$18.014~\mathrm{pset}~2$

10 Show that we have the following equations for any p, q

```
\begin{array}{l} h(0,p,q)=q+1 \\ h(1,p,q)=h(0,p,h(1,p,q-1))=h(1,p,q-1)+1=\ldots=h(1,p,0)+q=p+q \\ h(2,p,q)=h(1,p,h(2,p,q-1))=p+h(2,p,q-1)=\ldots=pq \\ h(3,p,q)=h(2,p,h(3,p,q-1))=p*h(3,p,q-1)=\ldots p^q \\ h(4,p,q)=h(3,p,h(4,p,q-1))=p^{h(4,p,q-1)}=p^{p^{p^{rrr}}} \end{array}
```

11 Define a function a(n) = h(n, n, n)