Índice	
1. Setup	1
2. STL 2.1. Algorithm	2 2 2
3. Range queries	3
4. Grafos	4
5. Matemática         5.1. Aritmética          5.2. Teoria de numeros          5.3. Geometria	5 5 6
6. Estructuras locas         6.1. Disjoint set union	<b>7</b> 7 7
7. Sin categorizar	7
8. Brainstorming	8

# 1. Setup

```
Template corto
#include <bits/stdc++.h>
using namespace std;
#define forr(i,a,b) for(int i = int(a); i < int(b); i++)</pre>
#define all(v)
                     begin(v), end(v)
#define mp(a,b)
                     make_pair(a,b)
#define pb
                     push_back
int main () {
   return 0;
}
Template completo
#include <bits/stdc++.h>
using namespace std;
#define forall(it,v) for (auto it = begin(v); it != end(v); it++)
#define forr(i,a,b) for(int i = int(a); i < int(b); i++)</pre>
#define forn(i,n)
                     forr(i,0,n)
#define all(v)
                     begin(v), end(v)
#define mp(a,b)
                     make_pair(a,b)
#define pb
                     push_back
#define fst
                     first
#define snd
                      second
#define endl
                     '\n'
                     cerr << #x << " = " << (x) << endl
#define dprint(x)
#define raya
                      cerr << "======== " << end1
                     template <class T>
#define templT
#define templAB
                     template <class A, class B>
templAB ostream& operator << (ostream& o, pair<A,B>& p) { return o <<
   → p.first << " " << p.second; }</pre>
templT ostream& operator << (ostream& o, vector <T>& v) { forall(it, v
   → ) { o << *it << " "; } return o; }</pre>
int main () { ios::sync_with_stdio(0); cin.tie(0); cout.tie(0);
   return 0;
}
Makefile
CC = g++
CPPFLAGS = -Wall -g \
-fsanitize=undefined -fsanitize=bounds \
```

```
-std=c++17 -00

comp.sh: Compilar $1 y mostrar primeras $2 lineas de error

clear

make -s $1 2>&1 | head -$2

run.sh: Correr $1 con el input $2

clear

make -s $1 && ./$1 < $2
```

### 2. STL

### 2.1. Algorithm

Funciones que modifican rangos

Función	Params	Ejemplo
copy	first last result	B.resize(A.size()); copy(all(A), B)
fill	first last val	memo.resize(MAXN); fill(all(memo), -1)
rotate	first middle last	<pre>rotate(begin(A), begin(A) + 3, end(A));</pre>

### Búsqueda binaria en vector ordenado

```
templT int primer_igual (vector<T>& arr, T x) {
    auto it = lower_bound(all(arr), x);
    if (it == arr.end() || *it != x) return -1;
    return it - arr.begin();
templT int ultimo_igual (vector < T > & arr, T x) {
    if (arr.begin() == arr.end()) return -1;
    auto it = prev(upper_bound(all(arr), x));
    if (*it != x) return -1;
    return it - arr.begin();
}
templT int ultimo_menor (vector<T>& arr, T x) {
    if (arr.begin() == arr.end()) return -1;
    auto it = prev(lower_bound(all(arr), x));
    if (*it >=) return -1:
    return it - arr.begin();
}
templT int primer_mayor (vector < T > & arr, T x) {
    auto it = upper_bound(all(arr), x);
    if (it == arr.end()) return -1;
    return it - arr.begin();
```

### Operaciones de conjuntos con vectors ordenados (lineal)

```
// Siempre hacer resize al final asi:

vector<int> A = { 5, 10, 15, 20, 25};
vector<int> B = {10, 20, 30, 40, 50};

vector<int> U(A.size() + B.size());

auto it = set_union(all(A), all(B), begin(U));

U.resize(it - U.begin());
```

Función	Descripción
set_union	Unión
set_intersection	Intersección
set_difference	Elementos que están en el primero y no en el segundo
set_symmetric_difference	Elementos que están en uno pero no los dos (como el xor)

## 2.2. Set y Map

### Indexed set y multiset

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
templT struct IndexedSet {
   tree<
        T, null_type, less<T>,
        rb_tree_tag, tree_order_statistics_node_update
    > s:
    void add (T
                 x) \{ ms.insert(x); \}
    int idx (T
                 x) { return ms.order_of_key(x); }
    bool has (T x) { return ms.find(x) != ms.end(); }
         ith (int i) { return *ms.find_by_order(i); }
};
templT struct IndexedMultiset {
   int t = 0; tree<</pre>
        pair <T, int>, null_type, less <pair <T, int>>,
        rb_tree_tag, tree_order_statistics_node_update
    > ms;
                x) { ms.insert(mp(x, t++)); }
    void add (T
                 x) { return ms.order_of_key(mp(x, -1)); }
        nle (T
    int nleq (T
                 x) { return ms.order_of_key(mp(x, INT_MAX)); }
                 x) { return nleq(x) - nle(x); }
         ith (int i) { return (*ms.find_by_order(i)).fst; }
};
```

### Compresion de coordenadas

```
templT map<T, int> compress (vector<T>& A) {
  map<T, int> ord;
  int n = 0;
  for (auto v : A) ord[v];
  for (auto& e : ord) e.snd = n++;
  return ord;
}
Intervalos consecutivos
struct IntervalosConsecutivos {
    set <int > I;
   map<int, int> L;
   IntervalosConsecutivos (int i, int j) {
       I.insert(i);
       I.insert(j);
       L[i - i]++;
   }
   void cortar (int k) {
       int i = *prev(I.lower_bound(k));
       int j = *(I.lower_bound(k));
       L[i - i]--;
       if (L[j-i] == 0) L.erase(j-i);
       L[k - i]++;
       L[j - k] ++;
       I.insert(k);
   }
   int max_intervalo () {
       return (*L.rbegin()).fst;
   }
};
    Range queries
Prefix/dff arrays
```

```
templT vector<T> prefix_array (vector<T>& A) {
    vector <T> P(A.size());
    P[O] = A[O]:
    forn(i, P.size() - 1) P[i+1] = P[i] + A[i+1];
    return P;
}
// Retorna A[i] + ... + A[j]
templT T query_prefix_array (vector<T>& P, int i, int j) {
    T res = P[i];
    if (i > 0) res -= P[i-1];
    return res;
}
Segment tree range query point set
templT struct SegmentTree {
    vector<T>& arr; int N;
    // Elegir operacion y neutro
    T id;
    T op (T a, T b) { return 0; }
    vector <T> t;
    void make () {
        t.resize(N << 1); forn(i,N) t[i+N] = arr[i];
        for (int i = N - 1; i; i--) t[i] = op(t[i<<1], t[i<<1|1]);
    void set (int i, T v) {
        for(t[i += N] = v; i > 1; i >>= 1) t[i>>1] = op(t[i], t[i^1])
            \hookrightarrow :
    T query (int 1, int r) {
        T res = id;
        for (1 += N, r += N; 1 < r; 1 >>= 1, r >>= 1) {
            if (1\&1) res = op(res, t[1++]);
            if (r\&1) res = op(res, t[--r]);
        } return res;
    }
};
// Usar asi:
vector < int > A = {...};
SegmentTree < int > segment_tree = {A, A.size(), 0};
segment_tree.make();
Sparse table
// Operacion asociativa IDEMPOTENTE
#define log2fl(x) (x ? 63 - __builtin_clzll(x) : -1)
templT struct SparseTable {
```

```
vector < T > & arr; int N;
    vector < vector < T >> st;
    // Modificar operacion
    T op (T a, T b) { return min(a,b); }
    void make () {
        st.resize(20, vector<T>(N));
        st[0] = arr; forn(w,19) forn(i,N - (1 << (w+1)) - 1)
            st[w+1][i] = op(st[w][i], st[w][i + (1 << w)]);
    }
    T query (int i, int j) {
        int w = log2fl(j - i + 1);
        return op(st[w][i], st[w][j - (1 << w) + 1]);
    }
};
// Usar asi:
vector < int > A = {...}:
SparseTable < int > sparse_table = {A, A.size()};
sparse_table.make();
    Grafos
Toposort de un DAG
```

DAG condensado

```
using AdjList = vector<vector<int>>;
vector<int> Toposort (AdjList& G) {
    int N = G.size();
   vector<int> indegree(N), res;
   forn(u, N) for (int v : G[u]) indegree[v]++;
   // Elegir crierio de priorizacion cambiando el orden en el que se

→ sacan

   // (por defecto el menor)
   using Bag = priority_queue<int, vector<int>, greater<int>>;
   Bag bag;
   forn(u, N) if(indegree[u] == 0) bag.push(u);
    while (bag.size()) {
       int u = bag.top();
       bag.pop();
       res.push_back(u);
       for (int v : G[u]) {
            indegree[v]--;
            if (indegree[v] == 0) bag.push(v);
       }
   }
   return res;
```

```
using AdjList = vector<vector<int>>;
AdjList DAGCondensado (AdjList& G) {
   int N = G.size():
   vector < bool > visitado(N);
   vector < int > orden;
   function < void(int) > get_orden = [&](int u) -> void {
      visitado[u] = true;
      for (int v : G[u]) if (!visitado[v]) get_orden(v);
      orden.pb(u);
   };
   forn(u, N) if (!visitado[u]) get_orden(u);
   reverse(all(orden));
   AdjList T(N);
   forn(u, N) for (int v : G[u]) T[v].pb(u);
   vector<int> comp, raiz(N), raices;
   function < void(int) > extraer_comp = [&](int u) -> void {
      visitado[u] = true;
      comp.pb(u);
      for (int v : T[u]) if (!visitado[v]) extraer_comp(v);
  };
   visitado.assign(N, false);
   for (int u : orden) if (!visitado[u]) {
      extraer_comp(u);
      int r = comp.front();
      for (int v : comp) raiz[v] = r;
      raices.pb(r);
      comp.clear();
   }
   int c = 0;
   map < int , int > coords;
   for (int r : raices) coords[r];
   for (auto& e : coords) e.snd = c++;
   AdjList SCC(raices.size());
   forn(u, N) for (int v : G[u]) {
      int ru = coords[raiz[u]], rv = coords[raiz[v]];
      if (ru != rv) SCC[ru].pb(rv);
   }
   return SCC;
Bipartite check
using AdjList = vector<vector<int>>;
```

```
bool EsBipartito (AdjList& G) {
    vector < int > color(G.size(), -1);
    color[0] = 0:
    queue < int > bag;
    for (bag.push(0); bag.size();) {
        int u = bag.front();
        bag.pop();
        for (int v : G[u]) {
            if (color[u] == color[v]) return false;
            if (color[v] == -1) {
                color[v] = 1 - color[u];
                bag.push(v);
            }
        }
    }
    return true;
Encontrar puentes y articulaciones
using AdjList = vector<vector<int>>;
using Edge = pair<int, int>;
pair < vector < Edge > , vector < int >> GetPuentesArticulaciones (AdjList& G)
   int N = G.size(), time = 0;
   vector < bool > visitado(N);
   vector <int > tin(N, -1), tlow(N, -1), articulaciones;
   vector < Edge > puentes;
   function < void(int, int) > dfs = [&](int u, int p) -> void {
      visitado[u] = true;
      tin[u] = tlow[u] = time++;
      int hijos = 0;
      for (int v : G[u]) {
         if (v == p) continue;
         if (visitado[v]) tlow[u] = min(tlow[u], tin[v]);
         else {
            dfs(v, u);
            hijos++;
            tlow[u] = min(tlow[u], tlow[v]);
            if (tlow[v] > tin[u]) puentes.pb({u,v});
            if (tlow[v] >= tin[u] && p != -1) articulaciones.pb(u);
         }
      }
      if (p == -1 && hijos > 1) articulaciones.pb(u);
   };
   forn(r, N) if (!visitado[r]) dfs(r, -1);
   return mp(puentes, articulaciones);
```

### Matemática

### 5.1. Aritmética

```
Techo de la división
        #define ceildiv(a,b) ((a + b - 1) / b)
Piso de la raiz cuadrada
using 11 = long long;
ll isqrt (ll x) {
    11 s = 0;
    for (11 k = 1 \ll 30; k; k \gg 1)
        if ((s+k) * (s+k) <= x) s += k;
    return s;
}
Piso del log2
        #define log2fl(x) (x ? 63 - _builtin_clzll(x) : -1)
Aritmética en Zp
using ll = long long;
const 11 mod = 1e9 + 7;
11 resta_mod (11 a, 11 b) { return (a - b + mod) % mod; }
ll pow_mod (ll x, ll n) {
    11 \text{ res} = 0;
    while (n) {
        if (n % 2) res = res * x % mod;
        n /= 2;
        x = x * x \% mod;
    } return res;
}
```

11 div\_mod (11 a, 11 b) { return a \* pow\_mod(b, mod - 2) % mod; }

### Teoria de numeros 5.2.

### Criba

```
struct Criba {
   bool c[1000001]; vector < int > p;
    Criba () {
        p.reserve(1<<16);
```

```
for (int j = 2; i*j \le 1000000; j++) c[i*j] = 1;
        }
    bool isprime (int x) {
        for (int i = 0, d = p[i]; d*d \le x; d = p[++i])
            if (!(x % d)) return false;
        return x \ge 2;
};
Phollards Rho
using 11 = long long;
11 gcd(ll a, ll b){return a?gcd(b %a, a):b;}
ll mulmod (ll a, ll b, ll c) { //returns (a*b)%c, and minimize

    overfloor

        11 x = 0, y = a\%c;
        while (b > 0) {
                if (b \% 2 == 1) x = (x+y) \% c;
                y = (y*2) \% c;
                b /= 2;
        return x % c;
}
ll expmod (ll b, ll e, ll m){\frac{1}{0}} (\log b)
        if(!e) return 1;
        ll q = expmod(b, e/2, m); q = mulmod(q, q, m);
        return e %2? mulmod(b,q,m) : q;
}
bool es_primo_prob (ll n, int a)
        if (n == a) return true;
        11 s = 0, d = n-1;
        while (d \% 2 == 0) s++, d/=2;
        11 x = expmod(a,d,n);
        if ((x == 1) || (x+1 == n)) return true;
        forn (i, s-1){
                x = mulmod(x, x, n);
                if (x == 1) return false;
                if (x+1 == n) return true;
        return false;
```

for (int i = 2; i <= 1000000; i++) if (!c[i]) {

```
bool rabin (ll n){ //devuelve true si n es primo
                       return false;
        if (n == 1)
        const int ar[] = \{2,3,5,7,11,13,17,19,23\};
        forn (j,9)
                if (!es_primo_prob(n,ar[j]))
                        return false;
        return true;
}
ll rho(ll n){
    if( (n & 1) == 0 ) return 2;
    11 x = 2 , y = 2 , d = 1;
    11 c = rand() % n + 1;
    while( d == 1 ){
        x = (mulmod(x, x, n) + c) %n;
        y = (mulmod(y, y, n) + c) %n;
        y = (mulmod(y, y, n) + c)%n;
        if(x - y >= 0) d = gcd(x - y, n);
        else d = gcd(y - x, n);
    return d==n? rho(n):d;
}
map<ll, ll> prim;
void factRho (ll n){ //O (lg n)^3. un solo numero
        if (n == 1) return;
        if (rabin(n)){
                prim[n]++;
                return;
        11 factor = rho(n):
        factRho(factor);
        factRho(n/factor);
}
```

### 5.3. Geometria

### Template geometria

```
Sca operator * (Vec a, Vec b) { return a.x * b.x + a.y * b.y; }
Sca operator ^ (Vec a, Vec b) { return a.x * b.y + a.y * b.x; }
bool operator < (Vec a, Vec b) { return (a.x != b.x) ? (a.x < b.x) :
   \hookrightarrow (a.v < b.v): }
ostream& operator << (ostream &o, Vec& p) { auto x = mp(p.x, p.y);
   → return o << x; }</pre>
Sca norma2 (Vec p) { return p.x * p.x + p.y * p.y; }
```

### Estructuras locas

### 6.1. Disjoint set union

```
struct DSU {
    vector < int > p, w; int nc;
    DSU (int n) {
        nc = n, p.resize(n), w.resize(n);
        forn(i,n) p[i] = i, w[i] = 1;
    int get (int x) { return p[x] == x ? x : p[x] = get(p[x]); }
    void join (int x, int y) {
        x = get(x), y = get(y);
        if (x == y) return;
        if (w[x] > w[y]) swap(x,y);
        p[x] = y, w[y] += w[x];
    bool existe_camino (int x, int y) { return get(x) == get(y); }
};
6.2. Binary trie
```

```
struct BinaryTrieVertex { vector<int> next = {-1, -1}; };
using BinaryTrie = vector < BinaryTrieVertex >;
void binary_trie_add (BinaryTrie& trie, int x) {
    int v = 0;
    for (int i = 31; i >= 0; i--) {
        bool b = (x & (1 << i)) > 0;
        if (trie[v].next[b] == -1) {
            trie[v].next[b] = trie.size();
            trie.emplace_back();
        }
        v = trie[v].next[b];
    }
}
int binary_trie_max_xor (BinaryTrie& trie, int x) {
    int v = 0, res = 0;
```

```
for (int i = 31; i >= 0; i--) {
         bool b = (x & (1 << i)) > 0;
         if (trie[v].next[!b] != -1) {
             v = trie[v].next[!b];
             if (!b) res |= (1 << i);</pre>
         }
         else {
             v = trie[v].next[ b];
             if ( b) res |= (1 << i);</pre>
    } return res;
}
// Inicializar asi:
BinaryTrie trie(1);
```

## Sin categorizar

Búsqueda binaria sobre un predicado

```
using ll = long long;
// Si existe, el primer i donde pred(i) == true
// Si es todo false, devuelve d
11 bsearch (11 i, 11 j, bool (*pred)(11), 11 d) {
    while (!(i + 1 == j)) {
        ll m = i + ((j - i) >> 1);
        pred(m) ? j = m : i = m;
    if (pred(i)) return i;
    if (pred(j)) return j;
    return d;
}
Enumerar subconjuntos de un conjuto con bitmask
```

```
// Imprimir representaciones en binario de todos los numeros "[0,
   \hookrightarrow .... 2^N-1]"
forn(mask, (1 << N)) {
    forn(i, N) cout << "01"[(mask & (1 << i)) > 0] << "\0\n"[i == N]
}
// Iterar por los bits de cada subconjunto
forn(mask, (1 << N)) {
    forn(i, N) {
        bool on = (mask & (1 << i)) > 0;
        if (on) { ... }
        else { ... }
}
```

### Hashing Rabin Karp

```
using ll = long long;
const ll primo = 27, MAX_PRIME_POW = 1e6;
11 prime_pow[MAX_PRIME_POW];
void get_prime_pow () {
    prime_pow[0] = 1;
    forn(i, MAX_PRIME_POW) prime_pow[i+1] = prime_pow[i] * primo %
}
vector<ll> get_rolling_hash (string& s) {
    vector<ll> rh(s.size() + 1);
    rh[0] = 0;
    // Djo: es 'A' o 'a' ???
    forn(i, s.size()) rh[i+1] = (rh[i] * primo % mod + s[i] - 'A') %
       \hookrightarrow mod;
    return rh;
ll hash_range_query (vector<ll>& rh, int i, int j) {
    return (rh[j] - (rh[i] * prime_pow[j - i] % mod) + mod) % mod;
```

# . Brainstorming

- $\blacksquare$  Graficar como puntos/grafos
- Pensarlo al revez
- $\blacksquare$  ¿Que propiedades debe cumplir una solución?
- $\blacksquare$  Si existe una solución, ¿ existe otra más simple?
- ¿Hay elecciones independientes?
- $\bullet$  ¿El proceso es parecido a un algoritmo conocido?
- $\blacksquare$  Si se busca calcular f(x) para todo x, calcular cuánto contribuye x a f(y) para los otros y
- $\blacksquare$  Definiciones e identidades: ¿ que significa que un array sea palindromo? (ejemplo)