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2. Estructuras

2.1. Prefix table

```

1 template<typename T>
2 class PTable {
3     vec<T> pt;
4     T opr (T a, T b) { return a + b; }
5     T inv (T a, T b) { return a - b; }
6     public:
7     PTable (vec<T>& a) {
8         pt.resize(a.size());
9         rep(i,a.size()) pt[i] = !i ? a[i] : opr(pt[i-1], a[i]);
10    }
11    T q (int i, int j) { return (--i < 0) ? pt[j] : inv(pt[j], pt[i]); }
12 };

```

2.2. Sparse table

Operacion asociativa *idempotente*.

```

1 template<typename T>
2 class STable {
3     vec<vec<T>> st;
4     T op (T a, T b) { return min(a,b); }
5     public:
6     STable (vec<T>& a) {
7         st.resize(20, vec<T>(a.size()));
8         st[0] = a; scn(w,1,19) scn(i,0,a.size()-(1<<w))
9             st[w][i] = op(st[w-1][i], st[w-1][i+(1<<(w-1))]);
10    }
11    T q (int i, int j) {
12        int w = log2fl(j - i + 1);
13        return op(st[w][i], st[w][j - (1 << w) + 1]);
14    }
15 };

```

2.3. Segment tree

```

1 const int MAXN = 1<<20; // ~1e6
2
3 long long ST[2*MAXN];
4

```

```

5 long long querie(int nodo, int left, int right, int a, int b) {
6     if (left >= b || right <= a) return 0;
7     if (left >= a && right <= b) return ST[nodo];
8     int m = (left + right) / 2;
9     long long q1 = querie(nodo*2,left,m,a,b);
10    long long q2 = querie(nodo*2+1,m,right,a,b);
11    return q1 + q2;
12 }
13 void update(int p, long long val) {
14     ST[p] = val;
15     for (p = p/2; p > 0; p /= 2) ST[p] = op(ST[p*2], ST[p*2+1]);
16 }

```

2.4. Disjiont Set Union

```

1 struct DSU {
2     vec<int> p, w; int nc;
3     DSU (int n) { nc = n; p.resize(n); w.resize(n); rep(i,n) { p[i] = i,
4         w[i] = 1; } }
5     int get (int x) { return p[x] == x ? x : p[x] = get(p[x]); }
6     void join (int x, int y) {
7         x = get(x), y = get(y);
8         if (x == y) return;
9         if (w[x] > w[y]) swap(x,y);
10        p[x] = y, w[y] += w[x];
11    }
12    bool same (int x, int y) { return get(x) == get(y); }
13 };

```

3. Algos

3.1. Búsqueda Binaria (discreta)

```

1 void dbisect (i64& i, i64& j, bool (*pred)(i64)) {
2     while (!(i + 1 == j)) {
3         i64 m = i + (j - i) / 2;
4         pred(m) ? j = m : i = m;
5     }
6 }
7 pair<bool, i64> dfirsttrue (i64 i, i64 j, bool (*pred)(i64)) {
8     dbisect(i, j, pred);
9     if (pred(i)) return mp(true, i);
10    if (pred(j)) return mp(true, j);

```

```

11     return mp(false, -1L);
12 }
13 pair<bool, i64> dlastfalse (i64 i, i64 j, bool (*pred)(i64)) {
14     dbisect(i, j, pred);
15     if (!pred(j)) return mp(true, j);
16     if (!pred(i)) return mp(true, i);
17     return mp(false, -1L);
18 }

```

4. Strings

5. Geometria

6. Math

6.1. Identidades

$$\sum_{i=0}^n \binom{n}{i} = 2^n$$

$$\sum_{i=0}^n i \binom{n}{i} = n * 2^{n-1}$$

$$\sum_{i=m}^n i = \frac{n(n+1)}{2} - \frac{m(m-1)}{2} = \frac{(n+1-m)(n+m)}{2}$$

$$\sum_{i=0}^n i = \sum_{i=1}^n i = \frac{n(n+1)}{2}$$

$$\sum_{i=0}^n i^2 = \frac{n(n+1)(2n+1)}{6} = \frac{n^3}{3} + \frac{n^2}{2} + \frac{n}{6}$$

$$\sum_{i=0}^n i(i-1) = \frac{6}{6} \left(\frac{n}{2}\right) \left(\frac{n}{2} + 1\right) (n+1) \text{ (doubles)} \rightarrow \text{Sino ver caso impar y par}$$

$$\sum_{i=0}^n i^3 = \left(\frac{n(n+1)}{2}\right)^2 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4} = \left[\sum_{i=1}^n i\right]^2$$

$$\sum_{i=0}^n i^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} - \frac{n}{30}$$

$$\sum_{i=0}^n i^p = \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^p \frac{B_k}{p-k+1} \binom{p}{k} (n+1)^{p-k+1}$$

$$r = e - v + k + 1$$

Teorema de Pick: (Area, puntos interiores y puntos en el borde)

$$A = I + \frac{B}{2} - 1$$

6.2. Criba

```

1 int es_compuesto[maxn]; vector<int> primos;
2 void criba (int n) {
3     forf(i,2,n) if (!es_compuesto[i]) {
4         primos.push_back(i); for (int j = 2; i*j < n; j++) es_compuesto[
5             i*j] = 1;
6     }
7 }

```

7. Grafos

7.1. Toposort

```

1 // Metodo 1: Flood fill con un reverse al final
2 // Facil
3 int topovisit[maxn]; vector<int> topoorder;
4 void topodfs (int u) {
5     topovisit[u] = 1;
6     for (int v : adj[u]) if (!topovisit[v]) {
7         topodfs(v); topoorder.push_back(u);
8     }
9 }
10 void toposort (void) {
11     forf(u,0,n) if(!topovisit[u]) topodfs(u);
12     reverse(topoorder.begin(), topoorder.end());
13 }
14 // Metodo 2: Basado en BFS;
15 // priority_queue permite priorizar entre vertices con mismo nivel
16 // topologico
17 int indegree[maxn]; vector<int> kahnsorder; void kahns () {
18     priority_queue<int, vector<int>, greater<int>> pq;
19     forf(u,0,n) for (int v : adj[u]) indegree[v]++;
20     forf(u,0,n) if (!indegree[u]) pq.push(u);
21     while (!pq.empty()) {
22         int u = pq.top(); pq.pop(); kahnsorder.push_back(u);
23         for (int v : adj[u]) { indegree[v]--; if (!indegree[v]) pq.push(
24             v); }
25     }
26 }

```

7.2. Componentes fuertemente conexas

```

1 const int maxn = int(5e5+1);
2 int n, m; vector<int> adj[maxn];
3
4 deque<int> kosaorder; int kosavisit[maxn];
5 void kosajaru1 (int u) { kosavisit[u] = 1; for (int v : adj[u]) if (!
6     kosavisit[v]) kosajaru1(v); kosaorder.push_front(u); }
7 vector<int> tadj[maxn]; void kosajaru2 (void) { forf(u,0,n) for (int v :
8     adj[u]) tadj[v].push_back(u); }
9 int kosaroot[maxn]; vector<vector<int>> kosacomp;
10 void kosajaru3 (int u, int r) { kosavisit[u] = 1; kosacomp.back().

```

```

    push_back(u); kosaroot[u] = r; for (int v : tadj[u]) if (!kosavisit[
v]) kosajaru3(v, r); }
9 vector<int> adjsc[maxn]; int aristas[maxn]; void kosajaru (void) {
10     forf(u,0,n) if (!kosavisit[u]) kosajaru1(u);
11     kosajaru2(); memset(kosavisit, 0, maxn*sizeof(int));
12     for (int u : kosaorder) if(!kosavisit[u]) { kosacomp.push_back({});
        kosajaru3(u, u); }
13     memset(aristas, -1, sizeof(aristas));
14     for (auto comp : kosacomp) for (int u : comp) for (int v : adj[u]) {
15         int ru = kosaroot[u], rv = kosaroot[v];
16         if (ru != rv && aristas[rv] != ru) aristas[rv] = ru, adjsc[ru].
            push_back(rv);
17     }
18 }

```

7.3. Puentes y puntos de articulación

```

1 const int maxn = int(1e5+1);
2 int n, m; vector<int> adj[maxn];
3
4 vector<pair<int, int>> bridges; vector<int> arts;
5 int dfsdt[maxn], dfslow[maxn], dfsparent[maxn], dfstime, dfsroot,
    rootchildren, isart[maxn];
6 void artdfs (int u) { dfslow[u] = dfsdt[u] = ++dfstime; for (int v :
    adj[u]) {
7     if (!dfsdt[v]) {
8         dfsparent[v] = u; if (u == dfsroot) ++rootchildren; artdfs(v
        );
9         if (dfslow[v] >= dfsdt[u]) isart[u] = 1;
10        if (dfslow[v] > dfsdt[u]) bridges.push_back({u,v});
11        dfslow[u] = min(dfslow[u], dfslow[v]);
12    } else if (v != dfsparent[u]) dfslow[u] = min(dfslow[u], dfsdt[v
        ]);
13    }
14 }
15 void getarts (void) { forf(u,0,n) dfsparent[u] = -1;
16     forf(u,0,n) { if (!dfsdt[u]) { dfsroot = u; rootchildren = 0; artdfs
        (u); isart[dfsroot] = (rootchildren > 1); } }
17     forf(u,0,n) if (isart[u]) arts.push_back(u);
18 }

```

8. Network Flow

9. Template

```

1 #include <bits/stdc++.h>
2 using namespace std;
3 using i64 = int64_t;
4 const int MAXN = 5e5;
5 const i64 INF = LLONG_MAX;
6 #define endl '\n'
7 #define rep(i,N) for (int i = 0; i < int(N); i++)
8 #define scn(k,i,j) for (int k = int(i); k <= int(j); k++)
9 #define forall(it,v) for(auto it = v.begin(); it != v.end(); it++)
10 #define printall(v) forall(x,v){cout << *x << " ";} cout << endl
11 #define vec vector
12 #define pb push_back
13 #define mp make_pair
14 #define printpair(p) cout << "(" << p.fst << ", " << p.snd << ")" <<
    endl
15 #define fst first
16 #define snd second
17 #define log2fl(x) (x ? 63 - __builtin_clzll(x) : -1)
18 typedef vec<vec<int>> adj;
19 typedef vec<vec<pair<int,i64>> > wadj;
20
21 int main (void) {
22     ios::sync_with_stdio(0); cin.tie(0);
23
24     // :)
25
26     return 0;
27 }

```

10. Ayudamemoria

Compilar y correr

```

1 // Makefile
2 CPPFLAGS = -std=c++20 -O0 -Wall -g
3 CC = g++
4 // comp.sh: compilar $1 y mostrar primeras $2 lineas de error
5 rm -f $1

```

```
6 clear
7 make $1 2>&1 | head -$2
8 // run.sh: correr $1 con $2 como input
9 rm -f $1
10 clear
11 make $1 && ./$1 < $2
```