Índice	
1. Setup	1
2. STL 2.1. <algorithm.h></algorithm.h>	2 2 2
3. Range queries	3
4. Grafos	4
5. Matemática 5.1. Aritmética 5.2. Teoria de numeros 5.3. Geometria	4 4 5 6
6.1. Disjoint set union	6
7. Sin categorizar	7
8. Brainstorming	7

. Setup

```
Template corto
#include <bits/stdc++.h>
using namespace std;
#define forr(i,a,b) for(int i = int(a); i < int(b); i++)</pre>
#define all(v)
                     begin(v), end(v)
#define mp(a,b)
                     make_pair(a,b)
#define pb
                     push_back
int main () {
   return 0;
}
Template completo
#include <bits/stdc++.h>
using namespace std;
#define forall(it,v) for (auto it = begin(v); it != end(v); it++)
#define forr(i,a,b) for(int i = int(a); i < int(b); i++)</pre>
#define forn(i,n)
                     forr(i,0,n)
#define all(v)
                     begin(v), end(v)
#define mp(a,b)
                     make_pair(a,b)
#define pb
                     push_back
#define fst
                     first
#define snd
                      second
#define endl
                     '\n'
                     cerr << #x << " = " << (x) << endl
#define dprint(x)
#define raya
                      cerr << "======== " << endl
#define templT
                     template <class T>
#define templAB
                     template <class A, class B>
templAB ostream& operator << (ostream& o, pair<A,B>& p) { return o <<
   → p.first << " " << p.second; }</pre>
templT ostream& operator << (ostream& o, vector <T>& v) { forall(it, v
   → ) { o << *it << " "; } return o; }</pre>
int main () { ios::sync_with_stdio(0); cin.tie(0); cout.tie(0);
   return 0;
}
Makefile
CC = g++
CPPFLAGS = -Wall -g \
```

-fsanitize=undefined -fsanitize=bounds \

```
-std=c++17 -00

comp.sh: Compilar $1 y mostrar primeras $2 lineas de error

clear

make -s $1 2>&1 | head -$2

run.sh: Correr $1 con el input $2

clear

make -s $1 && ./$1 < $2
```

2. STL

2.1. <algorithm.h>

Funciones que modifican rangos

Función	Params	Ejemplo
copy	first last result	<pre>B.resize(A.size()); copy(all(A), B)</pre>
fill	first last val	memo.resize(MAXN); fill(all(memo), -1)
rotate	first middle last	<pre>rotate(begin(A), begin(A) + 3, end(A));</pre>

Búsqueda binaria en vector ordenado

```
templT int primer_igual (vector<T>& arr, T x) {
    auto it = lower_bound(all(arr), x);
    if (it == arr.end() || *it != x) return -1;
    return it - arr.begin();
}
templT int ultimo_igual (vector < T > & arr, T x) {
    if (arr.begin() == arr.end()) return -1;
    auto it = prev(upper_bound(all(arr), x));
    if (*it != x) return -1;
    return it - arr.begin();
}
templT int ultimo_menor (vector<T>& arr, T x) {
    if (arr.begin() == arr.end()) return -1;
    auto it = prev(lower_bound(all(arr), x));
    if (*it >=) return -1;
    return it - arr.begin();
}
templT int primer_mayor (vector < T > & arr, T x) {
    auto it = upper_bound(all(arr), x);
    if (it == arr.end()) return -1;
    return it - arr.begin();
```

Operaciones de conjuntos con vectors ordenados (lineal)

```
// Siempre hacer resize al final asi:

vector<int> A = { 5, 10, 15, 20, 25};
vector<int> B = {10, 20, 30, 40, 50};

vector<int> U(A.size() + B.size());

auto it = set_union(all(A), all(B), begin(U));

U.resize(it - U.begin());
```

Función	Descripción
set_union	Unión
set_intersection	Intersección
set_difference	Elementos que están en el primero y no en el segundo
set_symmetric_difference	Elementos que están en uno pero no los dos (como el xor)

2.2. Set

Indexed set y multiset

Intervalos consecutivos

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
templT struct IndexedSet {
   tree<
       T, null_type, less<T>,
        rb_tree_tag, tree_order_statistics_node_update
   > s:
    void add (T
                 x) \{ ms.insert(x); \}
        idx (T
                 x) { return ms.order_of_key(x); }
    bool has (T x) { return ms.find(x) != ms.end(); }
         ith (int i) { return *ms.find_by_order(i); }
};
templT struct IndexedMultiset {
   int t = 0; tree<</pre>
        pair<T, int>, null_type, less<pair<T, int>>,
        rb_tree_tag, tree_order_statistics_node_update
    > ms;
                 x) { ms.insert(mp(x, t++)); }
    void add (T
                 x) { return ms.order_of_key(mp(x, -1)); }
        nle (T
                 x) { return ms.order_of_key(mp(x, INT_MAX)); }
    int nleq (T
        cnt (T x) { return nleq(x) - nle(x); }
         ith (int i) { return (*ms.find_by_order(i)).fst; }
};
```

```
struct IntervalosConsecutivos {
    set <int > I;
    map<int, int> L;
    IntervalosConsecutivos (int i, int j) {
        I.insert(i);
        I.insert(j);
        L[j - i] ++;
    void cortar (int k) {
        int i = *prev(I.lower_bound(k));
        int j = *(I.lower_bound(k));
        L[j - i]--;
        if (L[j - i] == 0) L.erase(j - i);
        L[k - i] ++;
        L[i - k] ++;
        I.insert(k);
    }
    int max_intervalo () {
        return (*L.rbegin()).fst;
    }
};
    Range queries
Prefix/dff arrays
templT vector<T> diff_array (vector<T>& A) {
    vector <T> D(A.size());
    D[0] = A[0];
    forn(i, D.size() - 1) D[i+1] = A[i+1] - A[i];
    return D;
}
// Aplica +x en A[i] ... A[j]
templT void update_diff_array (vector < T > & D, int i, unsigned j, T x)
   \hookrightarrow {
    D[i] += x;
    if (j + 1 < D.size()) D[j+1] -= x;</pre>
templT vector<T> prefix_array (vector<T>& A) {
    vector <T> P(A.size());
    P[0] = A[0];
    forn(i, P.size() - 1) P[i+1] = P[i] + A[i+1];
    return P;
}
```

// Retorna A[i] + ... + A[j]

templT T query_prefix_array (vector<T>& P, int i, int j) {

```
T res = P[j];
    if (i > 0) res -= P[i-1];
    return res;
}
Segment tree range query point set
templT struct SegmentTree {
    vector < T > & arr; int N;
    // Elegir operacion y neutro
    T id:
    T op (T a, T b) { return 0; }
    vector <T> t;
    void make () {
        t.resize(N \ll 1); forn(i,N) t[i+N] = arr[i];
        for (int i = N - 1; i; i--) t[i] = op(t[i << 1], t[i << 1|1]);
    void set (int i, T v) {
        for(t[i += N] = v; i > 1; i >>= 1) t[i>>1] = op(t[i], t[i^1])
    }
    T query (int 1, int r) {
        T res = id;
        for (1 += N, r += N; 1 < r; 1 >>= 1, r >>= 1) {
            if (1\&1) res = op(res, t[1++]);
            if (r\&1) res = op(res, t[--r]);
        } return res;
};
// Usar asi:
vector < int > A = {...}:
SegmentTree < int > segment_tree = {A, A.size(), 0};
segment_tree.make();
Sparse table
// Operacion asociativa IDEMPOTENTE
#define log2fl(x) (x ? 63 - __builtin_clzll(x) : -1)
templT struct SparseTable {
    vector < T > & arr; int N;
    vector < vector < T >> st;
    // Modificar operacion
    T op (T a, T b) { return min(a,b); }
    void make () {
        st.resize(20, vector<T>(N));
        st[0] = arr; forn(w,19) forn(i,N - (1 << (w+1)) - 1)
            st[w+1][i] = op(st[w][i], st[w][i + (1 << w)]);
    }
```

bag.pop();

```
T query (int i, int j) {
        int w = log2fl(j - i + 1);
        return op(st[w][i], st[w][j - (1 << w) + 1]);</pre>
    }
};
// Usar asi:
vector < int > A = {...};
SparseTable < int > sparse_table = {A, A.size()};
sparse_table.make();
    Grafos
Toposort
using AdjList = vector<vector<int>>;
vector<int> Toposort (AdjList& G) {
    int N = G.size();
    vector<int> indegree(N), visit(N), res;
    forn(u, N) for (int v : G[u]) indegree[v]++;
    // Elegir crierio de priorizacion cambiando el orden en el que se

→ sacan

    // (por defecto el menor)
    using Bag = priority_queue<int, vector<int>, greater<int>>;
    forn(u, N) if(indegree[u] == 0) bag.push(u);
    while (bag.size()) {
        int u = bag.top();
        bag.pop();
        res.push_back(u);
        for (int v : G[u]) {
            indegree[v]--;
            if (indegree[v] == 0) bag.push(v);
        }
    }
    return res;
Bipartite check
using AdjList = vector<vector<int>>;
bool EsBipartito (AdjList& G) {
    vector < int > color(G.size(), -1);
    color[0] = 0;
    queue < int > bag;
```

for (bag.push(0); bag.size();) {
 int u = bag.front();

```
for (int v : G[u]) {
            if (color[u] == color[v]) return false;
            if (color[v] == -1) {
                color[v] = 1 - color[u];
                bag.push(v);
            }
        }
    }
    return true:
}
Encontrar puentes y articulaciones
using AdjList = vector<vector<int>>;
using Edge = pair<int, int>;
pair < vector < Edge > , vector < int >> GetPuentesArticulaciones (AdjList& G)
   int N = G.size(), time = 0;
   vector < bool > visitado(N);
   vector<int> tin(N, -1), tlow(N, -1), articulaciones;
   vector < Edge > puentes;
   function < void(int, int) > dfs = [&](int u, int p) -> void {
      visitado[u] = true;
      tin[u] = tlow[u] = time++;
      int hijos = 0;
      for (int v : G[u]) {
         if (v == p) continue;
         if (visitado[v]) tlow[u] = min(tlow[u], tin[v]);
         else {
            dfs(v, u);
            hijos++;
            tlow[u] = min(tlow[u], tlow[v]);
            if (tlow[v] > tin[u]) puentes.pb({u,v});
            if (tlow[v] >= tin[u] && p != -1) articulaciones.pb(u);
         }
      }
      if (p == -1 && hijos > 1) articulaciones.pb(u);
   };
   forn(r, N) if (!visitado[r]) dfs(r, -1);
   return mp(puentes, articulaciones);
}
```

5. Matemática

5.1. Aritmética

Techo de la división

```
#define ceildiv(a,b) ((a + b - 1) / b)
```

```
Piso de la raiz cuadrada
using 11 = long long;
ll isqrt (ll x) {
    11 s = 0:
    for (11 k = 1 \ll 30; k; k \gg 1)
        if ((s+k) * (s+k) <= x) s += k;
    return s;
}
Piso del log2
       #define log2fl(x) (x ? 63 - _builtin_clzll(x) : -1)
Aritmética en Zp
using ll = long long;
const 11 mod = 1e9 + 7;
11 resta_mod (11 a, 11 b) { return (a - b + mod) % mod; }
ll pow_mod (ll x, ll n) {
    11 \text{ res} = 0;
    while (n) {
        if (n % 2) res = res * x % mod;
        n /= 2;
        x = x * x \% mod;
    } return res;
ll div_mod (ll a, ll b) { return a * pow_mod(b, mod - 2) % mod; }
      Teoria de numeros
Criba
struct Criba {
    bool c[1000001]; vector<int> p;
    Criba () {
        p.reserve(1<<16);
        for (int i = 2; i <= 1000000; i++) if (!c[i]) {
            for (int j = 2; i*j \le 1000000; j++) c[i*j] = 1;
        }
    }
    bool isprime (int x) {
        for (int i = 0, d = p[i]; d*d \le x; d = p[++i])
```

```
if (!(x % d)) return false;
         return x \ge 2;
    }
};
Phollards Rho
using ll = long long;
11 gcd(ll a, ll b){return a?gcd(b %a, a):b;}
11 mulmod (11 a, 11 b, 11 c) { //returns (a*b)%c, and minimize
    \hookrightarrow overfloor
        11 x = 0, y = a\%c;
         while (b > 0){
                 if (b \% 2 == 1) x = (x+y) \% c;
                 y = (y*2) \% c;
                 b /= 2;
        return x % c;
}
ll expmod (ll b, ll e, ll m)\{//0(\log b)\}
        if(!e) return 1;
        11 q = expmod(b, e/2, m); q = mulmod(q, q, m);
        return e %2? mulmod(b,q,m) : q;
}
bool es_primo_prob (ll n, int a)
        if (n == a) return true;
        11 s = 0.d = n-1:
         while (d \% 2 == 0) s++, d/=2;
        11 x = expmod(a,d,n);
        if ((x == 1) || (x+1 == n)) return true;
        forn (i, s-1) {
                 x = mulmod(x, x, n);
                 if (x == 1) return false;
                 if (x+1 == n) return true:
        return false;
}
bool rabin (ll n){ //devuelve true si n es primo
         if (n == 1)
                         return false;
         const int ar[] = \{2,3,5,7,11,13,17,19,23\};
        forn (j,9)
                 if (!es_primo_prob(n,ar[j]))
                         return false:
```

```
return true;
11 \text{ rho}(11 \text{ n})
    if( (n & 1) == 0 ) return 2;
    11 x = 2 , y = 2 , d = 1;
    11 c = rand() % n + 1;
    while( d == 1 ){
        x = (mulmod(x, x, n) + c) %n;
        y = (mulmod(y, y, n) + c) %n;
        y = (mulmod(y, y, n) + c) %n;
        if(x - y >= 0) d = gcd(x - y, n);
        else d = gcd(y - x, n);
    return d==n? rho(n):d;
}
map<ll,ll> prim;
void factRho (ll n){ //O (lg n)^3. un solo numero
        if (n == 1) return;
        if (rabin(n)){
                prim[n]++;
                return:
        }
        11 factor = rho(n);
        factRho(factor);
        factRho(n/factor);
}
     Geometria
Template geometria
```

```
Sca norma2 (Vec p) { return p.x * p.x + p.y * p.y; }
     Estructuras locas
6.1. Disjoint set union
struct DSU {
    vector < int > p, w; int nc;
    DSU (int n) {
        nc = n, p.resize(n), w.resize(n);
        forn(i,n) p[i] = i, w[i] = 1;
    int get (int x) { return p[x] == x ? x : p[x] = get(p[x]); }
    void join (int x, int y) {
        x = get(x), y = get(y);
        if (x == y) return;
        if (w[x] > w[y]) swap(x,y);
        p[x] = y, w[y] += w[x];
    bool existe_camino (int x, int y) { return get(x) == get(y); }
};
6.2. Binary trie
struct BinaryTrieVertex { vector<int> next = {-1, -1}; };
using BinaryTrie = vector < BinaryTrieVertex >;
void binary_trie_add (BinaryTrie& trie, int x) {
    int v = 0:
    for (int i = 31; i >= 0; i--) {
        bool b = (x & (1 << i)) > 0;
        if (trie[v].next[b] == -1) {
            trie[v].next[b] = trie.size();
            trie.emplace_back();
        v = trie[v].next[b];
    }
}
int binary_trie_max_xor (BinaryTrie& trie, int x) {
    int v = 0, res = 0;
    for (int i = 31; i >= 0; i--) {
        bool b = (x & (1 << i)) > 0;
        if (trie[v].next[!b] != -1) {
            v = trie[v].next[!b];
            if (!b) res |= (1 << i);</pre>
```

else {

```
v = trie[v].next[ b];
    if ( b) res |= (1 << i);
} return res;
}
// Inicializar asi:
BinaryTrie trie(1);</pre>
```

7. Sin categorizar

Búsqueda binaria sobre un predicado

```
using ll = long long;

// Si existe, el primer i donde pred(i) == true

// Si es todo false, devuelve d

ll bsearch (ll i, ll j, bool (*pred)(ll), ll d) {
    while (!(i + 1 == j)) {
        ll m = i + ((j - i) >> 1);
        pred(m) ? j = m : i = m;
    }
    if (pred(i)) return i;
    if (pred(j)) return j;
    return d;
}
Enumerar subconjuntos de un conjuto con bitmask
```

Hashing Rabin Karp

```
using ll = long long;
const ll primo = 27, MAX_PRIME_POW = 1e6;
ll prime_pow[MAX_PRIME_POW];
```

8. Brainstorming

- Graficar como puntos/grafos
- Pensarlo al revez
- ¿Que propiedades debe cumplir una solución?
- Si existe una solución, ¿existe otra más simple?
- ¿Hay elecciones independientes?
- ¿El proceso es parecido a un algoritmo conocido?
- Si se busca calcular f(x) para todo x, calcular cuánto contribuye x a f(y) para los otros y
- Definiciones e identidades: ¿que significa que un array sea palindromo? (ejemplo)