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| MODULE <i>LIFO</i>   |   |
| EXTENDS <i>Naturals, Sequences</i>   |   |
| CONSTANT <i>Message, QueueSize</i>   |   |
| VARIABLES <i>in, out, lifoq</i>  |   |
| <i>LIFOInterface</i> $\triangleq$ INSTANCE <i>LIFO_Interface</i> WITH $q \leftarrow lifoq$   |   |
| <i>Init</i> $\triangleq \wedge LIFOInterface!Init$   |   |
| <i>TypeInvariant</i> $\triangleq LIFOInterface!TypeInvariant$  |   |
| Send uses the generalized send method  |   |
| <i>SSend</i> ( <i>msg</i> ) $\triangleq LIFOInterface!Send(msg)$   |   |
| Receive message from channel <i>in</i> . change the queue to contain a concatenation of the new value from the in channel and the original queue                                   |   |
| <i>BufRcv</i> $\triangleq \wedge LIFOInterface!InChan!Rcv$<br>$\wedge lifoq' = \langle in.val \rangle \circ lifoq$<br>$\wedge$ UNCHANGED <i>out</i>                                |   |
| <i>BufSend</i> $\triangleq \wedge lifoq \neq \langle \rangle$<br>$\wedge LIFOInterface!OutChan!Send(Head(lifoq))$<br>$\wedge lifoq' = Tail(lifoq)$<br>$\wedge$ UNCHANGED <i>in</i> | Enabled only if <i>q</i> is nonempty.<br>Send <i>Tail(q)</i> on channel <i>out</i><br>and remove it from <i>q</i> . |
| <i>RRcv</i> $\triangleq LIFOInterface!Rcv$   |   |
| <i>Next</i> $\triangleq \vee \exists msg \in Message : SSend(msg)$<br>$\vee BufRcv$<br>$\vee BufSend$<br>$\vee RRcv$   |   |
| <i>Spec</i> $\triangleq Init \wedge \square[Next]_{\langle in, out, lifoq \rangle}$  |   |
| THEOREM $Spec \Rightarrow \square TypeInvariant$   |   |