Rudin calls its an r-neighborhood of x, or just a neighborhood.

Are there more general families of sets of points in a metric space (m, d) that could be used to determine convergence of sequences regardless of the particular seq or its limit?