

# WIRELESS COMMUNICATIONS SEMINAR 02

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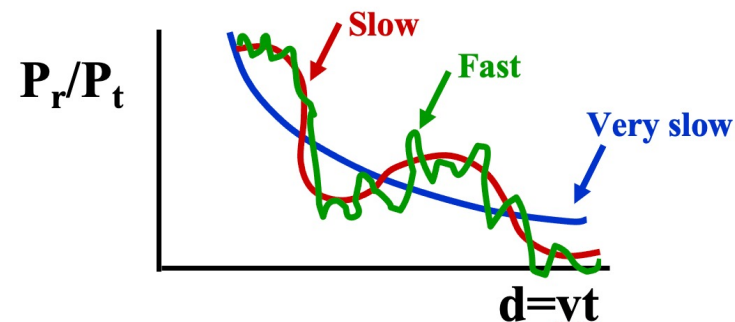
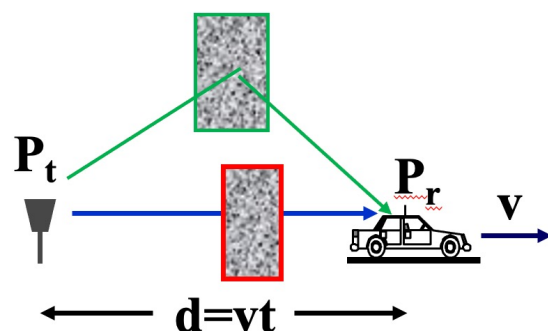
**DEPARTMENT OF ELECTRONIC ENGINEERING**

# CONTENTS

- Review of Large-scale fading
  - Pathloss
  - Shadowing
  - Cell Planning
- Small-scale fading (multi-path channel fading)
  - Time-varying impulse response
  - Coherence Bandwidth & Power Delay Profile
  - Coherence Time & Doppler spread spectrum

# REVIEW (LARGE-SCALE FADING)

- Path Loss
  - Signal power decrease by distance
- Shadowing
  - Attenuation by obstacles
- Multipath Fading
  - Reflection, diffraction, scattering



"Path loss" + "Shadowing" + "Multipath"

# REVIEW (LARGE-SCALE FADING)

- Pathloss + Shadowing
- Shadowing: Log-normal random variable

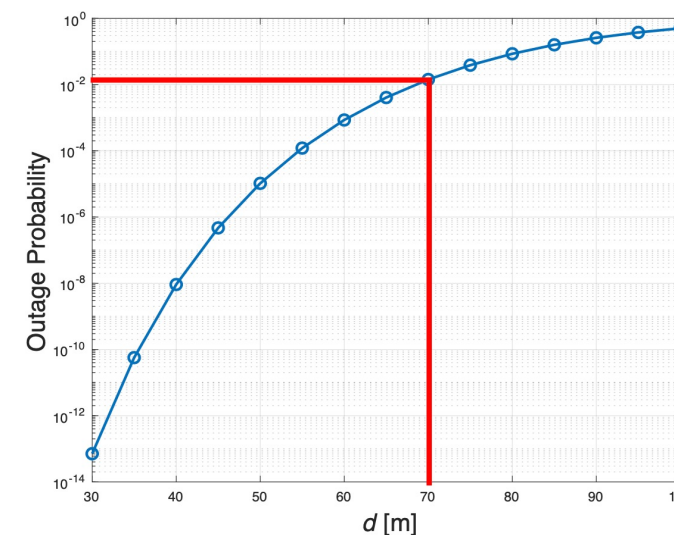
$$\frac{P_r}{P_t} dB = 10 \log_{10} K - 10\gamma \log_{10} \left( \frac{d}{d_0} \right) - \Psi_{dB}, \quad \Psi_{dB} \sim \mathcal{N}(\mu_\Psi, \sigma_\Psi^2)$$

- Outage probability:  $p_{out}(P_{min}, d) = p(P_r(d) < P_{min})$
- For Log-normal shadowing model:

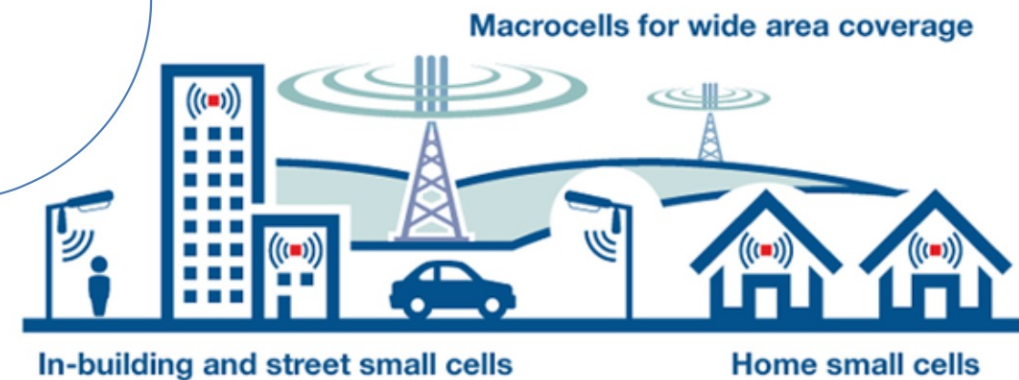
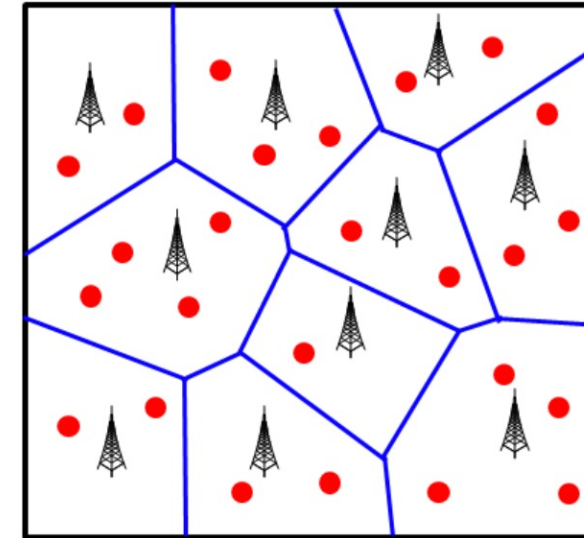
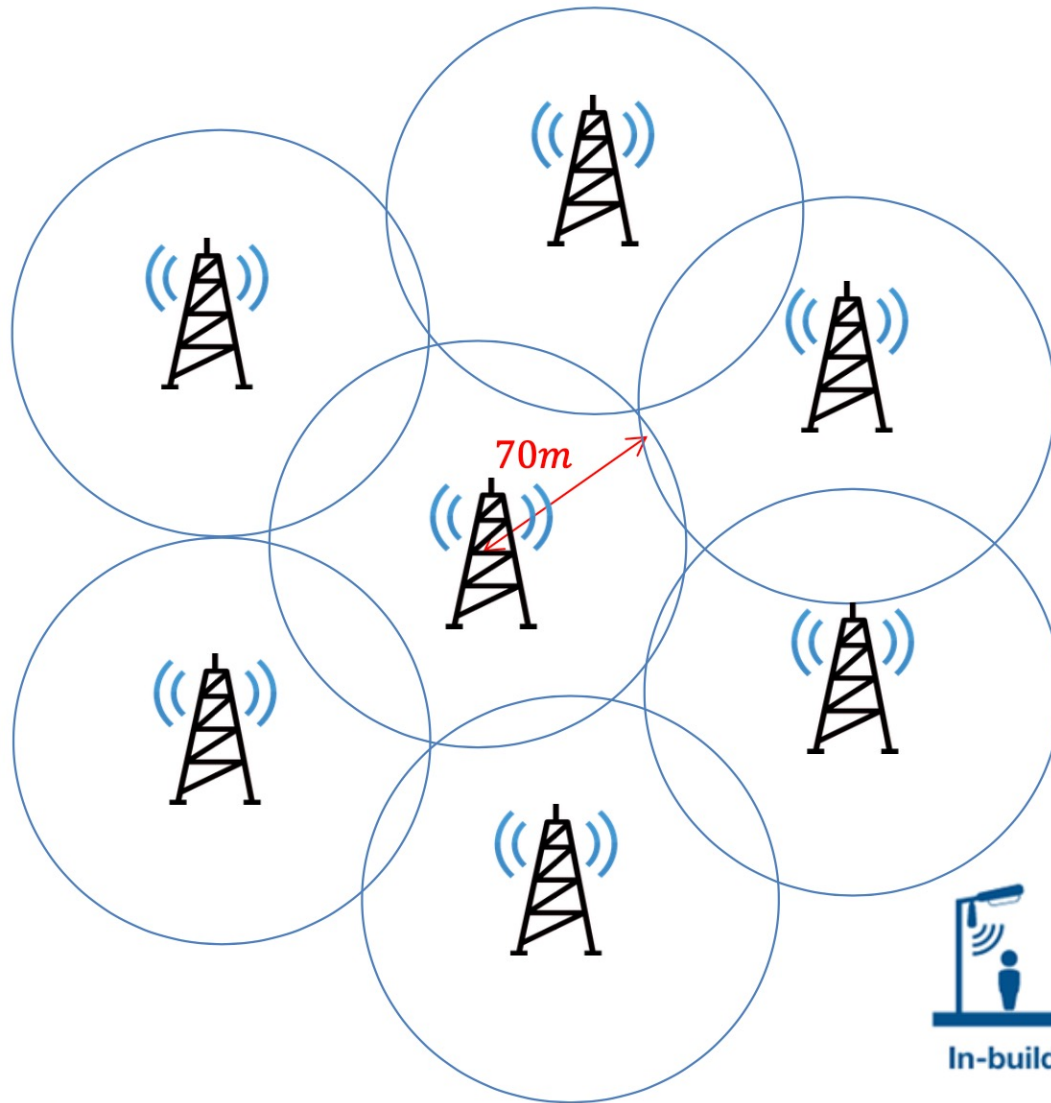
$$p(P_r(d) \leq P_{min}) = 1 - Q \left( \frac{P_{min} - (P_t + K_{dB} - 10\gamma \log_{10}(d/d_0))}{\sigma_{\Psi_{dB}}} \right)$$

# REVIEW (LARGE-SCALE FADING)

- Cell Planning : Choosing Cell Size
- Ex)
  - Consider wireless system
  - Transmit power at BS: **100dBm**
  - Path-loss model:  $P_r(d)\text{dBm} = P_t\text{dBm} - 40 \log_{10} d - \varphi_{dB}$ ,  $\varphi_{dB} \sim \mathcal{N}(0, 8^2)$
  - Required Received power: **20dBm**
  - Required Outage probability:  **$p_{out} < 0.01$**

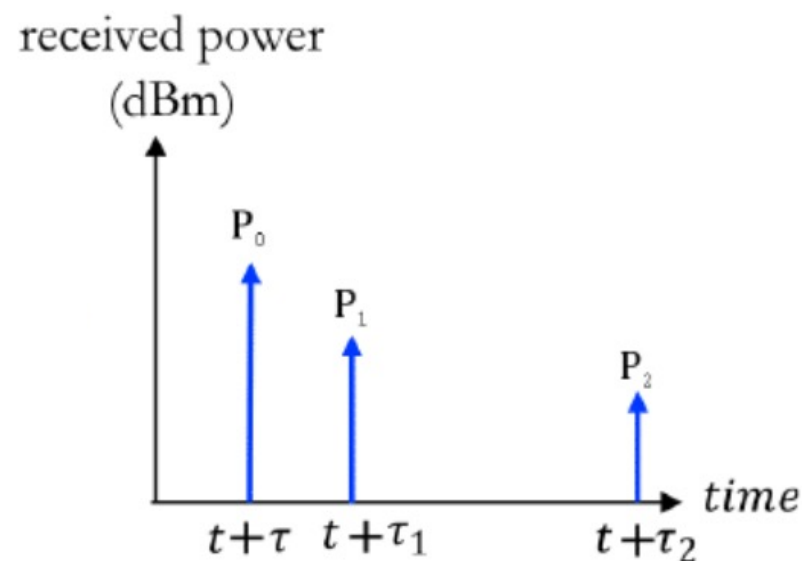
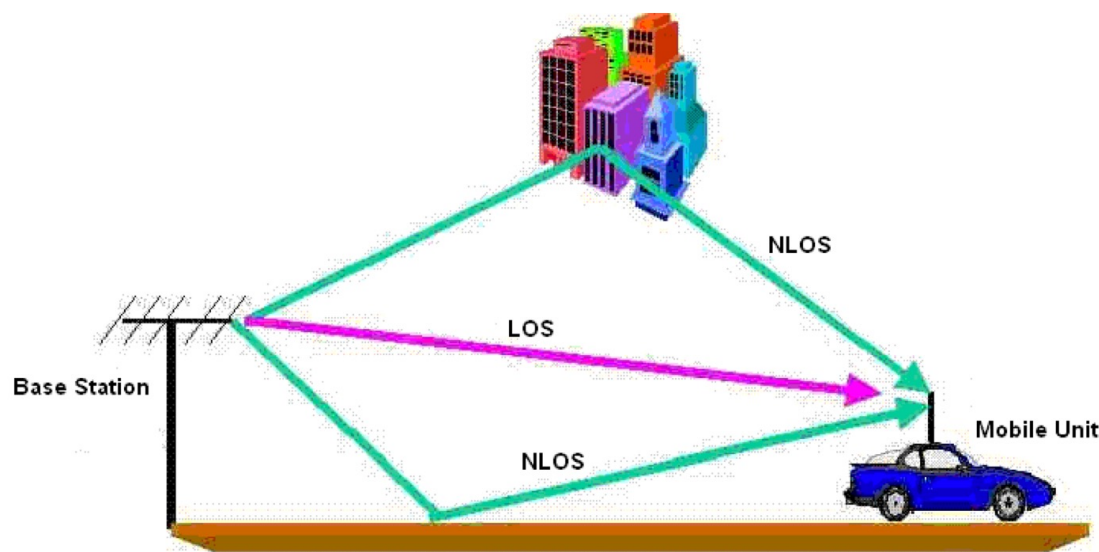


# REVIEW (LARGE-SCALE FADING)



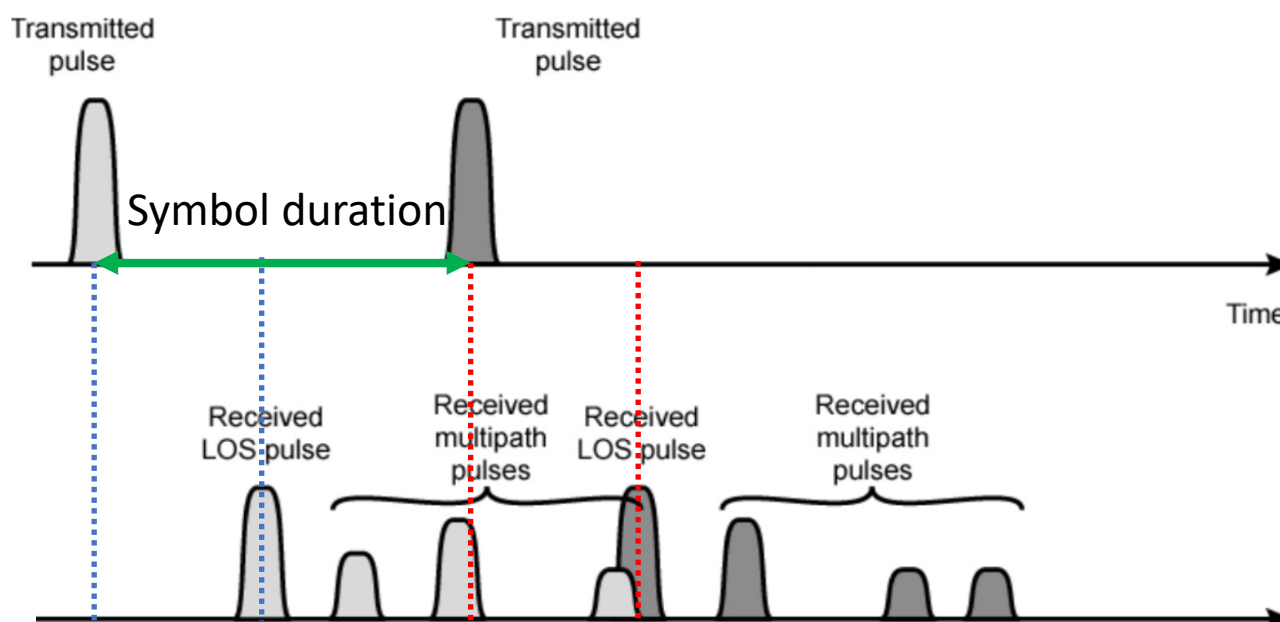
# MULTIPATH MODEL

- **Multipath Fading**
  - Constructive and destructive effects of different multipath components introduced by the channel
- Time-Varying Channel impulse response



# MULTIPATH MODEL

- **Multipath Fading**
  - Constructive and destructive effects of different multipath components introduced by the channel
- **Time-Varying Channel impulse response**
  - Impulse response → A Train of impulse responses





# STATISTICAL MULTIPATH MODEL

- Random number of multipath components
- Random Components change with time
  - The baseband signal :  $\tilde{s}(t)$
  - Amplitude :  $\alpha_i(t)$
  - Angle of arrival :  $\theta_i(t)$
  - Doppler shift :  $f_{D_i}(t) = \frac{v}{c} \cos \theta_i(t)$
  - Phase shift :  $\phi_{D_i}(t) = \int_t f_{D_i}(t) dt$
  - Path delay :  $\tau_i(t) = \frac{x_i(t)}{c}$ ,  $x_i(t)$ : path length
- The Received Signal

$$r(t) = \text{Re} \left\{ \sum_{i=0}^{N(t)-1} \alpha_i(t) \tilde{s}(t - \tau_i(t)) e^{j(2\pi f_c(t - \tau_i(t)) + \phi_{D_i}(t))} \right\}$$

Annotations in the equation:

- Pathloss, Shadowing** (yellow box) points to  $\alpha_i(t)$
- delay** (yellow box) points to  $\tau_i(t)$
- Doppler** (yellow box) points to  $\phi_{D_i}(t)$

# TIME-VARYING IMPULSE RESPONSE

- Received signal in multipath

$$\begin{aligned}
 r(t) &= \operatorname{Re} \left\{ \sum_{i=0}^{N(t)-1} \alpha_i(t) \tilde{s}(t - \tau_i(t)) e^{j(2\pi f_c(t - \tau_i(t)) + \phi_{Di}(t))} \right\} \\
 &= \operatorname{Re} \left\{ e^{j2\pi f_c t} \sum_{i=0}^{N(t)-1} \tilde{s}(t - \tau_i(t)) \alpha_i(t) e^{j\phi_i(t)} \right\}, \\
 &= \operatorname{Re} \left\{ e^{j2\pi f_c t} \sum_{i=0}^{N(t)-1} \int_{-\infty}^{\infty} \delta(\tau - \tau_i(t)) \tilde{s}(t - \tau) d\tau \alpha_i(t) e^{j\phi_i(t)} \right\} \\
 &= \operatorname{Re} \left\{ e^{j2\pi f_c t} \left( \int_{-\infty}^{\infty} c(\tau, t) \tilde{s}(t - \tau) d\tau \right) \right\}
 \end{aligned}$$

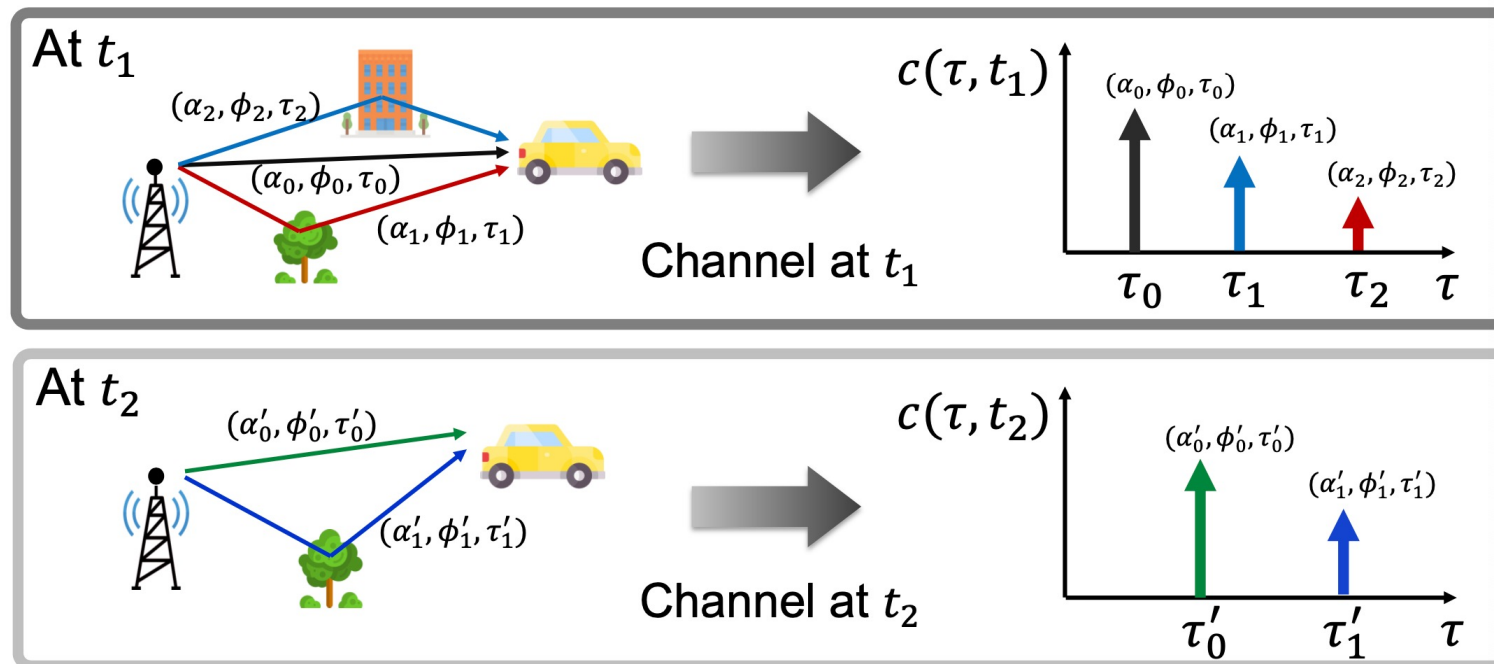
$\phi_i(t) = -2\pi f_c \tau_i(t) + \phi_{Di}(t)$

**Sifting property**

# TIME-VARYING IMPULSE RESPONSE

- Multipath is modeled by **time-varying channel impulse response**

$$c(\tau, t) = \sum_{i=0}^{N(t)-1} \delta(\tau - \tau_i(t)) \alpha_i(t) e^{j\phi_i(t)}$$



# WIDEBAND MODEL

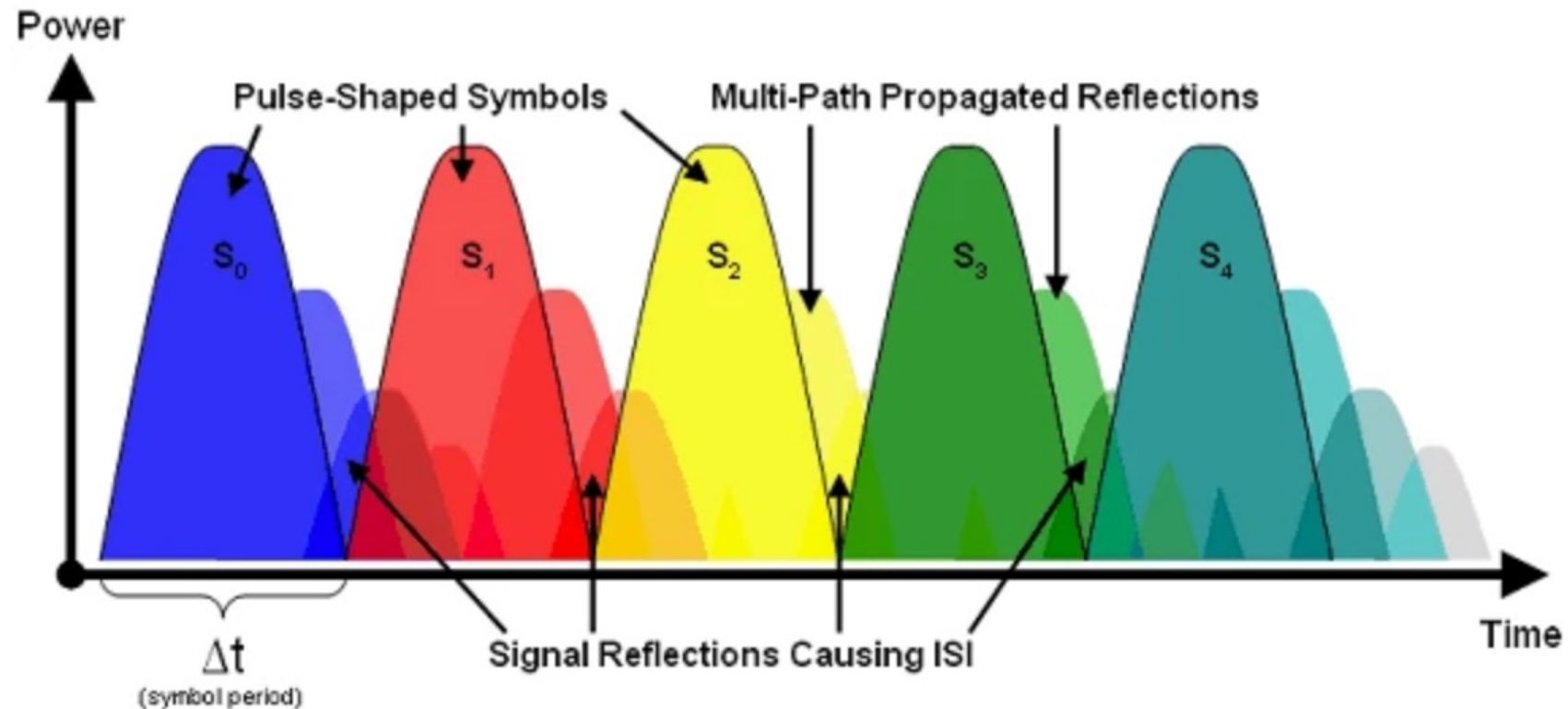
- Assume that the delay spread is significantly larger than the signal bandwidth (i.e.,  $T_D = \max_i |\tau_i - \tau_0| \gg B_s^{-1}$ )
  - Each of the multipath can be resolved
  - Multipath delay spread should be considered
- Use  $c(\tau, t)$  for characterizing channel

$$c(\tau, t) = \sum_{i=0}^{N(t)-1} \delta(\tau - \tau_i(t)) \alpha_i(t) e^{j\phi_i(t)}$$

- Since  $c(\tau, t)$  is random, we should characterize it statistically

# WIDEBAND MODEL

- An Intuition for ISI in wideband



# WIDEBAND MODEL

- Key Assumptions on  $c(\tau, t)$ 
  - Zero-mean complex Gaussian process
  - Phase of each multipath component is uniformly distributed
  - Wide Sense Stationary (WSS)
  - Uncorrelated scattering (US) : channel responses are uncorrelated between two different time delays
  
- Autocorrelation function ( $A_c(\tau, \Delta t)$ )
  - Characteristics of wideband channel are derived from the function
 
$$A_c(\tau_1, \tau_2; t, t + \Delta t) = \mathbb{E}[c^*(\tau_1, t)c(\tau_2, t + \Delta t)]$$

$$= A_c(\tau; \Delta t) \quad \because \text{Wide Sense Stationary}$$

# WIDEBAND MODEL

- Wideband Channel Characteristics

- Power delay profile
- Coherence bandwidth
- Doppler spread
- Coherence time

# COHERENCE BANDWIDTH

- Power delay profile

$$A_c(\tau) \triangleq A_c(\tau, 0) = \mathbb{E}[c^*(\tau_1, t)c(\tau_2, t)]$$

- Average power associated with a given multipath delay
- Delay spread
  - The delay associated with a given multipath component is weighted by its relative power
  - **Average** delay  $\mu_{T_D}$

$$\mu_{T_D} = \frac{\int_0^{\infty} \tau A_c(\tau) d\tau}{\int_0^{\infty} A_c(\tau) d\tau}$$

- **rms delay** spread  $\sigma_{T_D}$

$$\sigma_{T_D} = \sqrt{\frac{\int_0^{\infty} (\tau - \mu_{T_D})^2 A_c(\tau) d\tau}{\int_0^{(\infty)} A_c(\tau) d\tau}}$$



# COHERENCE BANDWIDTH

- Delay spread of the channel is roughly by the time delay  $T$  where  $A_c(\tau) \approx 0$  for  $\tau \geq T$
- $T_s \ll$  **rms** delay spread  $\sigma_{T_m}$   $\left(T_s < \frac{1}{10} \sigma_{T_m}\right)$

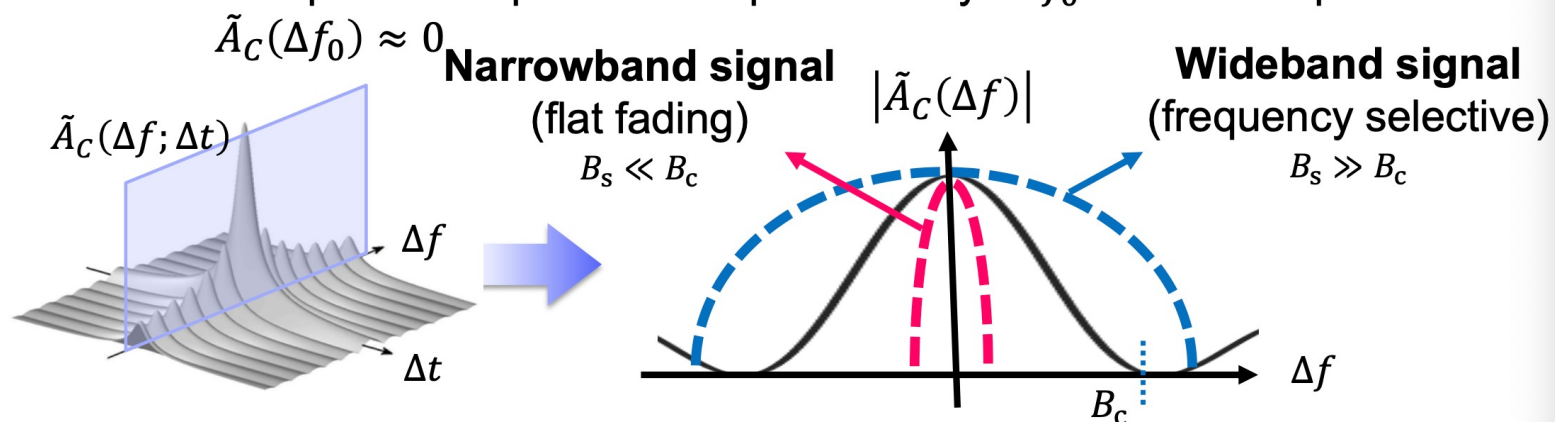
The system experiences **significant ISI**

- $T_s$  not small enough with respect to the **rms** delay spread  $\sigma_{T_m}$   $\left(T_s > \frac{1}{10} \sigma_{T_m}\right)$

The **ISI can be negligible**

# COHERENCE BANDWIDTH

- Define  $\tilde{A}(\Delta f; \Delta t) = \int_{-\infty}^{\infty} A_c(\tau; \Delta t) e^{-j2\pi\Delta f\tau} d\tau$
- $\tilde{A}(\Delta f) \triangleq \tilde{A}_c(\Delta f; 0)$ : The autocorrelation of time-varying multipath channel in frequency domain
- The Coherence Bandwidth  $B_c \approx \frac{1}{\sigma_{T_D}}$ 
  - Frequency  $B_c$  where  $\tilde{A}(\Delta f) \approx 0$  for all  $\Delta f > B_c$
  - Multipath components separated by  $\Delta f_0$  are independent if  $\tilde{A}_c(\Delta f_0) \approx 0$



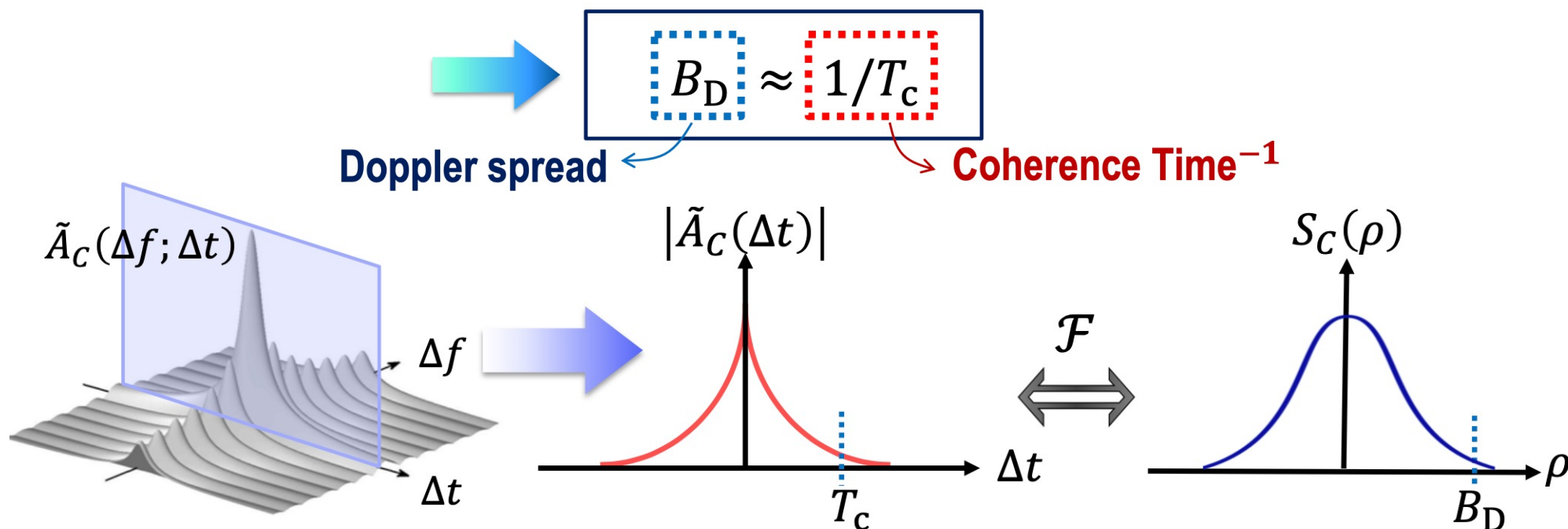
# COHERENCE TIME

- Define  $\tilde{A}_c(\Delta f; \Delta t) = \int_{-\infty}^{\infty} A_c(\tau; \Delta t) e^{-j2\pi\Delta f\tau} d\tau$
- Coherence time  $T_c$ 
  - Time variation of the channel (**by Doppler shift**)
  - $\tilde{A}_c(\Delta t) \triangleq \tilde{A}_c(\Delta f = 0; \Delta t)$
  - $\tilde{A}_c(\Delta t) = 0 \rightarrow$  uncorrelated and independent
  - $T_c$ : Range of  $\Delta t$  values over which  $\tilde{A}_c(\Delta t)$  is approximately nonzero
- Doppler spread  $B_D \approx \frac{1}{T_c}$ 
  - Doppler power spectrum:  $S_c(\rho) = \mathcal{F}_{\Delta t}[\tilde{A}_c(\Delta t)] = \int_{-\infty}^{\infty} A_c(\Delta t) e^{-j2\pi\rho\Delta t} d\Delta t$   
 $\rightarrow$  gives a Power Spectral Density of the received signal as a function of Doppler  $\rho$
  - $B_D$  : Maximum  $\rho$  value for which  $|S_c(\rho)|$  is greater than zero

# COHERENCE TIME

- Coherence time and Doppler Spread
  - By Fourier Transform

$$\tilde{A}_c(\Delta t) \xrightarrow{\text{Fourier Transform}} S_c(\rho)$$



# SUMMARY

- Coherence Bandwidth and Power delay profile

$$B_c \approx \frac{1}{\sigma_{T_D}}$$

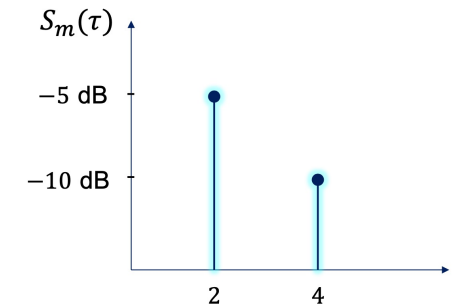
- Coherence Time and Doppler spread

$$T_c \approx \frac{1}{B_D}$$

- And they all come from  $c(\tau, t)$  : the time-varying channel impulse response

# SUMMARY

## • The Relationships of the Characteristics

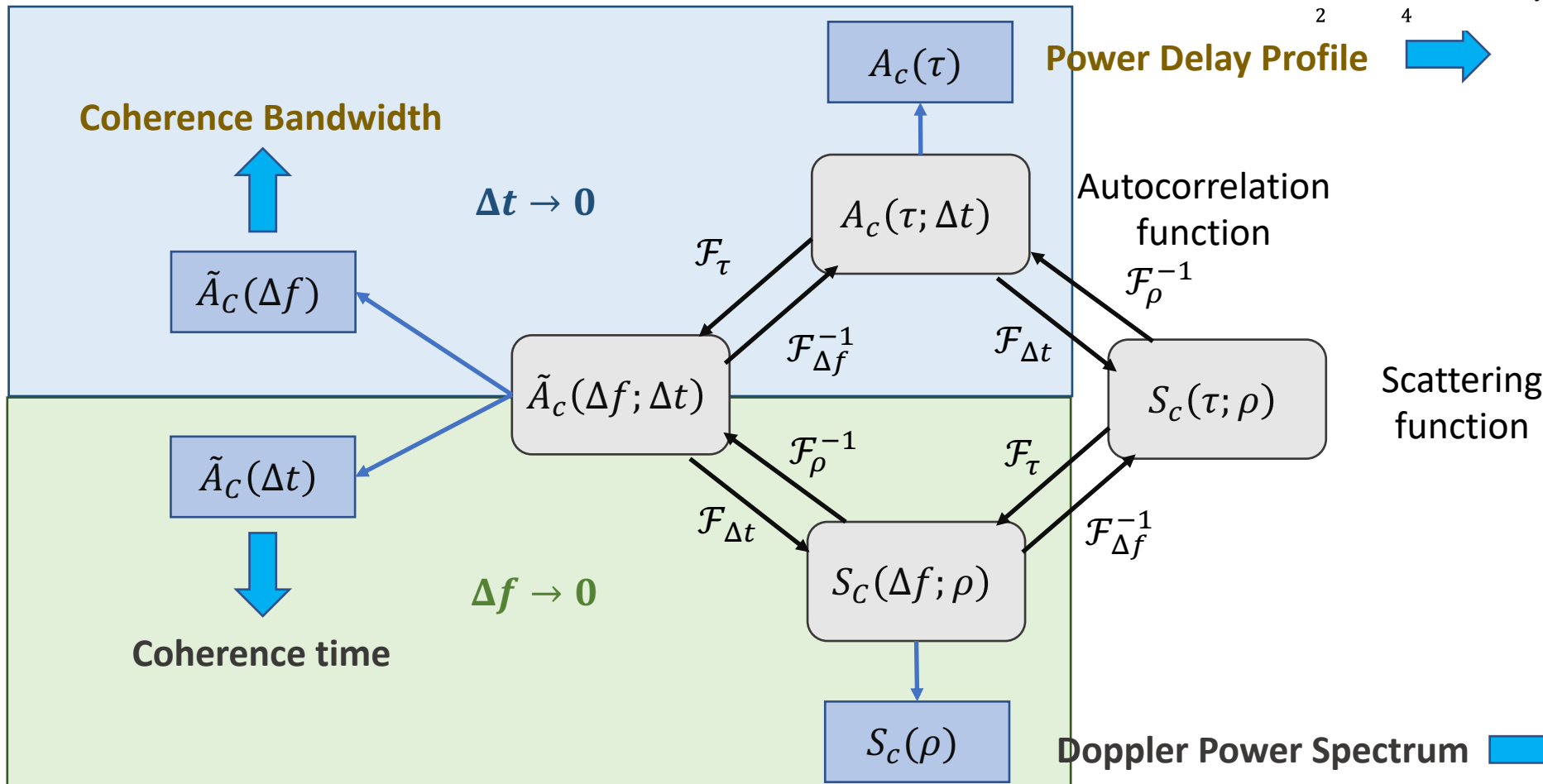


Power Delay Profile

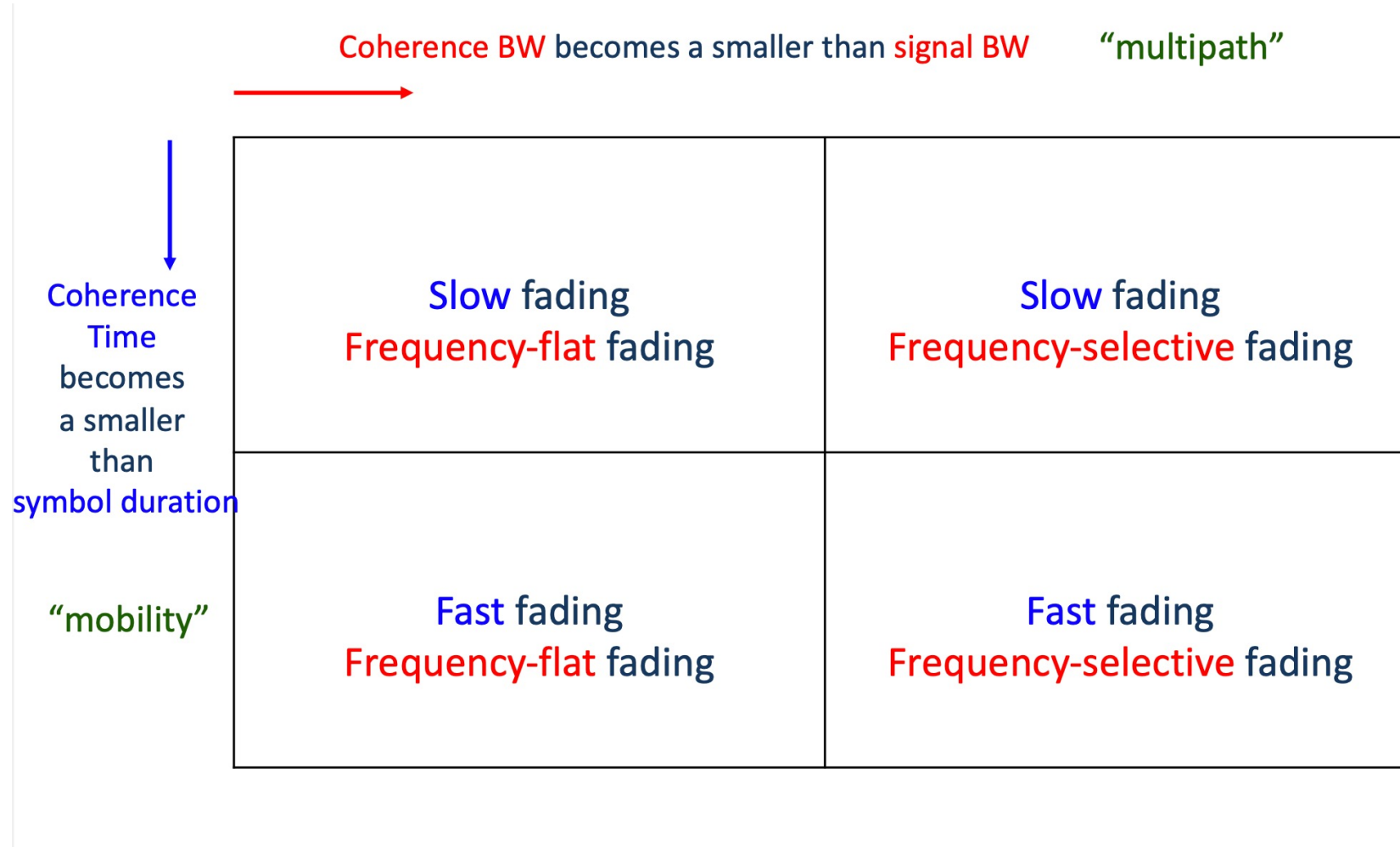
**Delay Spread**

$$\sigma_\tau = \sqrt{\tau^2 - \bar{\tau}^2}$$

$$\bar{\tau} = \frac{\int_0^\infty S_m(\tau)\tau d\tau}{\int_0^\infty S_m(\tau)d\tau} \quad \text{and} \quad \bar{\tau}^2 = \frac{\int_0^\infty S_m(\tau)\tau^2 d\tau}{\int_0^\infty S_m(\tau)d\tau}$$



# SUMMARY



# DISCRETE-TIME BASEBAND MODEL

- Frequency Flat / Slow Fading Channel (at time domain)

$$y[n] = hs[n] + v[n]$$

- Frequency Flat / Fast Fading Channel (at time domain)

$$y[n] = h[n]s[n] + v[n]$$

Channel tracking via Wiener/Kalman filters

- Frequency Selective / Slow Fading Channel

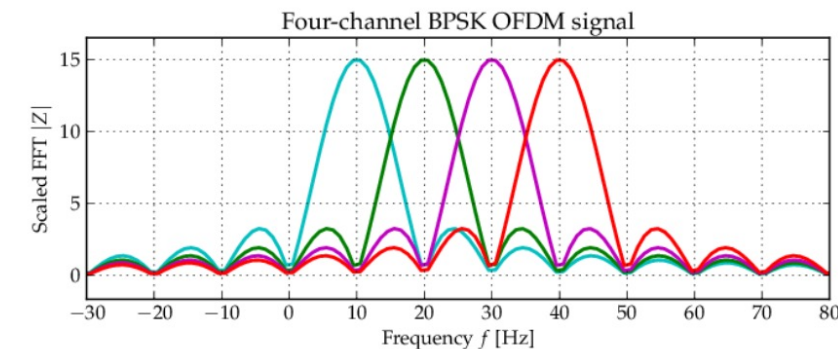
$$y[n] = \sum_{l=0}^L h[l]s[n-l] + v[n]$$

OFDM modulation

- Frequency Selective / Fast Fading Channel

$$y[n] = \sum_{l=1}^{(L)} h[n, l]s[n-l] + v[n]$$

V2V Communications





# REFERENCES

- ECE 432 Mobile Communications\_Lecture2\_Ajou\_university lecture notes by S.N. Hong & W.J Shin
- Goldsmith, Andrea. *Wireless communications*. Cambridge university press, 2005.

**QnA**

**Thank you**