IDS 702: Module 5.4

MULTIPLE IMPUTATION IN R

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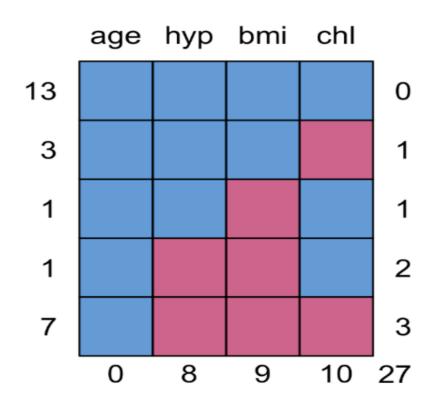


- Simple example using data that come with the MICE package in R.
- Dataset from NHANES includes 25 cases measured on 4 variables.
- Only 13 cases with complete data.
- We will use multiple imputation to make completed datasets and do analyses.
- The four variables are
 - 1. age (age group: 20-39, 40-59, 60+)
 - 2. bmi (body mass index, in kg/m^2)
 - 3. hyp (hypertension status: no, yes)
 - 4. chl (total cholesterol, in mg/dL)

```
library(mice)
data(nhanes2)
dim(nhanes2)
## [1] 25 4
summary(nhanes2)
                  bmi
                                           chl
##
                              hyp
      age
   20-39:12 Min. :20.40
                             no :13
                                      Min. :113.0
## 40-59: 7 1st Qu.:22.65 yes: 4
                                     1st Qu.:185.0
                            NA's: 8
## 60-99: 6 Median :26.75
                                     Median :187.0
             Mean :26.56
                                      Mean :191.4
##
             3rd Ou.:28.93
                                      3rd Qu.:212.0
##
             Max. :35.30
                                      Max. :284.0
##
             NA's :9
##
                                      NA's :10
str(nhanes2)
## 'data.frame': 25 obs. of 4 variables:
## $ age: Factor w/ 3 levels "20-39","40-59",..: 1 2 1 3 1 3 1 1 2 2 ...
## $ bmi: num NA 22.7 NA NA 20.4 NA 22.5 30.1 22 NA ...
## $ hyp: Factor w/ 2 levels "no", "yes": NA 1 1 NA 1 NA 1 1 NA ...
## $ chl: num NA 187 187 NA 113 184 118 187 238 NA ...
```

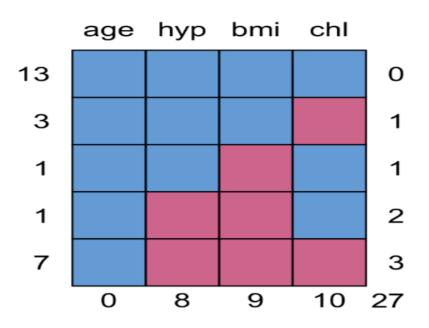
PATTERNS OF MISSING DATA

md.pattern(nhanes2)



5 patterns observed from $2^3=8$ possible patterns

PATTERNS OF MISSING DATA



- At the top: number of rows with each pattern, e.g., 3 cases where only cholesterol is missing.
- At the bottom: total number of missing values by variables.
- On the right: number of variables missing in each pattern.
- IDS 702

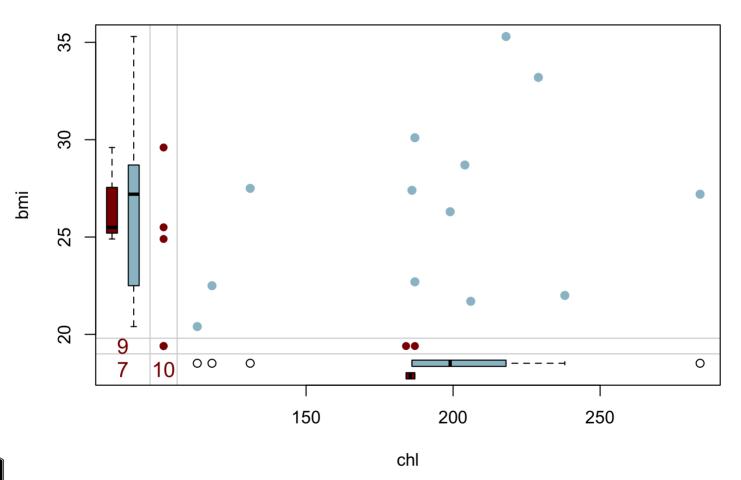
On the left: number of cases for each pattern.

The marginplot function can be used to understand how missingness affects the distribution of values on other variables.

- Blue box plots summarize the distribution of observed data given the other variable is observed.
- Red box plots summarize the distribution of observed data given the other variable is missing.
- If data are MCAR, you expect the boxplots to be the same (hard to evaluate in this small sample)

Let's look at the margin plot for the two continuous variables bmi and chl.

marginplot(nhanes2[,c("chl","bmi")],col=c("lightblue3","darkred"),cex.numbers=1.2,pch=19)



- Interpretation of the numbers in red.
 - 9 = number of observations with missingness in bmi
 - 10 = number of observations with missingness in chl
 - 7 = number of observations with missingness in both bmi and chl.
- The scatterplot of blue points display the relationship between bmi and chl when they are both observed (13 cases).
- The red points indicate the amount of data used to generate the red boxplots.

We will use the mice function to generate 10 imputed datasets. By default, mice uses

- pmm: Predictive mean matching for numeric data
- logreg: Logistic regression for factor data with 2 levels
- polyreg: Multinomial logistic regression for factor data with > 2 levels
- polr: Proportional odds model for factor data with > 2 ordered levels

Other commonly used methods are

- norm: Bayesian linear regression
- sample: Random sample from observed values
- cart: Classification and regression trees
- rf: Random forest

Personally, I prefer to use norm instead of pmm for imputing numeric/continuous variables.

For the illustration,

methods(mice)

```
## Warning in .S3methods(generic.function, class, envir): function 'mice' appears
## not to be S3 generic; found functions that look like S3 methods
   [1] mice.impute.2l.bin
                                 mice.impute.21.lmer
                                                          mice.impute.2l.norm
##
  [4] mice.impute.2l.pan
                                                          mice.impute.2lonly.norm
                                 mice.impute.2lonly.mean
  [7] mice.impute.2lonly.pmm
                                 mice.impute.cart
                                                          mice.impute.jomoImpute
## [10] mice.impute.lda
                                 mice.impute.logreg
                                                          mice.impute.logreg.boot
## [13] mice.impute.mean
                                 mice.impute.midastouch
                                                          mice.impute.mnar.logreg
## [16] mice.impute.mnar.norm
                                 mice.impute.norm
                                                          mice.impute.norm.boot
## [19] mice.impute.norm.nob
                                 mice.impute.norm.predict mice.impute.panImpute
## [22] mice.impute.passive
                                 mice.impute.pmm
                                                          mice.impute.polr
## [25] mice.impute.polyreg
                                 mice.impute.quadratic
                                                          mice.impute.rf
## [28] mice.impute.ri
                                 mice.impute.sample
                                                          mice.mids
## [31] mice.theme
## see '?methods' for accessing help and source code
```

PREDICTIVE MEAN MATCHING (PMM)

- lacktriangle Suppose y is subject to missing values while x is completely observed. The basic idea for pmm is:
 - Using complete cases, regress y on x, obtaining $\hat{\beta}=(\hat{\beta}_0,\hat{\beta}_1)$;
 - Draw a new β^* from the "posterior distribution" of $\hat{\beta}$ (e.g, multivariate normal);
 - Using β^* , generate predicted values of y for all cases;
 - For each case with a missing y, identify set of donors with no missing values, who have predicted y values close to that of the case with missing data;
 - From among these cases, randomly select one and assign its observed value of y as the imputed value;
 - Repeat for all observations and imputation data sets.
- Pmm matches the distribution of the original observed variable, as imputed values are taken from the real data.

Back to the nhanes2_imp object, first look at the original data

nhanes2

```
bmi
                  hyp chl
##
        age
## 1
     20-39
              NA <NA>
## 2
     40-59 22.7
                   no 187
## 3
     20-39
              NA
                   no 187
     60-99
## 4
              NA <NA>
                      NA
                   no 113
## 5
     20-39 20.4
## 6
     60-99
              NA <NA> 184
     20-39 22.5
                   no 118
## 8
     20-39 30.1
                   no 187
     40-59 22.0
## 9
                   no 238
## 10 40-59
             NA <NA>
                       NA
## 11 20-39
             NA <NA>
## 12 40-59
              NA <NA>
                       NA
## 13 60-99 21.7
                   no 206
## 14 40-59 28.7
                  ves 204
## 15 20-39 29.6
                   no
## 16 20-39
              NA <NA>
                       NA
## 17 60-99 27.2
                  yes 284
## 18 40-59 26.3
                  yes 199
## 19 20-39 35.3
                   no 218
## 20 60-99 25.5
                  yes
                      NA
## 21 20-39
              NA <NA>
                       NA
## 22 20-39 33.2
                   no 229
## 23 20-39 27.5
                   no 131
## 24 60-99 24.9
                   no NA
## 25 40-59 27.4
                   no 186
```

Look at the first imputed-dataset

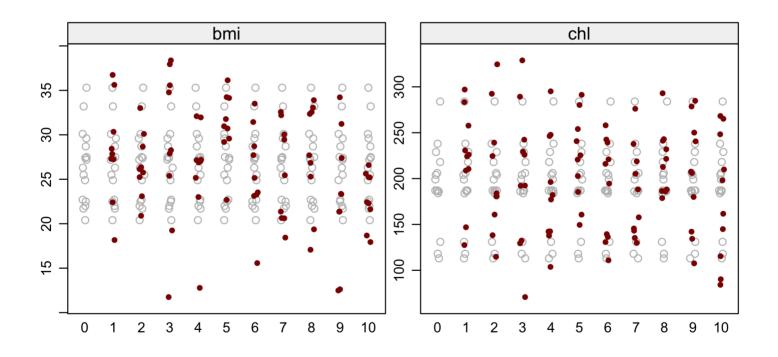
```
d1 <- complete(nhanes2_imp, 1); d1</pre>
                 bmi hyp
##
        age
                              chl
      20-39 30.34098
                      no 224,2285
## 1
     40-59 22.70000
                      no 187,0000
##
  2
##
  3
     20-39 27.29756
                     no 187.0000
## 4
     60-99 35.61975 yes 297.0469
## 5
     20-39 20.40000
                      no 113.0000
## 6
     60-99 18.16587 yes 184.0000
## 7
     20-39 22.50000
                      no 118.0000
## 8
     20-39 30.10000
                      no 187.0000
     40-59 22.00000
                      no 238.0000
## 10 40-59 27.84743
                      no 210.5014
## 11 20-39 27.24996
                      no 146.9218
## 12 40-59 28.43579
                      no 226.0825
## 13 60-99 21.70000
                      no 206.0000
## 14 40-59 28.70000 yes 204.0000
## 15 20-39 29.60000
                      no 208.7224
## 16 20-39 36.73795
                      no 230.7358
## 17 60-99 27.20000 yes 284.0000
## 18 40-59 26.30000 yes 199.0000
## 19 20-39 35.30000
                      no 218.0000
  20 60-99 25.50000 yes 257.7126
  21 20-39 22.42268
                      no 127.4948
## 22 20-39 33.20000
                      no 229.0000
                      no 131.0000
## 23 20-39 27.50000
## 24 60-99 24.90000
                      no 283.3828
## 25 40-59 27.40000
                      no 186.0000
```

Look at the last imputed-dataset

```
d10 <- complete(nhanes2_imp, 10); d10</pre>
                 bmi hyp
##
        age
                               chl
      20-39 26.59731
## 1
                      no 115.34762
     40-59 22,70000
                      no 187,00000
##
  2
     20-39 22.42548 no 187.00000
##
  3
     60-99 25.20745 ves 268.22285
## 4
## 5
     20-39 20.40000
                      no 113.00000
## 6
     60-99 22,29470
                      no 184,00000
     20-39 22.50000
                      no 118.00000
## 8
     20-39 30.10000
                      no 187.00000
     40-59 22.00000
                      no 238.00000
## 10 40-59 25.63055 yes 198.06595
## 11 20-39 17.93695
                         90.22238
                     no
## 12 40-59 21.62430 yes 209.92840
## 13 60-99 21.70000
                      no 206.00000
## 14 40-59 28.70000 yes 204.00000
## 15 20-39 29.60000
                      no 161.64022
## 16 20-39 18.67313
                      no 84,17346
## 17 60-99 27.20000 yes 284.00000
## 18 40-59 26.30000 yes 199.00000
## 19 20-39 35.30000
                      no 218.00000
  20 60-99 25.50000 yes 265.20195
## 21 20-39 25.22149
                      no 144.88429
## 22 20-39 33.20000
                      no 229.00000
## 23 20-39 27.50000
                      no 131.00000
## 24 60-99 24.90000
                      no 248.27329
## 25 40-59 27.40000
                      no 186.00000
```

Let's plot imputed and observed values for continuous variables.

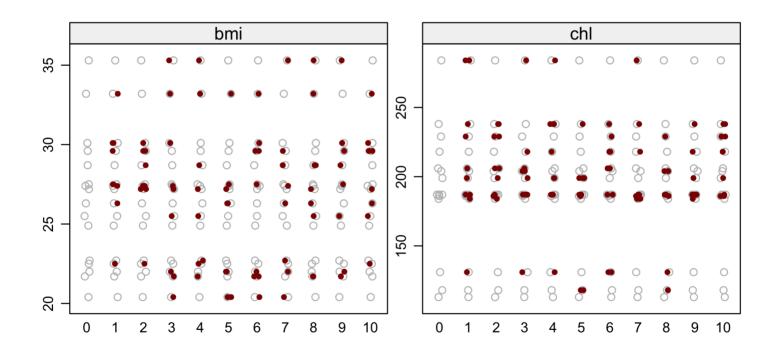
```
stripplot(nhanes2_imp, col=c("grey","darkred"),pch=c(1,20))
```



Grey dots are observed values and red dots are imputed values.

Let's see how this would change when we use pmm instead of norm.

```
nhanes2_imp2 <- mice(nhanes2,m=10,defaultMethod=c("pmm","logreg","polyreg","polr"),print=F
stripplot(nhanes2_imp2, col=c("grey","darkred"),pch=c(1,20))</pre>
```

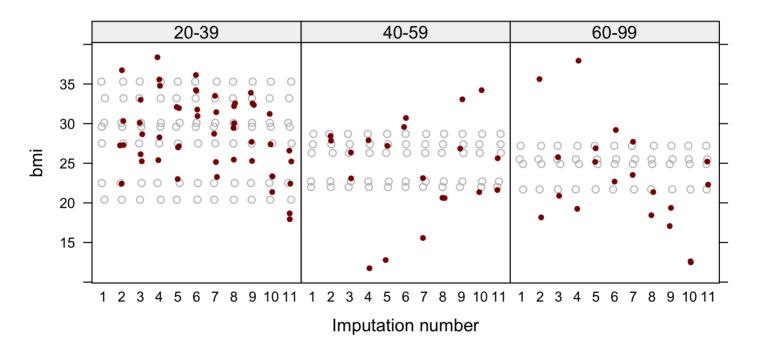




Easy to see that the distribution of the original observed data is preserved.

Also can do plots by values of categorical variable, say bmi by age. Let's look at the imputations using norm

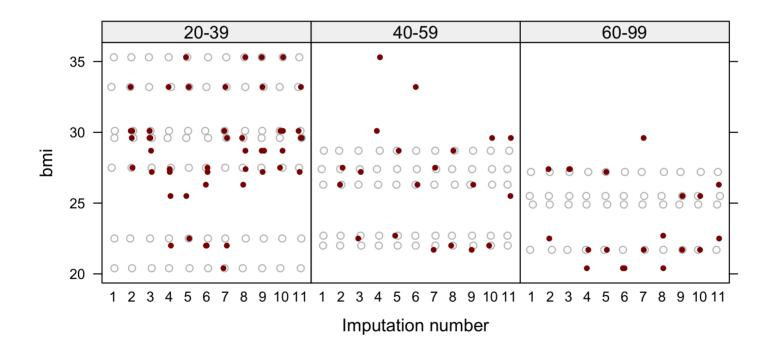
```
stripplot(nhanes2_imp, bmi~.imp|age, col=c("grey","darkred"),pch=c(1,20))
```





Using pmm instead of norm, we have:

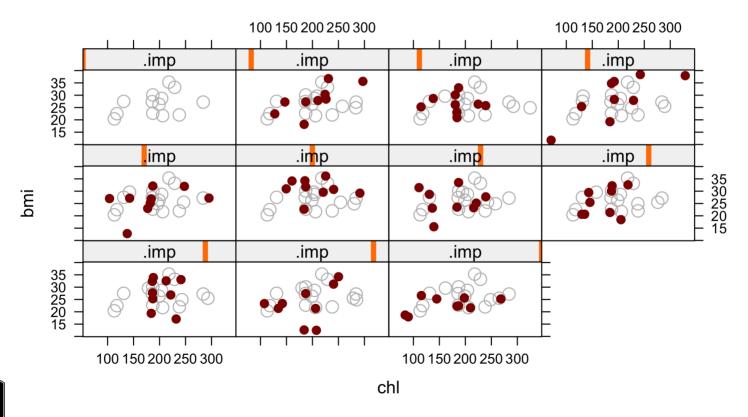
```
stripplot(nhanes2_imp2, bmi~.imp|age, col=c("grey","darkred"),pch=c(1,20))
```



Going forward, let's focus only on imputations using norm.

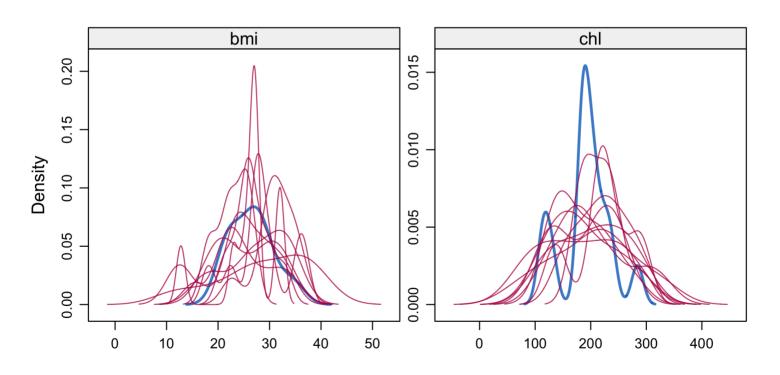
Scatterplot of chi and bmi for each imputed dataset. Here we can see why we should not use single imputations.

```
xyplot(nhanes2_imp, bmi ~ chl | .imp,pch=c(1,20),cex = 1.4,col=c("grey","darkred"))
```



To detect interesting differences in distribution between observed and imputed data, use the densityplot function.

densityplot(nhanes2_imp)



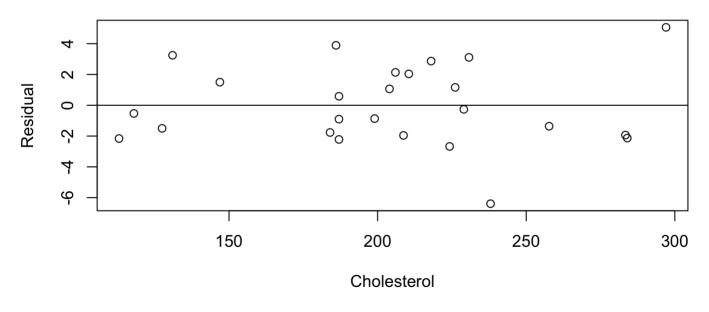


For model specification, i.e., transformations, either look at the complete cases or use one of the completed datasets. For example, to use the first dataset in a regression of bmi on age, hyp and chl, use

```
bmiregd1 <- lm(bmi~age+hyp+chl, data = d1)</pre>
summary(bmiregd1)
##
## Call:
## lm(formula = bmi ~ age + hyp + chl, data = d1)
##
## Residuals:
##
      Min
              10 Median
                             30
                                   Max
## -6.3936 -1.9368 -0.5314 2.0384 5.0614
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 11.94077
                         2.74697 4.347 0.000313 ***
## age40-59 -5.91646 1.50677 -3.927 0.000835 ***
## age60-99 -11.73873 2.13243 -5.505 2.18e-05 ***
            2.43724 1.71224 1.423 0.170027
## hypyes
## chl
               ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.845 on 20 degrees of freedom
## Multiple R-squared: 0.7062, Adjusted R-squared: 0.6474
## F-statistic: 12.02 on 4 and 20 DF, p-value: 3.866e-05
```

- To check residuals, you can examine the fit of the model in one or more completed datasets
- Any transformations will have to apply to all the datasets, so don't be too dataset-specific in your checks.

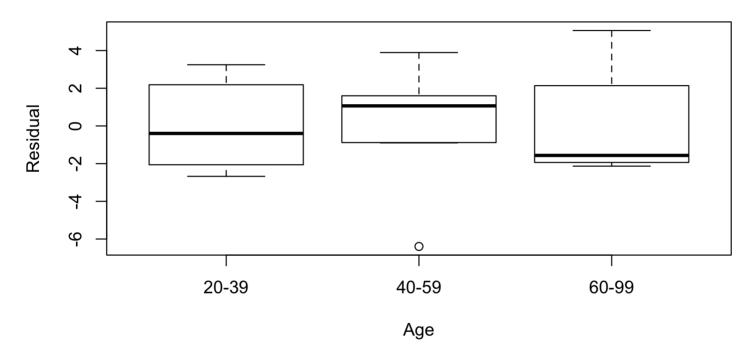
```
plot(bmiregd1$residual,x=d1$chl,xlab="Cholesterol",ylab="Residual"); abline(0,0)
```





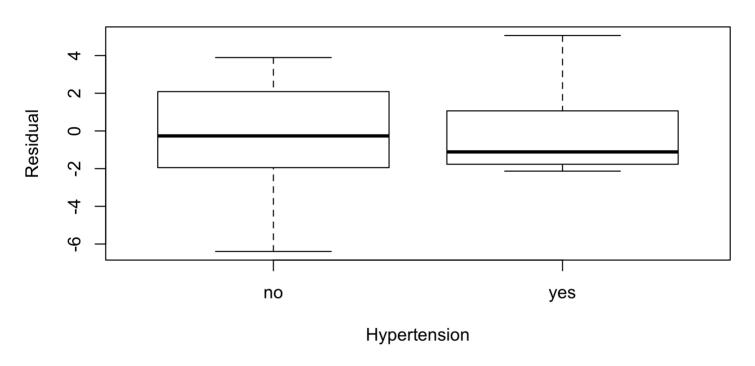
Looks good!

```
boxplot(bmiregd1$residual ~ d1$age, xlab = "Age", ylab = "Residual")
```



Pretty reasonable especially given the size of the dataset.

boxplot(bmiregd1\$residual ~ d1\$hyp, xlab = "Hypertension", ylab = "Residual")



- Good idea to repeat for more than one completed dataset.
- If you decide transformations are needed, you might reconsider the imputation models too and fit them with transformed values.

```
bmireg_imp <- with(data=nhanes2_imp, lm(bmi~age+hyp+chl))</pre>
#results for second dataset
bmireg_imp[[4]][[2]]
##
## Call:
## lm(formula = bmi ~ age + hvp + chl)
##
## Coefficients:
## (Intercept)
                  age40-59 age60-99
                                             hypyes
                                                             ch1
     18.44372 -6.53144
                             -10.51157
                                            1.41484
                                                         0.06152
##
#results for fifth dataset
bmireg_imp[[4]][[5]]
##
## Call:
## lm(formula = bmi ~ age + hyp + chl)
##
## Coefficients:
## (Intercept)
                  age40-59 age60-99
                                             hypyes
                                                            chl
     18.17017
                  -7.50997
                             -11.66474
                                            2.31496
                                                         0.07016
##
```



Now to get the multiple imputation inferences based on the Rubin (1987) combining rules

```
bmireg <- pool(bmireg_imp)</pre>
summary(bmireg)
##
                    estimate std.error statistic
                                                                 p.value
           term
## 1 (Intercept) 16.03269801 4.37392771 3.6655151 6.317986 0.009594146
## 2
       age40-59 -6.57207247 1.97111257 -3.3341944 11.653096 0.006179856
       age60-99 -10.83536538 2.90742365 -3.7267928 7.366405 0.006740526
## 3
                  2.04370148 2.35795119 0.8667276 8.976479 0.408661074
         hypyes
## 4
## 5
            chl
                  0.07394739 0.02428787 3.0446227 6.597552 0.020136806
```



- You can still do a nested F test (well, technically a test that is asymptotically equivalent to a nested F test) for the multiply-imputed dataset using the pool.compare function.
- For example, suppose we want to see if age is a useful predictor, then

```
bmireg_imp <- with(data=nhanes2_imp, lm(bmi~hyp+chl+age))</pre>
bmireg_impnoage <- with(data=nhanes2_imp, lm(bmi~hyp+chl))</pre>
#type "pool.compare(bmireg_imp, bmireg_impnoage)" to see full results
pool.compare(bmireg_imp, bmireg_impnoage)[c(9:12,18)]
## $qbar1
## (Intercept)
                    hypyes
                                            age40-59
                                                        age60-99
                                    chl
   16.03269801
                 ##
## $qbar0
## (Intercept)
                  hypyes
                                 chl
## 20.78380117 -0.88512898 0.03078513
##
## $ubar1
## [1] 8.4661183053 3.2824280668 0.0002711616 2.7734500763 4.2665578296
##
## $ubar0
## [1] 1.738379e+01 6.590985e+00 4.824345e-04
##
## $pvalue
               \lceil , 1 \rceil
##
## [1,] 1.654266e-05
```

You also can fit logistic regressions. For example to predict hypertension from all the other variables, do

```
hyplogreg_imp <- with(data=nhanes2_imp, glm(hyp~bmi+chl+age, family = binomial))</pre>
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

This turns out to be problematic here because we have some logistic regressions with perfect predictions.

```
hyplogreg <- pool(hyplogreg_imp)
summary(hyplogreg)</pre>
```

```
estimate
                       std.error
                                   statistic
                                                   p.value
##
         term
## 2
               90.415352 13854.295 6.526161e-03 18.25698 0.9948637
          bmi
## 3
         chl
              8.402631 1359.481 6.180766e-03 18.25763 0.9951355
## 4
      age40-59
              996.882034 169469.486 5.882369e-03 18.25787 0.9953704
      age60-99
              503.458547 8664479.986 5.810603e-05 18.25904 0.9999543
## 5
```

We do not have enough data to do a meaningful logistic regression here, unless we drop age as a predictor, but the command structure is fine!

MODIFYING PREDICTORS IN THE IMPUTATION MODELS

Going back to the imputed datasets, which variables does mice() use as predictors for imputation of each incomplete variable?

```
nhanes2_imp$predictorMatrix
```

```
## age bmi hyp chl
## age 0 1 1 1
## bmi 1 0 1 1
## hyp 1 1 0 1
## chl 1 1 0
```



MODIFYING PREDICTORS IN THE IMPUTATION MODELS

We can choose to exclude variables from any of the imputation models. For example, suppose we think that hyp should not predict bmi. Then,

```
pred <- nhanes2_imp$predictorMatrix
pred["bmi", "hyp"] <- 0
pred

## age bmi hyp chl
## age 0 1 1 1
## bmi 1 0 0 1
## hyp 1 1 0 1
## chl 1 1 1 0</pre>

mice(nhanes2, m=10, defaultMethod=c("norm", "logreg", "polyreg", "polr"), predictorMatrix=pred)
```



WHAT'S NEXT?

MOVE ON TO THE READINGS FOR THE NEXT MODULE!

