

## 1 Time evolution of wavefunction in box potential

- a)  $|\psi|^2 = C^2(2^2 + 3^2 + 1)\frac{a}{2} = 7a = 1, C = \frac{1}{\sqrt{7a}}$   
b)  $c_1 = 2C\sqrt{\frac{2}{a}\frac{a}{2}} = 2C\sqrt{\frac{a}{2}}, c_2 = 3C\sqrt{\frac{a}{2}}, c_3 = C\sqrt{\frac{a}{2}}$   
 $S = 14C^2a/2 = 14/7aa/2 = 1$   
c)  $\psi(t) = C(2\sin(kx)e^{-iE_2t/\hbar} + 3\sin(2kx)e^{-iE_2t/\hbar} + \sin(3kx)e^{-iE_3t/\hbar})$   
d) Yes  
e) 4:9:1 (/14)  
f) No  
g) Particle's energy not known prior to measurement.

## 2 Diabatic (sudden) expansion of infinite box

Griffiths

## 3 Hermitian operators

## 4 Square well centered at origin, parity

a)

$$\begin{aligned}f(x) &= Ae^{ikx} + Be^{-ikx} \\f(-a/2) &= Ae^{-ika/2} + Be^{ika/2} = 0 \\Ae^{-ika} + B &= 0\end{aligned}$$

substituting,

$$\begin{aligned}f(x) &= Ae^{ikx} - Ae^{-ika}e^{-ikx} \\&= Ae^{-ika/2}(e^{ikx}e^{ika/2} - e^{-ikx}e^{-ika/2}) \\&= C\sin k(x + a/2)\end{aligned}$$

Now the rest is the same,  $k = \frac{n\pi}{a}$  and  $C = \sqrt{\frac{2}{a}}$

b)

$$\begin{aligned}P\sin\frac{n\pi}{a}(x + a/2) &= \sin\frac{n\pi}{a}(-x + a/2) \\&= \sin\frac{n\pi}{a}(-x - a/2 + a) \\&= \sin\frac{n\pi}{a}(-x - a/2) + n\pi \\&= -\sin\frac{n\pi}{a}(x + a/2) - n\pi \\&= -\psi(x)(-1)^n\end{aligned}$$

c)

$$\begin{aligned}H\psi &= E\psi \\PH\psi &= EP\psi \\HP\psi &= EP\psi - [P, H]\psi\end{aligned}$$

so  $[P, H]\psi = \lambda P\psi$  but obviously  $[P, D] = 0$  so

$$\begin{aligned}[P, V]\psi &= \lambda P\psi \\PV\psi - VP\psi &= \lambda P\psi \\V(-x)\psi(-x) - V(x)\psi(-x) &= \lambda\psi(-x) \\V(-x) &= V(x) + \lambda \\&= V(-x) + 2\lambda \\\lambda &= 0\end{aligned}$$

$V$  must be an even function