(Bolzano Weierstrass)

Corollary If $\{a_n\}$ is a bounded seq in R, it has a convergent subsequence.

(Even if $\{a_n\}$ is not bounded, it has a subseq converging in $R\infty$.)