

# CMPT 155: Computer Applications for Life Sciences

## Lecture 9: Regression

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# Presentation Outline

- 1 Administrative
- 2 Analyzing Trendlines
- 3 Prediction
- 4 Exercises
- 5 Further Reading

# Homework And Administrative

- Midterm 2 is on April 13<sup>th</sup>.
- You may bring a 1 page cheat sheet print or handwritten.
- Homework 5 is due ???

# Trendline (Regression Line)

- Data analysis is about revealing patterns and facts about data sets.
- Linear regression is a technique describes outputs  $y$  as linearly dependent on inputs  $x$ .

# Trendline Example

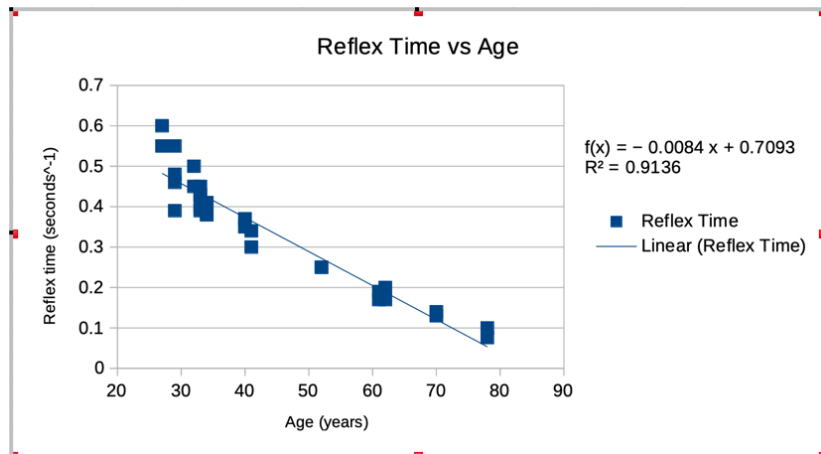


Figure: Example Linear Regression of Age against Reflex Time

# Adding a Trendline

A Trendline can be added to XY (Scatter) graphs.

Lets try plotting *CancerStudy.xlsx* and adding a Trendline:

- ➊ Download *CancerStudy.xlsx* from moodle.
- ➋ Select cells B2:C18
- ➌ Navigate to the XY Scatter Plot, and create scatter plot.
- ➍ be sure to include a chart title and axis titles.
- ➎ To add a trendline we can:
  - ▶ 'Chart Tools' → 'Add Chart Element' → 'Linear'.
  - ▶ Select the Datapoints → right(Ctrl)-click → 'Add Trendline'

# Types of Trendlines

Type	Excel Option	General Form
Linear	Linear	$y = mx + b$
Exponential	Exponential	$y = ae^{bx}$
Quadratic	Polynomial deg=2	$y = ax^2 + bx + c$
Cubic	Polynomial deg=3	$y = ax^3 + bx^2 + cx + d$

When computing predictions in excel, we can write trendline equations in the following fashion.

Type	Excel Form
Linear	$m * X + b$
Exponential	$(a)*EXP((b)*x)$
Quadratic	$(a)*(X^2) + (b)*X + c$
Cubic	$(a)*(X^3) + (b)*(X^2) + (c)*X + d$

Where  $X$  is a *cell reference* to an  $x$ -value in the dataset and  $a, b, c, d, m$  are real numbers that can be written as a decimal or in scientific notation  $1.234 * 10^{-4}$ , (i.e.,  $1.234 * (10^{-4})$ )

# Formatting Trendlines

Trendlines can be formatted through the 'Format Trendline' pane, which can be accessed by:

- 1 Selecting Data by left clicking a point on the XY scatter graph.
- 2 Right(Ctrl) clicking the points
- 3 Selecting the 'Format Trendline' menu option.

Trendlines modifications include:

- Equation and Displayed Statistics.
  - ▶ The equation of the trendline
  - ▶ whether to display the equation
  - ▶ whether to display correlation squared,  $R^2$ .
- Thickness and color
  - ▶ Thickness, color, effects, labelling
- Extrapolation
  - ▶ The range of the trendline is within the dataset by default
  - ▶ can be extrapolated by increasing the Forward/Backward periods option



# Analyzing Trendlines

After specifying a model we must be able to specify, analyze and measure models. Common functions for Analyzing a *linear* trendline include:

- slope using SLOPE()
- y- intercept using INTERCEPT()
- Correlation, R, using CORRELL()

Non Linear Trendlines can be analyzed using *Sum of Squared Residuals*, SSR.

# SLOPE()

SLOPE() - computes the slope of a linear regression line for a collection of  $x$  and  $y$  values.

- inputs
  - ▶ `known_ys` : selection  
array/selection of known  $y$  values
  - ▶ `known_xs` : selection  
array/selection of known  $x$  values
- outputs
  - ▶ computed slope : numeric  
estimated slope for a linear regression line for the given data.

# INTERCEPT()

Compute the  $y$  intercept of a linear regression line for a collection of  $x$  and  $y$  values.

- inputs
  - ▶ `known_ys` : selection array/selection of known  $y$  values
  - ▶ `known_xs` : selection array/selection of known  $x$  values
- outputs
  - ▶ computed intercept : numeric estimated **intercept** for a linear regression line for the given data.

# Correlation Coefficient (R)

Measures the correlations between  $x$ 's and  $y$ 's.

- inputs :
  - ▶ `known_x` : selection array/selection of known  $x$ 's.
  - ▶ `known_y` : selection array/selection of known  $y$ 's.
- outputs :
  - ▶ `correlation` : numeric correlation coefficient; between -1 and 1.

# Interpreting Correlation Coefficients

R value	Qualitative description
$-1 \leq R \leq -0.7$	<b>Very Strong</b> <i>Negative</i> Correlation
$-0.7 < R \leq -0.4$	<b>Strong</b> <i>Negative</i> Correlation
$-0.40 < R \leq -0.3$	<b>Moderate</b> <i>Negative</i> Correlation
$-0.30 < R \leq -0.2$	<b>Weak</b> <i>Negative</i> Correlation
$-0.2 < R < 0$	<b>No or Negligible</b> <i>Negative</i> Correlation
$R = 0$	<b>No Relationship, Uncorrelated</b>
$0 < R \leq 0.2$	<b>No or Negelible</b> <i>Positive</i> Correlation
$0.2 < R \leq 0.3$	<b>Weak</b> <i>Positive</i> Correlation
$0.3 < R \leq 0.4$	<b>Moderate</b> <i>Positive</i> Correlation
$0.4 < R \leq 0.7$	<b>Strong</b> <i>Positive</i> Correlation
$0.7 < R \leq 1$	<b>Very Strong</b> <i>Positive</i> Correlation.

Want to learn more for a correlation coefficients? Check out  
[CorrelationCoefficient - StatisticsHowTo](#)

# Which Trendline to choose?

## Things to Consider:

- What kind of relationship do you expect between your datapoints?
- What are the limitations of this dataset?
  - ▶ Do you expect to collect data outside this range?
  - ▶ Is this survey of physical data?
- How will this trendline be used in your later analysis?
- How do you measure best fit and trendline performance?

# Which Trendline to choose?

Common measures of trendline fit are

- Pearsons  $R^2$ .
  - ▶ is equal to squared correlation
  - ▶ can only be used with *Linear* regression lines
- Sum of Squared Residuals *SSR*.
  - ▶ Takes a sum of the *square* of the **residuals** (i.e., difference between the actual data and estimated function value).
  - ▶ the ***smaller the better the trendline fit.***

# Prediction

- Trendlines can be used to to predict values you don't have.
  - ▶ In Sample Prediction (interpolation) : Using the *trendline* to predict values that fall within the range of sample data that was used to create the trendline.
  - ▶ Out of Sample Prediction(extrapolation) : Using the *trendline* to predict values that fall out of the range of sample data that was used to create the trendline.
- for Extrapolation, you can visualize these predictions by adding *forward* and *backward* periods to the trendline in the *Format Trendline* panel.



# Prediction

- Lets try predicting the mortality in regions by:
  - ▶ Interpolation : average annual temperatures between 30 and 50 degrees, in 1 degree increments.
  - ▶ Extrapolating : average annual temperatures between 55 and 65 degrees, in 1 degree increments.
- Save the spreadsheet for future reference.
- Follow the same format when working through the homework.
- See '*CancerStudyStolution(Complete).xlsx*'

# Exercise 1: Lung Cancer Prevalance

- ➊ Download *Cigarettes.xlsx*
- ➋ Find
  - ▶  $m$  : the slope of the linear regression line
  - ▶  $b$  : the intercept of the linear regression line
  - ▶  $r$  : the correlation coefficient.
- ➌ Create a Scatter plot of the data and:
  - ▶ Add the linear regression line to the chart
  - ▶ Add exponential, quadratic, and cubic regression curves.
- ➍ In the excel document answer the following questions in a text box.
  - ▶ Which is the best model?
  - ▶ What is your prediction if a region's average number of cigarettes per person is 3500? How about 4000?

## Exercise : Solution

- ➊ Create a scatter plot of Cigarettes vs Lung Cancer deaths by:
  - ➊ selecting Cells A2:B16.
  - ➋ Going to “Insert” → “X Y (Scatter)”.
- ➋ Add a linear regression line by selecting the data, right-(Ctrl) clicking the data points and selecting “Add Trendline”
- ➌ In Cell B18 compute the slope of linear regression line, by writing:
  - ▶ `=SLOPE(B3:B16, A3:A16)`
- ➍ In Cell B19 compute the y-intercept of linear regression line, by writing:
  - ▶ `=INTERCEPT(B3:B16, A3:A16)`
- ➎ In Cell B20 compute the correlation between the x and y values by writing:
  - ▶ `=CORRELL(B3:B16, A3:A16)`

## Exercise : Solution (continued)

- ① Compute the linear estimates for all  $x$ 's using the  $m$  and  $b$  computed earlier.
  - ▶ In Cell D3 write: `=B$18*A3 + B$19`
  - ▶ Use autofill to apply the formula for all  $x$ 's.
- ② Find the equations for the non-linear regression curves by modifying the trendline:
  - ① Select the trendline and right-(Ctrl) click the trendline and click "Format Trendline"
  - ② In the "Format Trendline" menu check the box for "Display Equation on chart" and change the selection for trendline to be:
    - ★ Linear for Linear
    - ★ Exponential for Expon
    - ★ Polynomial with deg=2 for Quad
    - ★ Polynomial with deg=3 for Cubic

## Exercise : Solution (continued)

- 1 In cells E3, F3, and G3 compute the estimates given regression curve equations found previously. In cells:
  - ▶ E3 write:  $=9.1389*EXP(0.0003*A3)$
  - ▶ F3 write:  $=-3*(10\wedge-6)*(A3\wedge2) + 0.0205*A3 -14.218$
  - ▶ G3 write:  $=-3*(10\wedge-9)*(A3\wedge3) + 2*(10\wedge-5)*(A3\wedge2) -0.0507*A3 + 43.723$
- 2 Use autofill to fill in estimates for the three non-linear models.
- 3 Compute the residuals between the *estimates* and *observed* values by taking their difference. In cells:
  - ▶ I3 write :  $=B3-D3$
  - ▶ J3 write :  $=B3-E3$
  - ▶ K3 write :  $=B3-F3$
  - ▶ L3 write :  $=B3-G3$
- 4 Use autofill to compute residuals for all pairs of  $y$  observations and estimates for each model.

## Exercise : Solution (continued)

- ① Compute the Sum of Squared Residuals by using SUMSQ().
  - ▶ In Cell I17 write : =SUMSQ(I3:I16)
  - ▶ Autofill from I17 to L17.
- ② Compare the computed sum of squared residuals
  - ▶ The model with the best fit is the one with the *smallest* Sum of Squared Residuals
- ③ Compute out of sample Estimates using the cubic model by
  - ① writing down the x values, 3500, 4000 in cells A24, and A25 respectively.
  - ② Copy over the equation text from cell L3 and paste into Cell B24.
  - ③ Edit the equation in B24 such that it is passing in the x values from A24.
  - ④ Once you have an estimate in B24, use autofill to get the estimate in B25.

# Exercise : Solution (continued)

	A	B	C	D	E	F	G	H	I	J	K	L	M
1	Row data			Estimates					Residuals				
2	Cigarettes per person	Lung Cancer		Linear	Expon	Quad	Cubic		Linear	Expon	Quad	Cubic	
3	2860	22.07		21.08	21.55	19.87	23.65		-0.99	-0.52	-2.20	1.58	
4	2010	13.58		16.65	16.70	14.87	14.62		3.07	3.12	1.29	1.04	
5	2791	22.8		20.72	21.11	19.63	22.93		-2.08	-1.69	-3.17	0.13	
6	2618	20.3		19.82	20.04	18.89	21.03		-0.48	-0.26	-1.41	0.73	
7	2212	16.59		17.71	17.75	16.45	16.55		1.12	1.16	-0.14	-0.04	
8	2184	16.84		17.56	17.60	16.24	16.26		0.72	0.76	-0.60	-0.58	
9	2344	17.71		18.39	18.46	17.35	17.96		0.68	0.75	-0.36	0.25	
10	2692	22.04		20.20	20.49	19.23	21.85		-1.84	-1.55	-2.81	-0.19	
11	2206	14.2		17.67	17.71	16.41	16.49		3.47	3.51	2.21	2.29	
12	2914	25.02		21.36	21.91	20.04	24.19		-3.66	-3.11	-4.98	-0.83	
13	3034	25.88		21.98	22.71	20.36	25.31		-3.90	-3.17	-5.52	-0.57	
14	4240	23.03		28.26	32.61	18.77	23.04		5.23	9.58	-4.26	0.01	
15	1400	12.01		13.48	13.91	8.60	11.92		1.47	1.90	-3.41	-0.09	
16	2257	20.74		17.94	17.99	16.77	17.02		-2.80	-2.75	-3.97	-3.72	
17								SUMSQ	98.609	152.812	132.536	24.6352	
18													
19	m=	0.00520226											
20	b=	6.19762832										Cubic is the best model.	
21	r=	0.7758662	Strong Linear Relationship										
22													
23	Prediction (using the cubic model)												
24	3500	28.00											
25	4000	26.27											

# Further Reading

Computer Applications for Life Sciences Chapter 2, p. 15-20