

DB 11

Comparison Test

Then suppose $|a_n| \leq b_n$

$$\text{Let } S_n = \sum_{j=1}^n a_j, \quad T_n = \sum_{j=1}^n b_j$$

$$\text{and } \bar{S}_n = \sum_{j=1}^n |a_j|$$

Then

(i) If $\lim_{n \rightarrow \infty} T_n < \infty$ then

S_n and \bar{S}_n converge

(ii) If \bar{S}_n diverges

then T_n diverges

Def: When $\lim_{n \rightarrow \infty} \bar{S}_n < \infty$ $\sum_{j=1}^{\infty} a_j$ is said to converge absolutely