

## I. STREAMING GRAPH ALGORITHM INSTANCES

Based on different state updating strategies, GraphFlow provides efficient and effective graph updates. GraphFlow is a general model to support different graph algorithms, but the implemental details are different for different algorithms. Because of the space limitation, here, we only select the Triangle Count (TC) algorithm as an example to illustrate the application of our GraphFlow model.

### A. GraphFlow-based Triangle Count (GTC)

TC algorithm is used to count the number of different triangles. Following the GraphFlow model, here is a design of State, Event, and Transform for GraphFlow-based Triangle Count (GTC) algorithm:

**State:** The state of a graph consists of each vertex's adjacent vertices information, i.e.,  $State = \{f_1, f_2, \dots, f_n\}$ , where  $n$  is the number of vertices in the graph. We define the factor of a node  $v_i$  for TC as (3):

$$f_i = (v_i, A_i, t_i), 1 \leq i \leq n \quad (3)$$

where  $A_i$  is the set of adjacent vertices of  $v_i$ , and  $t_i$  is the number of triangles formed by  $v_i$ .

**Event:** EventStream contains a sequence of Events, i.e.,  $\{e_1, e_2, \dots, e_n\}$ , where  $n$  is the number of events. We define an event for TC as (4):

$$e_i = (TYPE, m_i), 1 \leq i \leq n \quad (4)$$

where  $TYPE \in \{ADD, UPDATE, DELETE\}$ , and  $m_i$  is the event messages of  $e_i$ .

**Transform:** The state update process for TC algorithm is an instantiation of Algorithm 1. For a given event  $e$ , the source vertex  $v_{source}$  and the target vertex  $v_{target}$  can be got from  $GET\_VALUE(e)$ . For TC algorithm, there are two expanded functions:  $GET\_NEIGHBOR(S_{source})$  is used to get the neighbors of  $v_{source}$ , while  $GET\_TRIANGLE(S_{source})$  is used to get the triangle counter of  $v_{source}$ .

GTC is presented in Algorithm 1. A sequence of events (*EventStream*) is the input. For each event  $e \in EventStream$ , two adjacent sets are initialed first (lines 3-4):  $adjacentSet_1$  stores the neighbor vertices of  $v_{source}$ , and  $adjacentSet_2$  stores the neighbor vertices of  $v_{target}$ . After  $v_{source}$  and  $v_{target}$  are retrieved from  $e$  (line 5), based on FGL, these two vertices are locked to avoid potential update conflicts (lines 6-7). The next step (lines 9-19) is to compute the common adjacent neighbors of  $v_{source}$  and  $v_{target}$ . If  $f_{source}$  is not null, the set of adjacent neighbors  $adjacentSet_1$  for  $v_{source}$  is the union of  $v_{target}$  and the previous neighbors of  $v_{source}$  (lines 11-12). Otherwise, the  $v_{target}$  would be the first neighbor of  $v_{target}$  (lines 13-14). The computation of  $adjacentSet_2$  for  $v_{target}$  is similar (lines 15-18). We use  $intersectSet$  to store those common neighbor vertices (line 19). For each vertex in  $intersectSet$ , its triangle counts can be increased or decreased by one according to the event type (lines 20-27). Similarly, the factor of  $v_{source}$  and  $v_{target}$  can be updated based on event type (lines 28-37). When these update operations are finished, FGL will release the lock of  $v_{source}$  and  $v_{target}$ .

Fig. 1 shows an example of GraphFlow-based Triangle Count. In this example, suppose the latest graph state is as shown in Fig. 1(a). When an edge is added as shown in Fig.

1(b), we can calculate the common adjacent neighbors for  $v_{source}$  and  $v_{target}$  as shown in Fig. 1(c). Finally, the triangle counts of  $v_{source}$ ,  $v_{target}$  and their common adjacent neighbors can be updated.

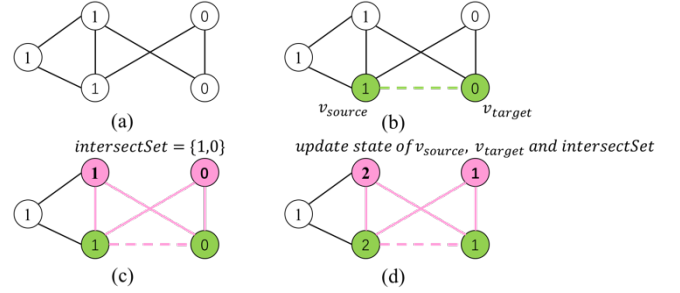


Fig. 1 GraphFlow-based Triangle Count Example.

#### Algorithm 1: GraphFlow-based Triangle Count (GTC)

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1: procedure DTC(EventStream)
2:   for all  $e \in EventStream$  do
3:      $adjacentSet_1 \leftarrow \emptyset$ 
4:      $adjacentSet_2 \leftarrow \emptyset$ 
5:      $(v_{source}, v_{target}) \leftarrow GET\_VALUE(e)$ 
6:      $FGL\_LOCK(v_{source})$ 
7:      $FGL\_LOCK(v_{target})$ 
8:      $UPDATE(e)$ 
9:      $f_{source} \leftarrow GET\_STATE(v_{source})$ 
10:     $f_{target} \leftarrow GET\_STATE(v_{target})$ 
11:    if  $f_{source} \neq \emptyset$  then
12:       $adjacentSet_1 \leftarrow GET\_NEIGHBOR(f_{source}) \cup \{v_{target}\}$ 
13:    else
14:       $adjacentSet_1 \leftarrow \{v_{target}\}$ 
15:    if  $f_{target} \neq \emptyset$  then
16:       $adjacentSet_2 \leftarrow GET\_NEIGHBOR(f_{target}) \cup \{v_{source}\}$ 
17:    else
18:       $adjacentSet_2 \leftarrow \{v_{source}\}$ 
19:     $intersectSet \leftarrow adjacentSet_1 \cap adjacentSet_2$ 
20:     $type \leftarrow GET\_TYPE(e)$ 
21:    for all  $v \in intersectSet$  do
22:       $f_v \leftarrow GET\_STATE(v)$ 
23:       $t \leftarrow GET\_TRIANGLE(f_v)$ 
24:       $N \leftarrow GET\_NEIGHBOR(f_v)$ 
25:      if  $type = ADD$  then  $f_v \leftarrow (v, N, t+1)$ 
26:      elseif  $type = DELETE$  then  $f_v \leftarrow (v, N, t-1)$ 
27:       $SET\_STATE(v, f_v)$ 
28:     $t_{source} \leftarrow GET\_TRIANGLE(f_{source})$ 
29:     $t_{target} \leftarrow GET\_TRIANGLE(f_{target})$ 
30:    if  $type = ADD$  then
31:       $f_{source} \leftarrow (v_{source}, adjacentSet_1, t_{source} + |intersectSet|)$ 
32:       $f_{target} \leftarrow (v_{target}, adjacentSet_2, t_{target} + |intersectSet|)$ 
33:    elseif  $type = DELETE$  then
34:       $f_{source} \leftarrow (v_{source}, adjacentSet_1, t_{source} - |intersectSet|)$ 
35:       $f_{target} \leftarrow (v_{target}, adjacentSet_2, t_{target} - |intersectSet|)$ 
36:     $SET\_STATE(v_{source}, f_{source})$ 
37:     $SET\_STATE(v_{target}, f_{target})$ 
38:     $FGL\_UNLOCK(v_{source})$ 
39:     $FGL\_UNLOCK(v_{target})$ 

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