \ at \ 0x7fdb8eb18e90> Out[\ ]:$ 



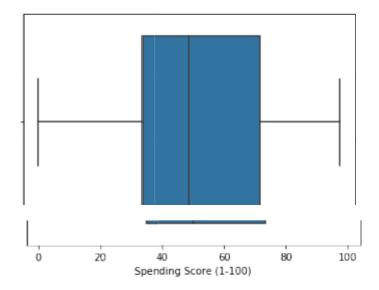
```
In [ ]: df['Annual Income (k$)'].max()

126.0 Out[ ]:

In [ ]: sns.boxplot(df['Spending Score (1-100)'])
```

/usr/local/lib/python3.7/dist-packages/seaborn/\_decorators.py:43: FutureWarnin g: Pass the following variable as a keyword arg: x. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without a  $\,$ n explicit keyword will result in an error or misinterpretation.

FutureWarning



#### Scaling the data

In [ ]:

```
sklearn.preprocessing
                                                                                                                                                                     import
from
                                                                                                                                                                                                                        StandardScaler
     StandardScaler().fit_transform(df) ss
  array([[-1.7234121, 1.12815215, -1.42456879, -1.78843062, -0.43480148], Out[]:
                                                 [-1.70609137, 1.12815215, -1.28103541, -1.78843062, 1.19570407], [-1.68877065, -1.28103541, -1.78843062, -1.19570407]
                                                 0.88640526, -1.3528021 , -1.74850629, -1.71591298], [-1.67144992, -0.88640526, -
                                                 1.13750203, -1.74850629, 1.04041783],
                                                 \hbox{ $[-1.6541292$ , $-0.88640526, $-0.56336851, $-1.70858195, $-0.39597992], $[-1.63680847, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.88640526, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.886406, $-0.88640
                                                 0.88640526, -1.20926872, -1.70858195, 1.00159627], [-1.61948775, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526, -0.88640526
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```

### Clustering Algorithm

```
In []:

from sklearn.cluster import KMeans TWSS = []

k = list(range(2,9))

for i in k:

kmeans = KMeans(n_clusters = i , init = 'k-means++') kmeans.fit(df)

TWSS.append(kmeans.inertia_)

In []:

TWSS

[381507.64738523855, Out[]:
```

191550.08627670942, 153530.68956249507,

268062.55433747417,

119166.15727643928, 101321.0166427429, 85744.90139221892]

In []: plt.plot(k,TWSS, 'ro--')

[<matplotlib.lines.Line2D at 0x7fdb8d642b90>] Out[]: In [ ]: model = KMeans(n\_clusters = 4) model.fit(df) KMeans(n\_clusters=4) Out[]: In [ ]: mb = pd.Series(model.labels\_) In [ ]: df['Cluster'] = mb In [ ]: Out[]: CustomerID Gender Age Annual Income (k\$) Spending Score (1-100) Cluster 15.00 15.00 16.00 16.00 17.00 120.00 126.00 126.00 60.55 60.55 

200 rows × 6 columns