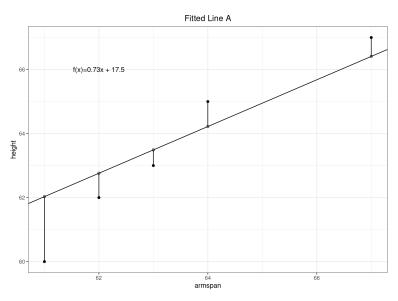
Name:	Date:

Which is the better fit?

Instructions:

A random sample of 5 observations was taken from the arm_span data. Calculate the Mean Squared Error (MSE) for each of the fitted lines by using the distances between the actual heights (the points) and their predicted heights (the points on the line). This will help you determine which of the linear models is the better fit.



Fitted Line A:

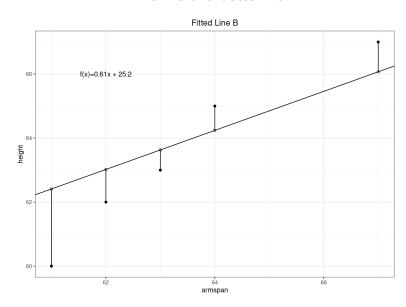
(armspan, height)	Actual height (observed)	Predicted height	Actual – Predicted	(Actual – Predicted) ²	MSE
(61, 60)	60	0.73(61) + 17.5 = 62.03	60 - 62.03 = -2.03	$(-2.03)^2 = 4.1209$	
(62, 62)	62				
(63, 63)	63				
(64, 65)	65				
(67, 67)	67				
				Sum =	÷ 5 =

Remember: We square our values when using MSE, which means that our units are now inches2, so you need to take the square root to get back to inches as the units.

$$\sqrt{MSE} = \sqrt{} =$$
_____ inches

Interpretation: When using arm span to predict height with Fitted Line A, our predictions will typically be off by inches.

Which is the better fit?



Fitted Line B:

(armspan, height)	Actual height (observed)	Predicted height	Actual – Predicted	(Actual – Predicted) ²	MSE
(61, 60)	60	0.61(61) + 25.2 = 62.41	60 - 62.41 = -2.41	$(-2.41)^2 = 5.8081$	
(62, 62)	62				
(63, 63)	63				
(64, 65)	65				
(67, 67)	67				
				Sum =	÷ 5 =

Remember: We square our values when using MSE, which means that our units are now inches², so you need to take the square root to get back to inches as the units.

$$\sqrt{MSE} = \sqrt{}$$
 = ____ inches

Interpretation: When using arm span to predict height with Fitted Line B, our predictions will typically be off by _____ inches.

Conclusion:

1. Which linear model is the better fit? How do you know?

Name: Date:	
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Which is the better fit?

ANSWER KEY

Fitted Line A:

(armspan, height)	Actual height (observed)	Predicted height	Actual – Predicted	(Actual – Predicted) ²	MSE
(61, 60)	60	0.73(61) + 17.5 = 62.03	60 - 62.03 = -2.03	$(-2.03)^2 = 4.1209$	
(62, 62)	62	0.73(62) + 17.5 = 62.76	60 - 62.76 = -2.76	$(-2.76)^2 = 7.6176$	
(63, 63)	63	0.73(63) + 17.5 = 63.49	60 - 63.49 = -3.49	$(-3.49)^2 = 12.1801$	
(64, 65)	65	0.73(65) + 17.5 = 64.95	60 - 64.95 = -4.95	$(-4.95)^2 = 24.5025$	
(67, 67)	67	0.73(67) + 17.5 = 66.41	60 - 66.41 = -6.41	$(-6.41)^2 = 41.0881$	
				Sum = 89.5092	÷ 5 = 17.90184

Remember: We square our values when using MSE, which means that our units are now inches², so you need to take the square root to get back to inches as the units.

$$\sqrt{MSE} = \sqrt{17.90184} = 4.231$$
 inches

Interpretation: When using arm span to predict height with Fitted Line A, our predictions will typically be off by <u>4.231</u> inches.

Fitted Line B:

(armspan, height)	Actual height (observed)	Predicted height	Actual – Predicted	(Actual – Predicted) ²	MSE
(61, 60)	60	0.61(61) + 25.2 = 62.41	60 - 62.41 = -2.41	$(-2.41)^2 = 5.8081$	
(62, 62)	62	0.61(61) + 25.2 = 63.02	60 - 63.02 = -3.02	$(-3.02)^2 = 9.1204$	
(63, 63)	63	0.61(61) + 25.2 = 63.63	60 - 63.63 = -3.63	$(-3.63)^2 = 13.1769$	
(64, 65)	65	0.61(61) + 25.2 = 64.85	60 - 64.85 = -4.85	$(-4.85)^2 = 23.5225$	
(67, 67)	67	0.61(61) + 25.2 = 66.07	60 - 66.07 = -6.07	$(-6.07)^2 = 36.8449$	
_				Sum = 88.4728	÷ 5 = 17.69456

Remember: We square our values when using MSE, which means that our units are now inches², so you need to take the square root to get back to inches as the units.

$$\sqrt{MSE} = \sqrt{17.69456} = 4.206$$
 inches

Interpretation: When using arm span to predict height with Fitted Line B, our predictions will typically be off by 4.206 inches.

Conclusion:

Which linear model is the better fit? How do you know? Fitted Line B is the better fit because our MSE value is 0.20728 lower, which means that the overall error is less than Fitted Line A's error.