

M6

for any $z \in M$
the path
 $x \rightarrow z$ followed by
 $z \rightarrow y$

can be no shorter
than the shortest
path from x to y
Hence we require

$$(iv) \quad d(x, y) \leq d(x, z) + d(z, y)$$

This is called the triangle inequality.