

1 Time delay in photoelectric effect

$$P = I\pi r^2$$

$$\text{a) } t = E/P = \frac{E}{I\pi r^2}$$

$$\text{b) } t = \frac{2E}{3I\pi\lambda^2} \quad \text{c) } P = IA, t = (hc/\lambda)/P = \frac{hc}{\lambda IA}$$

2 Photons interacting with electrons

$$\text{a) } hc/\lambda - 1.6eV = hc/\lambda_{max}$$

$$\text{b) } \text{compton scattering}$$

3 Momentum shift and spatial wavefunction

$$\bar{\phi}(k) = \phi(k - k_0)$$

$$\bar{\psi}(x) = \frac{1}{\sqrt{2\pi}} \int \phi(k - k_0) e^{ikx} dk$$

$$= \frac{1}{\sqrt{2\pi}} \int \phi(k') e^{i(k' + k_0)x} dk'$$

$$= e^{ik_0x} \psi(x)$$

4 Double-slit interference of electrons

5 Hydrogen atom ground state as structure of minimum energy allowed by Heisenberg uncertainty

$$\text{a) } p^2/2m_e - k_e q^2/r$$

$$\text{b) }$$

$$k_e q^2/r^2 = p^2/m_e r$$

$$k_e q^2/r = p^2/m_e$$

$$E = -\frac{k_e q^2}{2m_e r}$$

$$\text{c) } \lambda = 2\pi r, p = hc/\lambda = hc/2\pi r, p^2 \quad \text{d) }$$

6 Rutherford scattering