

yield_strength_prediction

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2 Solid solution strength

```
[1]: import math
```

```
[2]: # Coefficients for Solid solution strength
beta_Al=225
beta_Co=39.4
beta_Cr=337
beta_Mo=1015
beta_Ti=775
```

```
[3]: # Composition of the alloy in atom fraction - As built
c_Al=3.2155E-02
c_Co=9.8145E-02
c_Cr=2.2248E-01
c_Mo=5.1244E-02
c_Ti=2.5368E-02
```

$$\sigma_{ss} = (1 - f) \left(\sum_i (\beta_i c_i^{1/2})^2 \right)^{1/2}$$

for as-built, we take f as 0 and for aged it is 0.17, calculated from Thermo-Calc

```
[4]: f=0.17
```

```
[5]: # Composition of gamma matrix obtained from Thermo-Calc Eqm calculation at 788 C
c_age_Al=1.56810E-02
c_age_Co=1.11295E-01
c_age_Cr=2.65970E-01
c_age_Mo=6.15777E-02
c_age_Ti=4.46602E-03
```

```
[6]: alist=[beta_Al,beta_Co,beta_Cr,beta_Mo,beta_Ti]
clist=[c_Al,c_Co,c_Cr,c_Mo,c_Ti]
c_age_list=clist=[c_age_Al,c_age_Co,c_age_Cr,c_age_Mo,c_age_Ti]
```

```
temp=0
temp_age=0
for i in range(len(alist)):
    temp = temp + (alist[i]*alist[i]*clist[i])
    temp_age = temp_age + (alist[i]*alist[i]*c_age_list[i])
```

```
[7]: y_ss = math.sqrt(temp)
y_age_ss=(1-f)*math.sqrt(temp_age)
print(y_ss)
print(y_age_ss)
```

```
311.91963180633564
258.8932943992586
```

3 Grain Boundary strengthening

$$\sigma_D = \kappa D^{-1/2}$$

```
[8]: kappa=370 #MPa/sqrt(mu m)
```

```
[9]: # equivalent circle diameter (from EBSD) in microns
d_67=25
d_90=29
d_137=24
```

```
[10]: y_d_67= kappa*(d_67**-0.5)
y_d_90= kappa*(d_90**-0.5)
y_d_137= kappa*(d_137**-0.5)

print(y_d_67)
print(y_d_90)
print(y_d_137)
```

```
74.0
68.70727512550918
75.52593373581466
```

4 Dislocation Strengthening

$$\sigma_\rho = M\alpha b G \sqrt{\rho}$$

```
[11]: # Dislocation Density obtained from EBSD data
rho_67=3.2e+14
rho_90=3.1e+14
rho_137=4.6e+14
```

```
[12]: M=2.2 #Obtained from EBSD
      G=82 #GPa
      b=0.248 #nm
      alpha=0.3
```

```
[13]: y_rho_67=M*alpha*G*b*math.sqrt(rho_67)*1e-6 #Convert N/m2 to MPa
      y_rho_90=M*alpha*G*b*math.sqrt(rho_90)*1e-6 #Convert N/m2 to MPa
      y_rho_137=M*alpha*G*b*math.sqrt(rho_137)*1e-6 #Convert N/m2 to MPa
```

```
[14]: print(y_rho_67)
      print(y_rho_90)
      print(y_rho_137)
```

```
240.0957419015006
236.31447028114044
287.8646819060928
```

5 Precipitation Strengthening

$$\sigma_p = \frac{M\gamma_{APB}}{2b} \frac{l}{\Lambda + d}$$

$$l = d, \text{ if } d < d_m \quad l = (d^2 - (d - d_m)^2)^{1/2}, \text{ if } d \geq d_m$$

$$d_m = \frac{\mu b^2}{\gamma_{APB}}$$

$$\Lambda = \max\{\lambda, L - l\}$$

$$\lambda = L \left(\frac{2T}{d\gamma_{APB}} \right)^{1/2}$$

$$T = 0.5\mu b^2$$

$$L = d\left(\frac{\pi}{6f}\right)^{1/2}$$

```
[15]: mu=82 #GPa
      b=0.248 #nm
      gamma=0.28 #J/m2
      d=26 #nm

[16]: dm=mu*b*b/gamma

[17]: if d<dm:
      l=d
      else:
      l=math.sqrt((d*d)-(d-dm)**2)

[18]: T=0.5*mu*b*b*1e-9 #N/m

[19]: L=d*math.sqrt(math.pi/(6*f))

[20]: lamda=L*math.sqrt(2*T/(1e-9*d*gamma))

[21]: LL=max(L-l,L)

[22]: y_p=1e3*M*gamma*l/(2*b*(LL+d)) #converts to MPa
      print(y_p)
```

428.9914702429991

6 Total Yield Strength - Add all the contributions

```
[23]: # For As-built
      y_67= y_ss+y_d_67+y_rho_67
      y_90= y_ss+y_d_90+y_rho_90
      y_137= y_ss+y_d_137+y_rho_137

[24]: print(y_67)
      print(y_90)
      print(y_137)
```

```
626.0153737078363
616.9413772129852
675.3102474482431
```

```
[25]: aged_67= y_age_ss+y_d_67+y_rho_67+y_p
aged_90= y_age_ss+y_d_90+y_rho_90+y_p
aged_137= y_age_ss+y_d_137+y_rho_137+y_p
```

```
[26]: print(aged_67)
print(aged_90)
print(aged_137)
```

```
1001.9805065437583
992.9065100489074
1051.2753802841653
```

```
[27]: #Relative Error Percentage
y_exp=[654,674,656,1001,1010,986]
y_pred=[y_67,y_90,y_137,aged_67,aged_90,aged_137]

for i in range(len(y_exp)):
    print(100*(y_exp[i]-y_pred[i])/y_exp[i])
```

```
4.278994845896596
8.465671036649077
-2.9436352817443754
-0.09795270167415965
1.6924247476329286
-6.620221124154695
```

```
[28]: import matplotlib.pyplot as plt
```

```
[29]: # X axis
x=[1,2,3,4,5,6]
xlist=['67$^\circ$ As-built','90$^\circ$ As-built','137$^\circ$
↪As-built','67$^\circ$ Aged','90$^\circ$ Aged','137$^\circ$ Aged']
```

```
[30]: # Y-axis
ys=[654,674,656,1001,1010,986]
pred=[y_67,y_90,y_137,aged_67,aged_90,aged_137]
```

```
[31]: ys_err=[37,3,13,18,28,28]
```

```
[32]: # Template for paper quality figures
plt.rcParams['font.family'] = 'sans-serif'
plt.rcParams['font.sans-serif'] = ['Arial']
plt.rcParams['font.size'] = 16
plt.rcParams['axes.linewidth'] = 1.1
```

```
plt.rcParams['axes.labelpad'] = 4.0
plot_color_cycle = plt.cycler('color', ['000000', '0000FE', 'FE0000', '008001', 'FD8000', '8c564b',
                                         'e377c2', '7f7f7f', 'bcbd22', '17becf'])
plt.rcParams['axes.prop_cycle'] = plot_color_cycle
plt.rcParams.update({"figure.figsize" : (10.0,5.0),
                    "figure.subplot.left" : 0.177, "figure.subplot.right" : 0.946,
                    "figure.subplot.bottom" : 0.156, "figure.subplot.top" : 0.965,
                    "axes.autolimit_mode" : "round_numbers",
                    "lines.markersize" : 10,
                    "lines.markerfacecolor" : "none",
                    "lines.markeredgewidth" : 0.8})
```

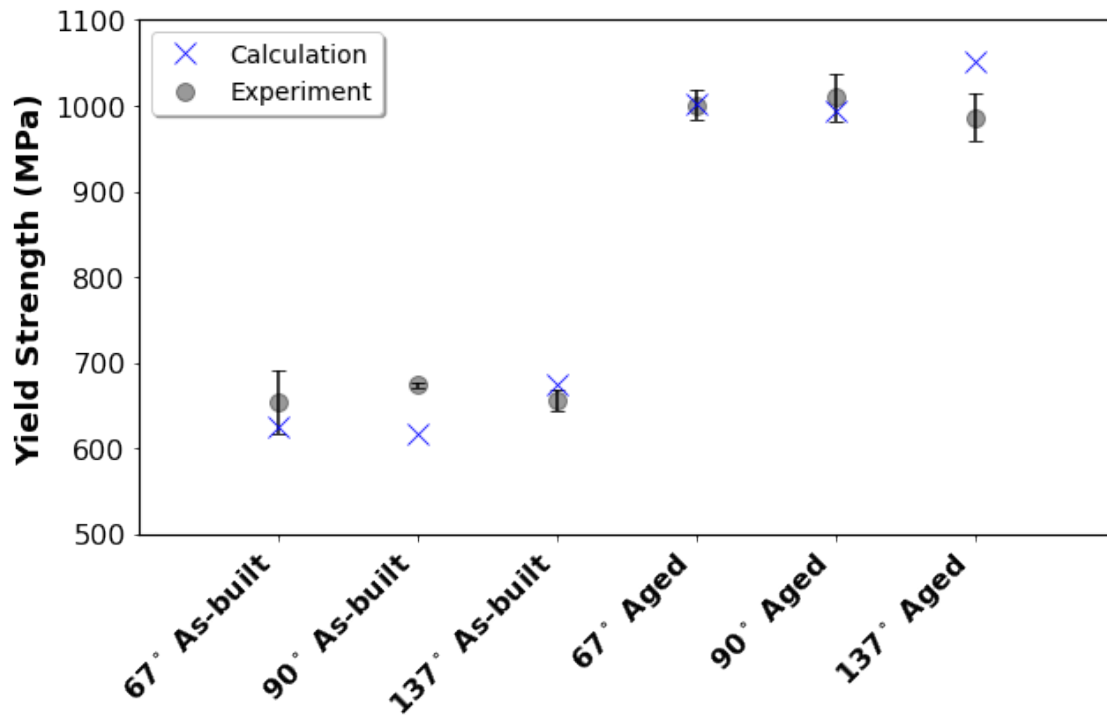
[33]: pred

```
[33]: [626.0153737078363,
      616.9413772129852,
      675.3102474482431,
      1001.9805065437583,
      992.9065100489074,
      1051.2753802841653]
```

```
[34]: plt.scatter(x,ys,label="Experiment",alpha=0.4,marker="o",linestyle="None")
plt.errorbar(x,ys,yerr=ys_err,capsize=4,linestyle="None")
plt.plot(x,pred,"bx",label="Calculation",markersize=12)
plt.xticks(x,xlist,rotation=45,ha="right",fontweight="bold")
plt.legend(loc='upper left',
          ncol=1, fancybox=True, shadow=True,fontsize=14)
plt.ylabel("Yield Strength (MPa)",fontsize=18,fontweight="bold")
plt.savefig("mech_prop_prediction.jpg",bbox_inches='tight',dpi=400)
```

[34]: Text(0, 0.5, 'Yield Strength (MPa)')

```
findfont: Font family ['sans-serif'] not found. Falling back to DejaVu Sans.
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```



[]: