Suppose we require that these 3 operations $^c, \cup, \cap$ always produce sets.

Then

$$A \cap A^c \equiv \{x \in U : x \in A \text{ and } x \notin A\}$$

must be a set in U!

It is called the empty set ϕ. The set with no elements.