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1. Setup

```
Template corto
#include <bits/stdc++.h>
using namespace std;
#define forr(i,a,b) for(int i = int(a); i < int(b); i++)</pre>
#define all(v)
                     begin(v), end(v)
#define mp(a,b)
                     make_pair(a,b)
#define pb
                     push_back
int main () {
   return 0;
}
Template completo
#include <bits/stdc++.h>
using namespace std;
#define forall(it,v) for (auto it = begin(v); it != end(v); it++)
#define forr(i,a,b) for(int i = int(a); i < int(b); i++)</pre>
#define forn(i,n)
                     forr(i,0,n)
#define all(v)
                     begin(v), end(v)
#define mp(a,b)
                     make_pair(a,b)
#define pb
                     push_back
#define fst
                     first
#define snd
                      second
#define endl
                     '\n'
                     cerr << #x << " = " << (x) << endl
#define dprint(x)
#define raya
                      cerr << "======== " << end1
                     template <class T>
#define templT
#define templAB
                     template <class A, class B>
templAB ostream& operator << (ostream& o, pair<A,B>& p) { return o <<
   → p.first << " " << p.second; }</pre>
templT ostream& operator << (ostream& o, vector <T>& v) { forall(it, v
   → ) { o << *it << " "; } return o; }</pre>
int main () { ios::sync_with_stdio(0); cin.tie(0); cout.tie(0);
   return 0;
}
Makefile
CC = g++
CPPFLAGS = -Wall -g \
-fsanitize=undefined -fsanitize=bounds \
```

```
-std=c++17 -00

comp.sh: Compilar $1 y mostrar primeras $2 lineas de error

clear

make -s $1 2>&1 | head -$2

run.sh: Correr $1 con el input $2

clear

make -s $1 && ./$1 < $2
```

2. STL

2.1. Algorithm

Funciones que modifican rangos

Función	Params	Ejemplo
copy	first last result	<pre>B.resize(A.size()); copy(all(A), B)</pre>
fill	first last val	memo.resize(MAXN); fill(all(memo), -1)
rotate	first middle last	<pre>rotate(begin(A), begin(A) + 3, end(A));</pre>

Búsqueda binaria en vector ordenado

```
templT int primer_igual (vector < T > & arr, T x) {
    auto it = lower_bound(all(arr), x);
    if (it == arr.end() || *it != x) return -1;
    return it - arr.begin();
templT int ultimo_igual (vector < T > & arr, T x) {
    if (arr.begin() == arr.end()) return -1;
    auto it = prev(upper_bound(all(arr), x));
    if (*it != x) return -1;
    return it - arr.begin();
}
templT int ultimo_menor (vector<T>& arr, T x) {
    if (arr.begin() == arr.end()) return -1;
    auto it = prev(lower_bound(all(arr), x));
    if (*it >=) return -1;
    return it - arr.begin();
}
templT int primer_mayor (vector < T > & arr, T x) {
    auto it = upper_bound(all(arr), x);
    if (it == arr.end()) return -1;
    return it - arr.begin();
```

Compresion de coordenadas

using ll = long long;

```
vector<1l> compress (vector<1l>& A) {
   int N = A.size();
   vector<1l> D = A;
   sort(all(D));
   D.resize(unique(all(D)) - D.begin());
   forn(i, N) A[i] = lower_bound(all(D), A[i]) - D.begin();
   return D;
}

Operaciones de conjuntos con vectors ordenados (lineal)

// Siempre hacer resize al final asi:

vector<int> A = { 5, 10, 15, 20, 25};
   vector<int> B = {10, 20, 30, 40, 50};

vector<int> U(A.size() + B.size());

auto it = set_union(all(A), all(B), begin(U));

U.resize(it - U.begin());
```

Función	Descripción
set_union	Unión
set_intersection	Intersección
set_difference	Elementos que están en el primero y no en el segundo
set_symmetric_difference	Elementos que están en uno pero no los dos (como el xor)

2.2. Set y Map

Indexed set y multiset

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

templT struct IndexedSet {
    tree <
        T, null_type, less<T>,
        rb_tree_tag, tree_order_statistics_node_update
    > s;
    void add (T x) { ms.insert(x); }
    int idx (T x) { return ms.order_of_key(x); }
    bool has (T x) { return ms.find(x) != ms.end(); }
    T ith (int i) { return *ms.find_by_order(i); }
};

templT struct IndexedMultiset {
```

```
int t = 0; tree<</pre>
        pair<T, int>, null_type, less<pair<T, int>>,
        rb_tree_tag, tree_order_statistics_node_update
    > ms;
    void add (T x) { ms.insert(mp(x, t++)); }
                 x) { return ms.order_of_key(mp(x, -1)); }
    int nle (T
        nleq (T x) { return ms.order_of_key(mp(x, INT_MAX)); }
        cnt (T x) { return nleq(x) - nle(x); }
         ith (int i) { return (*ms.find_by_order(i)).fst; }
};
Compresion de coordenadas generico
templT map<T, int> Compress (vector<T>& A) {
   map < T , int > ord;
   int n = 0;
   for (auto v : A) ord[v];
   for (auto& e : ord) e.snd = n++;
   return ord;
}
Intervalos consecutivos
struct IntervalosConsecutivos {
    set <int > I:
    map<int, int> L;
    IntervalosConsecutivos (int i, int j) {
        I.insert(i);
       I.insert(j);
        L[j - i] ++;
    void cortar (int k) {
        int i = *prev(I.lower_bound(k));
        int j = *(I.lower_bound(k));
       L[j - i]--;
        if (L[j-i] == 0) L.erase(j-i);
       L[k - i] ++;
       L[j - k] ++;
        I.insert(k);
    }
    int max_intervalo () {
        return (*L.rbegin()).fst;
    }
};
```

3. Range queries

```
Prefix/dff arrays
templT vector<T> diff_array (vector<T>& A) {
    vector<T> D(A.size());
```

```
D[O] = A[O]:
    forn(i, D.size() - 1) D[i+1] = A[i+1] - A[i];
    return D:
}
// Aplica +x en A[i] ... A[j]
templT void update_diff_array (vector < T > & D, int i, unsigned j, T x)
    \hookrightarrow {
    D[i] += x;
    if (j + 1 < D.size()) D[j+1] -= x;</pre>
}
templT vector<T> prefix_array (vector<T>& A) {
    vector <T> P(A.size());
    P[0] = A[0];
    forn(i, P.size() - 1) P[i+1] = P[i] + A[i+1];
    return P:
}
// Retorna A[i] + ... + A[j]
templT T query_prefix_array (vector<T>& P, int i, int j) {
    T res = P[j];
    if (i > 0) res -= P[i-1];
    return res;
}
Segment tree range query point set
templT struct SegmentTree {
    vector < T > & arr; int N;
    // Elegir operacion y neutro
    T id;
    T op (T a, T b) { return 0; }
    vector <T> t;
    void make () {
        t.resize(N << 1); forn(i,N) t[i+N] = arr[i];</pre>
         for (int i = N - 1; i; i--) t[i] = op(t[i<<1], t[i<<1|1]);
    }
    void set (int i, T v) {
         for(t[i += N] = v; i > 1; i >>= 1) t[i>>1] = op(t[i], t[i^1])
    T query (int 1, int r) {
        T res = id;
        for (1 += N, r += N; 1 < r; 1 >>= 1, r >>= 1) {
             if (1\&1) res = op(res, t[1++]);
             if (r\&1) res = op(res, t[--r]);
         } return res;
    }
};
```

```
// Usar asi:
vector < int > A = {...};
SegmentTree < int > segment_tree = {A, A.size(), 0};
segment_tree.make();
Sparse table
// Operacion asociativa IDEMPOTENTE
#define log2fl(x) (x ? 63 - __builtin_clzll(x) : -1)
templT struct SparseTable {
    vector < T > & arr; int N;
    vector < vector < T >> st;
    // Modificar operacion
    T op (T a, T b) { return min(a,b); }
    void make () {
        st.resize(20, vector<T>(N));
        st[0] = arr; forn(w,19) forn(i,N - (1 << (w+1)) - 1)
            st[w+1][i] = op(st[w][i], st[w][i + (1 << w)]);
    }
    T query (int i, int j) {
        int w = log2fl(j - i + 1);
        return op(st[w][i], st[w][j - (1 << w) + 1]);
    }
};
// Usar asi:
vector < int > A = {...};
SparseTable < int > sparse_table = {A, A.size()};
sparse_table.make();
    Grafos
Toposort de un DAG
using AdjList = vector<vector<int>>;
vector<int> Toposort (AdjList& G) {
    int N = G.size();
    vector < int > indegree(N), res;
    forn(u, N) for (int v : G[u]) indegree[v]++;
    // Elegir crierio de priorizacion cambiando el orden en el que se

→ sacan

    // (por defecto el menor)
    using Bag = priority_queue<int, vector<int>, greater<int>>;
```

forn(u, N) if(indegree[u] == 0) bag.push(u);

```
while (bag.size()) {
        int u = bag.top();
        bag.pop();
        res.push_back(u);
        for (int v : G[u]) {
            indegree[v]--;
            if (indegree[v] == 0) bag.push(v);
        }
    }
    return res;
}
DAG condensado
using AdjList = vector<vector<int>>;
AdjList DAGCondensado (AdjList& G) {
   int N = G.size();
   vector < bool > visitado(N);
   vector < int > orden;
   function < void(int) > get_orden = [&](int u) -> void {
      visitado[u] = true;
      for (int v : G[u]) if (!visitado[v]) get_orden(v);
      orden.pb(u);
   };
   forn(u, N) if (!visitado[u]) get_orden(u);
   reverse(all(orden));
   AdjList T(N);
   forn(u, N) for (int v : G[u]) T[v].pb(u);
   vector<int> comp, raiz(N), raices;
   function < void(int) > extraer_comp = [&](int u) -> void {
      visitado[u] = true;
      comp.pb(u);
      for (int v : T[u]) if (!visitado[v]) extraer_comp(v);
   };
   visitado.assign(N, false);
   for (int u : orden) if (!visitado[u]) {
      extraer_comp(u);
      int r = comp.front();
      for (int v : comp) raiz[v] = r;
      raices.pb(r);
      comp.clear();
   }
   // Opcion 1: hacer compresion de coordenadas: O(nlogn) lento
   map < int , int > coords;
```

```
for (int r : raices) coords[r];
   for (auto& e : coords) e.snd = c++;
   AdjList SCC(raices.size());
   forn(u, N) for (int v : G[u]) {
      int ru = coords[raiz[u]], rv = coords[raiz[v]];
      if (ru != rv) SCC[ru].pb(rv);
   }
   return SCC;
   // Opcion 2: no hacer compresion y devolver raices (rapido)
   // AdjList SCC(N);
   // forn(u, N) for (auto [v, w] : G[u]) {
      // int ru = raiz[u], rv = raiz[v];
      // if (ru != rv) SCC[ru].pb({rv, w});
      // else (RC[ru]) += R(w):
  // }
Bipartite check
using AdjList = vector<vector<int>>;
bool EsBipartito (AdjList& G) {
    vector < int > color(G.size(), -1);
    color[0] = 0;
    queue < int > bag;
    for (bag.push(0); bag.size();) {
        int u = bag.front();
        bag.pop();
        for (int v : G[u]) {
            if (color[u] == color[v]) return false;
            if (color[v] == -1) {
                color[v] = 1 - color[u];
                bag.push(v);
            }
        }
    return true;
Encontrar puentes y articulaciones
using AdjList = vector<vector<int>>;
using Edge = pair<int, int>;
pair < vector < Edge >, vector < int >> GetPuentesArticulaciones (AdjList&G)
   \hookrightarrow {
   int N = G.size(), time = 0;
   vector < bool > visitado(N);
   vector < int > tin(N, -1), tlow(N, -1), articulaciones;
   vector < Edge > puentes;
   function < void (int, int) > dfs = [&] (int u, int p) -> void {
```

```
visitado[u] = true;
      tin[u] = tlow[u] = time++;
      int hijos = 0;
      for (int v : G[u]) {
         if (v == p) continue;
         if (visitado[v]) tlow[u] = min(tlow[u], tin[v]);
         else {
            dfs(v, u);
            hijos++;
            tlow[u] = min(tlow[u], tlow[v]);
            if (tlow[v] > tin[u]) puentes.pb({u,v});
            if (tlow[v] >= tin[u] && p != -1) articulaciones.pb(u);
         }
      if (p == -1 && hijos > 1) articulaciones.pb(u);
   };
   forn(r, N) if (!visitado[r]) dfs(r, -1);
   return mp(puentes, articulaciones);
}
```

5. Matemática

5.1. Aritmética

Techo de la división

```
#define ceildiv(a,b) ((a + b - 1) / b)
```

Piso de la raiz cuadrada

```
using ll = long long;

ll isqrt (ll x) {
    ll s = 0;
    for (ll k = 1 << 30; k; k >>= 1)
        if ((s+k) * (s+k) <= x) s += k;
    return s;
}</pre>
```

Piso del log2

```
#define log2fl(x) (x ? 63 - _builtin_clzll(x) : -1)
```

Aritmética en Zp

```
using 11 = long long;
const 11 mod = 1e9 + 7;
```

```
11 resta_mod (11 a, 11 b) { return (a - b + mod) % mod; }
ll pow_mod (ll x, ll n) {
    11 \text{ res} = 0:
    while (n) {
        if (n % 2) res = res * x % mod;
        n /= 2:
        x = x * x \% mod;
    } return res;
}
ll div_mod (ll a, ll b) { return a * pow_mod(b, mod - 2) % mod; }
5.2. Teoria de numeros
Criba
struct Criba {
    bool c[1000001]; vector<int> p;
    Criba () {
        p.reserve(1<<16);
        for (int i = 2; i <= 1000000; i++) if (!c[i]) {</pre>
            for (int j = 2; i*j \le 1000000; j++) c[i*j] = 1;
        }
    }
    bool isprime (int x) {
        for (int i = 0, d = p[i]; d*d \le x; d = p[++i])
            if (!(x % d)) return false;
        return x \ge 2;
    }
};
Phollards Rho
using ll = long long;
11 gcd(ll a, ll b){return a?gcd(b %a, a):b;}
11 mulmod (11 a, 11 b, 11 c) { //returns (a*b) %c, and minimize

    overfloor

        11 x = 0, y = a\%c;
        while (b > 0) {
                if (b \% 2 == 1) x = (x+y) \% c;
                y = (y*2) \% c;
                b /= 2;
        return x % c;
}
ll expmod (ll b, ll e, ll m)\{//0(\log b)
```

```
if(!e) return 1;
        11 q= expmod(b,e/2,m); q=mulmod(q,q,m);
        return e %2? mulmod(b,q,m) : q;
}
bool es_primo_prob (ll n, int a)
        if (n == a) return true;
        11 s = 0, d = n-1;
        while (d \% 2 == 0) s++, d/=2;
        11 x = expmod(a,d,n);
        if ((x == 1) || (x+1 == n)) return true;
        forn (i, s-1){
                x = mulmod(x, x, n);
               if (x == 1) return false:
                if (x+1 == n) return true;
        }
        return false;
}
bool rabin (ll n){ //devuelve true si n es primo
        if (n == 1)
                       return false:
        const int ar[] = \{2,3,5,7,11,13,17,19,23\};
        forn (j,9)
                if (!es_primo_prob(n,ar[j]))
                        return false;
        return true;
}
ll rho(ll n){
    if( (n & 1) == 0 ) return 2;
    11 x = 2 , y = 2 , d = 1;
    11 c = rand() % n + 1;
    while( d == 1 ){
        x = (mulmod(x, x, n) + c) %n;
        y = (mulmod(y, y, n) + c) %n;
        y = (mulmod(y, y, n) + c) %n;
        if(x - y >= 0) d = gcd(x - y, n);
        else d = gcd(y - x, n);
    return d==n? rho(n):d;
}
map<ll,ll> prim;
void factRho (ll n){ //O (lg n)^3. un solo numero
        if (n == 1) return;
        if (rabin(n)){
                prim[n]++;
```

```
return;
}
ll factor = rho(n);
factRho(factor);
factRho(n/factor);
}
```

5.3. Geometria

Template geometria

```
using flt = long double;
const flt EPS = 1e-9;
bool flt_leq (flt a, flt b) { return a < b + EPS; }</pre>
bool flt_eq (flt a, flt b) { return -EPS <= a - b && a - b <= EPS;
   \hookrightarrow }
using Sca = long long;
struct Vec { Sca x, y; };
Vec operator + (Vec a, Vec b) { return { a.x + b.x, a.y + b.y }; }
Vec operator - (Vec a, Vec b) { return { a.x - b.x, a.y - b.y }; }
Sca operator * (Vec a, Vec b) { return a.x * b.x + a.y * b.y; }
Sca operator ^ (Vec a, Vec b) { return a.x * b.y + a.y * b.x; }
bool operator < (Vec a, Vec b) { return (a.x != b.x) ? (a.x < b.x) :
   \hookrightarrow (a.y < b.y); }
ostream& operator << (ostream &o, Vec& p) { auto x = mp(p.x, p.y);

    return o << x; }
</pre>
Sca norma2 (Vec p) { return p.x * p.x + p.y * p.y; }
```

6. Estructuras locas

6.1. Disjoint set union

```
struct DSU {
    vector < int > p, w; int nc;
    DSU (int n) {
        nc = n, p.resize(n), w.resize(n);
        forn(i,n) p[i] = i, w[i] = 1;
    }
    int get (int x) { return p[x] == x ? x : p[x] = get(p[x]); }
    void join (int x, int y) {
        x = get(x), y = get(y);
        if (x == y) return;
        if (w[x] > w[y]) swap(x,y);
        p[x] = y, w[y] += w[x];
    }
    bool existe_camino (int x, int y) { return get(x) == get(y); }
};
```

6.2. Binary trie

```
struct BinaryTrieVertex { vector<int> next = {-1, -1}; };
using BinaryTrie = vector < BinaryTrieVertex >;
void binary_trie_add (BinaryTrie& trie, int x) {
    int v = 0:
    for (int i = 31; i >= 0; i--) {
        bool b = (x & (1 << i)) > 0;
        if (trie[v].next[b] == -1) {
             trie[v].next[b] = trie.size();
             trie.emplace_back();
        v = trie[v].next[b];
    }
}
int binary_trie_max_xor (BinaryTrie& trie, int x) {
    int v = 0, res = 0;
    for (int i = 31; i >= 0; i--) {
        bool b = (x & (1 << i)) > 0;
        if (trie[v].next[!b] != -1) {
             v = trie[v].next[!b];
             if (!b) res |= (1 << i);</pre>
        else {
             v = trie[v].next[ b];
            if ( b) res |= (1 << i);</pre>
    } return res;
}
// Inicializar asi:
BinaryTrie trie(1);
```

7. Sin categorizar

Búsqueda binaria sobre un predicado

```
using ll = long long;

// Si existe, el primer i donde pred(i) == true
// Si es todo false, devuelve d

ll bsearch (ll i, ll j, bool (*pred)(ll), ll d) {
    while (!(i + 1 == j)) {
        ll m = i + ((j - i) >> 1);
        pred(m) ? j = m : i = m;
    }
    if (pred(i)) return i;
```

```
if (pred(j)) return j;
    return d;
}
Enumerar subconjuntos de un conjuto con bitmask
// Imprimir representaciones en binario de todos los numeros "[0,
   \hookrightarrow ..., 2^N-1]"
forn(mask, (1 << N)) {
    forn(i, N) cout << "01"[(mask & (1 << i)) > 0] << "\n"\0\n"[i == N
       → -11:
// Iterar por los bits de cada subconjunto
forn(mask, (1 << N)) {
    forn(i, N) {
        bool on = (mask & (1 << i)) > 0;
        if (on) { ... }
        else { ... }
    }
}
Hashing Rabin Karp
using ll = long long;
const ll primo = 27, MAX_PRIME_POW = 1e6;
11 prime_pow[MAX_PRIME_POW];
void get_prime_pow () {
    prime_pow[0] = 1;
    forn(i, MAX_PRIME_POW) prime_pow[i+1] = prime_pow[i] * primo %
       \hookrightarrow mod;
vector<ll> get_rolling_hash (string& s) {
    vector<ll> rh(s.size() + 1);
    rh[0] = 0;
    // Ojo: es 'A' o 'a' ???
    forn(i, s.size()) rh[i+1] = (rh[i] * primo % mod + s[i] - 'A') %
       \hookrightarrow mod;
    return rh:
ll hash_range_query (vector<ll>& rh, int i, int j) {
```

return (rh[j] - (rh[i] * prime_pow[j - i] % mod) + mod) % mod;

3. Brainstorming

- Graficar como puntos/grafos
- Pensarlo al revez
- ¿Que propiedades debe cumplir una solución?
- Si existe una solución, ¿existe otra más simple?
- ¿Hay electiones independientes?
- ¿El proceso es parecido a un algoritmo conocido?
- \blacksquare Si se busca calcular f(x) para todo x, calcular cuánto contribuye x a f(y) para los otros y
- Definiciones e identidades: ¿que significa que un array sea palindromo? (ejemplo)