FROM: Ecnation diferentialy - 12.12.2017 - way

Ecuatio afine de cordin superior

a1(), -1 an(), 5(): IcIR->1R

Jistimal comanic associat

$$\frac{dx_1}{dt} = x_2$$

$$\frac{dx_2}{dt} = x_3$$

$$\frac{dx_3}{dt} = x_3$$

$$\frac{dx_4}{dt} = x_3$$

$$\frac{dx_5}{dt} = x_5$$

dt = E ai(t) Traje, + b(t)

PROP (de echivalenta): 4(·) sol. a cc. (1) (3) \$(·) = (4(·), 6'(·), --, 6(n-1)(·)) sol-a cc. (2)

Th. (E. U. G.)

a.(·), -, a.m(·), b(·): Ic IR > IR Y def(1)

Affinei Y (to, (xo, xo', ..., xo'')) E I x IR ~ £! & (·): I -> IR sol. on 4(to) = xo, 4'(to) = 2xo'.

... y [m-1] (to) = xo''-1

... y [m-1] (to) = xo''-1

Sail-), -, an(-), bc.) = 16(-): I -> 1R; 4(-) sol. ec. (1)4

The (varietation tol.)

+ (Po(1) 4 + Po(1) & Sa1(), an(1) (6()) Sai(1) = Sai(1) = Sai(1) = Dan(1)

The (principled variation constantilor)

Tie [[. (-), ..., [n[.]) sistem fundamental de sal. pt. ec. limoria asacianta [n] = \(\sigma_i (t) \overline{\pi} (n-i) \)

At. 4(1) E Sai(1) (an(1), b(1) a) & C(-) = (circ.) primitiva a function

t + > (Fi(t) ... Fn(t) | b(t) | a. j. 4(t) | E(it) | fi(t) |

Fi(t) ... Fn(t) | b(t) | b(t) |

Dun: Th. (Immapial van, count. pt. ac. afine pe 12") apl. hai 12) + Prop. de echivalunta

Fig. (v) = (File) = 3 (File) = 3 (File) (C) SA(-) sist-fundamental de sal.

pt. & = A(t) x A(t) = comp (a1, ..., an) => X(t) = cal(F(t), ... \(\vec{V}_n(t))\) state matrice fundamentalà de sal. pt. dr = A(t) x Aplic Th (Pr. var. eaust. pt. ec. afine pe IRM) lui (z) (dx = A(t) x + b(t)] ((.) bal-ec. (e) @ f c(-) primitiva a lui t => x-1 (+) [(+) a- ?. F(t) = X(t) c(t) => Se retine daar egalitatea dintre prima comp. din stånga en prima comp. din drugta » 2. e. d Hagaritm x(m) = \(\sigma^2(\x) x(m-1) + P(\x) 1. Consideram ec. linioura asacinta x en = Z aj (+) x (n-j)

Determina (, (), ..., (n ()) sistem fundamental de sal. Obs: Daca aj (+) = aj e IR + j = Tim - s vezi Algoritm Some sol generalà x(t) = > c: q: (t) c: E/R, i= in 2. Variatia const. proprin-zisa m Consta lie sol de forma x(t)= \(\int \cit(t) \vec{v}_i(t) \) Rezolva sistemme algebric = cilt) \$ (t) = 0 = c: (t) vi(t) =0 Kromby ci(t) = - 1=1,4 € ci (t) 4: (t) =0 => Cilti ... la la = c: (t) [(m-1) (t) = 0 = () X () = ... Jana sol. generala

2

FROM: Integrale prime pt. c. diferentiale in R. f(.,.): 0 = 1R x 1R ~ -> 1R ~ dt = f(t,x) Def. a) F(-,-): Do CD-21R s.n. integrala prima pt. campul victorial flow f(.,-)

(our pt. cc. 4x ~ f(t,x)) daca & ye) salufie en graph b(.) eDo f ce IR a.j.

F(t, b(t)) = c b) F(·,·): D. c.D → IR s.n. integralà prima vectoriala pt. e.v. f(·,·) (sanpt. ec. da = f(t,x)) daca + 4(·) solutie en graph 4(·) a D. J C & € IR (a.i. F (f,4(f)) = C 4 Chol. M. F(:,:) = (F1(:), ..., Fc(:)) integr. prima associata & F; (ii) int. pr. V i=1,K Obsz: F(t, x) = c integrale prime triviale (Nemicitation integnalison prime)

Fr (;), -, Fr (;): Do -> 1R int. prime. H: 1R" -> 1R at. F(\(\xi\)):= H(\(\xi\)(\xi\))..., Fr (\(\xi\)) Ste integrala prima The (Critorial St. integrale prime) Fir f(.,): D=Dc[RxIR~-> IR cont. == L(t,x) Fix F(:): Do = Do CD -> IR dwaivabilà
Atunci F(:) este integralà prima @ 1, F(t, x) + 1, F(t, x) f(t, x) = 0 \ \tau(t, x) \end{alignment} $\frac{Q_{00}: f(\cdot,\cdot) = (f_{1}(\cdot,\cdot), f_{2}(\cdot,\cdot), \dots, f_{m}(\cdot,\cdot))}{\int_{t}^{\infty} \int_{t}^{\infty} \int_{t$ lun: , 3" Fic (to, xo) & loc) = 1, f(;) cont. => T. franc => 14(): Io & V(to) -> Rem D. F(t, 1(+1) + D2F(6,4(4)). t= to, xo= p(to): 1, F(to, xo) + 0 = (to, xo) f(to, xo) = 0 0.E. 1 = " fie p(-) bol. in graph p(-) c Do (=) 0, F(t, p(t) + Dz F(t, p(t)) f(t, p(t)) = 0 D. F(t, p(t)) + D2 F(t, y(t) y'(t) = 0 3 (F(t, 4(t))) = 0 >) fee 1R a. p. f(t, 4(t)) Zc Def: F((;)), Fz(:), ..., Fx(:): D=Do -> IR derivolite, integrale prime s. m. functionals independente daca (dfi (t,x)):=1, x = k(maxim) = n \ \((t,x) \in \)

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T2 (Outominaria de a ajutoral integrables prime):
Fie flii) D= SEIRXIR = DIR cont. dx = f(t,x)
Fie Fo(.,.), ..., Fu(.,.): Do=Do - 1 > 12 (integrale prime funct. independent)
[It ( 3ti (t,x)) is time of 0 + (t,x) elo]. At.
 6(.): I cles IR m, grouph 4(.)c Do vote sal. @ fci o 1R a.r. Fi(t, 4(t)) = ci, xi fin
Jam: "=>" Evident din def.
       (6" Fie 6(-): I -3 1Rm, graph 4(-)cbo, fci...
      1. Le mata p () este durivabila (in Th. de fanctii implicità)
      2. Anatom ca (1.) vontica ecuatria
                                                     C= ((1) -- (m)
      Fie F(-1) = (Filip), Felip), --, Fn(-1))
     => F(t, p(t)) = c | & t | bt | (+1) . 4 (+1) = c
      Firm, For funct. indep => let (3Fi) ij=1, m + 0 + (5,x) & lo=) l= F(6x)
inversability
      (1) = -() = F(t, ((+1)) 1 ) , F(t, ((+1)) = f(t, ((+1))) (1)
      Fili) int. prime in D. Filt, x) + D2 Filt, x) = 0 i=1, 4
                      (1, F(tx) b, f(t,x) + 0 = f(t,x) f(t,x) = 0
      => f(t,x) = - (Dz F(t,x)) - 1 DiF(t,x)
      x = 9(t) f(t, 9(t)) = - (Dz F(t, 9(t))) 1 D, F(t, 9(t)) (2)
      (1) & (2) => q.e.d.
  Obj: Fi(:,), --, Fn(:,) integrale prime funct. indep., Fi(t,x)=ci,
 Obs. (Algoritan) [Reducura ordinalui en ajutorul jutegraldor prime]
    11 to = f(t,x) f(:,:) = De 18x18 = > 18x, f(:,:) = (f(:,:),.... fu(:,r))
     Maxi i=1,m
  Filis), ..., Filis) cha D = Do > 12 m, kah integrale prime funct. indy.
   Pr. dut \left(\frac{3F_c}{0x_i}(f_ix)\right)i_{i,j} = I_{i,k} \neq 0 \quad \forall (f_ix) \in J_0
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Pasuls: Resolva sistemal algebraic in neconoscatele 81, ..., x wimator: FI (t. XII) XXXXXIII VM = C1 [FE(t, X1, X21 --- , Xx, Xx+1, --, xn) = CR Posulz: Integreora sistemal de ec. dex+1 = f(t, 4, (t, xk+1, ..., xn, C1, ..., Cx), ...) ..., 4 x (+1, × x , e, ; ... (), × x + 1 - 1 × m) den = talt, yalt, xxx1, -1 xm, C1, -Ck WK (CIXETA) - 1 XM) CTICK 1 XK+ (1 m) XM) This (Existentia integralder prime) Fie f(:): D= B'c 12 x12 = 2 (17) out c'(17) out = f(t,x) At. & (to, xo) &) I Fr (.,.), Fu(.,.) . Do & U (to, xo) > 12 mc l'integrale primo functional indep.

Mai mult, daca f(:,:): Do > 12 ste integrala prima at. J H(:): 12 m > 12 a.i.

F(t,x)= H(F,(t,x)),..., Fm(t,x))