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   "from tensorflow.keras.datasets import mnist\n",
   "from tensorflow.keras.models import Sequential\n",
   "from tensorflow.keras.layers import Conv2D, Dense, Flatten\n",
   "from tensorflow.keras.optimizers import Adam\n",
   "from tensorflow.keras.models import load model\n",
   "from PIL import Image, ImageOps\n",
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]

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  "Y test = np utils.to categorical(y test, number of classes)"
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  "model.add(Conv2D(32, (3, 3), activation=\"relu\"))\n",
  "model.add(Flatten())\n",
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- val loss: 0.1058 - val accuracy: 0.9701\n",
       "Epoch 2/5\n",
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- val_loss: 0.0962 - val accuracy: 0.9752\n",
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 "from matplotlib import pyplot\n",
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 "print('X train:' +str(X train.shape))\n",
 "print('y_train:' +str(y_train.shape))\n",
 "print('X test:' +str(X test.shape))\n",
 "print('y test:' +str(y test.shape))\n",
 "from matplotlib import pyplot\n",
 "for i in range(9):\n",
 " pyplot.subplot(330+1+i)\n",
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