

Three Musketeers

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1 NumberTheory

1.1 extended_euclidean

```
// Find a solution to ax + by = 1
int gcd(int a, int b, int& x, int& y) {
    x = 1, y = 0;
    int x1 = 0, y1 = 1, a1 = a, b1 = b;
    while (b1) {
        int q = a1 / b1;
        tie(x, x1) = make_tuple(x1, x - q * x1);
        tie(y, y1) = make_tuple(y1, y - q * y1);
        tie(a1, b1) = make_tuple(b1, a1 - q * b1);
    }
    return a1;
}

// find any solution to ax + by = c (g will store their gcd).
// Generalized x and y can be given by: x = x0 + r*lcm(a,b) and y = y0 - r*lcm(a,b)
bool find_any_solution(long long a, long long b, long long c, long long &x0, long long &y0, long long &g) {
    g = gcd(abs(a), abs(b), x0, y0);
    if (c % g) {
        return false;
    }
    x0 *= c / g;
    y0 *= c / g;
    if (a < 0) x0 = -x0;
    if (b < 0) y0 = -y0;
    return true;
}
```

1.2 factorizer

```
#define mp make_pair
using i32 = int32_t;
using i64 = int64_t;
using i128 = __int128_t;
namespace factorizer {
constexpr i128 mult(i128 a, i128 b, i128 mod) {
    i128 ans = 0;
    while (b) {
        if (b & 1) {
            ans += a;
            if (ans >= mod) ans -= mod;
        }
        a <<= 1;
        if (a >= mod) a -= mod;
        b >>= 1;
    }
    return ans;
}
constexpr i64 mult(i64 a, i64 b, i64 mod) {
    return (i128)a * b % mod;
}
constexpr i32 mult(i32 a, i32 b, i32 mod) {
    return (i64)a * b % mod;
}

template <typename T>
constexpr T f(T x, T c, T mod) {
```

```
T ans = mult(x, x, mod) + c;
if (ans >= mod) ans -= mod;
return ans;
}

template <typename T>
constexpr T brent(T n, T x0 = 2, T c = 1) {
    T x = x0;
    T g = 1;
    T q = 1;
    T xs, y;

    int m = 128;
    int l = 1;
    while (g == 1) {
        y = x;
        for (int i = 1; i < l; i++) x = f(x, c, n);
        int k = 0;
        while (k < l && g == 1) {
            xs = x;
            for (int i = 0; i < m && i < l - k; i++) {
                x = f(x, c, n);
                q = mult(q, abs(y - x), n);
            }
            g = __gcd(q, n);
            k += m;
        }
        l *= 2;
    }
    if (g == n) {
        do {
            xs = f(xs, c, n);
            g = __gcd(abs(xs - y), n);
        } while (g == 1);
    }
    return g;
}

template <typename T>
T binpower(T base, T e, T mod) {
    T result = 1;
    base %= mod;
    while (e) {
        if (e & 1) result = mult(result, base, mod);
        base = mult(base, base, mod);
        e >>= 1;
    }
    return result;
}

template <typename T>
bool check_composite(T n, T a, T d, int s) {
    T x = binpower(a, d, n);
    if (x == 1 || x == n - 1) return false;
    for (int r = 1; r < s; r++) {
        x = mult(x, x, n);
        if (x == n - 1) return false;
    }
    return true;
};

template <typename T>
bool MillerRabin(T n, const vector<T>& bases) {
    // returns true if n is prime,
    // else returns false.

    if (n < 2) return false;
```

```

int r = 0;
T d = n - 1;
while ((d & 1) == 0) {
    d >>= 1;
    r++;
}

for (T a : bases) {
    if (n == a) return true;
    if (check_composite(n, a, d, r)) return false;
}
return true;
}

template <typename T>
bool IsPrime(T n, const vector<T>& bases) {
    if (n < 2) {
        return false;
    }
    vector<T> small_primes = {2, 3, 5, 7, 11, 13, 17,
        19, 23, 29};
    for (const auto& x : small_primes) {
        if (n % x == 0) {
            return n == x;
        }
    }
    if (n < 31 * 31) {
        return true;
    }

    return MillerRabin(n, bases);
}

bool IsPrime(i64 n) {
    return IsPrime(n, {2, 3, 5, 7, 11, 13, 17, 19, 23,
        29, 31, 37});
}

bool IsPrime(i32 n) { return IsPrime(n, {2, 7, 61}); }

template <typename T>
vector<pair<T, int>> MergeFactors(const vector<pair<T,
    int>>& a,
                                const vector<pair<T,
    int>>& b) {

    vector<pair<T, int>> c;
    int i = 0;
    int j = 0;
    while (i < (int)a.size() || j < (int)b.size()) {
        if (i < (int)a.size() && j < (int)b.size() &&
            a[i].first == b[j].first) {
            c.emplace_back(a[i].first, a[i].second +
                b[j].second);
            ++i;
            ++j;
            continue;
        }
        if (j == (int)b.size() ||
            (i < (int)a.size() && a[i].first <
                b[j].first)) {
            c.push_back(a[i++]);
        } else {
            c.push_back(b[j++]);
        }
    }
    return c;
}

```

```

}

template <typename T>
vector<pair<T, int>> RhoC(T n, T c) {
    if (n <= 1) return {};
    if (!(n & 1))
        return MergeFactors({mp(static_cast<T>(2), 1)},
            RhoC(n >> 1, c));
    if (IsPrime(n)) return {mp(n, 1)};
    T g = brent(n, static_cast<T>(2), c);
    return MergeFactors(RhoC(g, c + 1), RhoC(n / g, c +
        1));
}

template <typename T>
vector<pair<T, int>> Factorize(T n) {
    if (n <= 1) return {};
    return RhoC(n, static_cast<T>(1));
}
// example factorizer::Factorize(35)

```

1.3 floor_sum

```

// f(a,b,c,n) = \sigma ( (a*x + b)/c ) from x=0 to n in
//O(logn) where value is floor of the value.
long long FloorSumAP(long long a, long long b,
    long long c, long long n){
    if(!a) return (b / c) * (n + 1);
    if(a >= c or b >= c) return ( (n * (n + 1) ) / 2) *
        (a / c)
        + (n + 1) * (b / c) + FloorSumAP(a % c, b % c, c, n);
    long long m = (a * n + b) / c;
    return m * n - FloorSumAP(c, c - b - 1, a, m - 1);
}

```

1.4 cipolla_sqrt

```

template<int p>
class cipolla_sqrt{
private:
    static int const phim = p-2;
    static int const phi = p-1;
    static int const phihalf = phi>>1;
    static int const phalf = (p+1)>>1;
public:
    static int pow(int a,int po=phim){
        int res = 1;
        for(;po;po>>=1,a=normalise(a*1ll*a))
            if(po&1){
                res=normalise(a*1ll*res);
            }
        return res;
    }
    static int normalise(ll x){
        if(x>=p){
            x-=p;if(x>=p)x%=p;return x;
        }
    }
    static int get(int x){
        int a = 0,b;
        while(
            pow(b = normalise(a*1ll*a-x+p),
                phihalf)==1

```

```

)++a;
int po = phalf;
pair<int,int> v = {a,1}, res = {1,1};
while(po){
    if(po&1){
        int temp = normalise(res.S*1ll*v.S);
        res.S = normalise((v.F*1ll*res.S)
            +(res.F*1ll*v.S));
        res.F = normalise((v.F*1ll*res.F)
            +(b*1ll*temp));
    }
    po>>=1;
    int temp = normalise(v.S*1ll*v.S);
    v.S = normalise((v.F*1ll*v.S)
        +(v.F*1ll*v.S));
    v.F = normalise((v.F*1ll*v.F)
        +(b*1ll*temp));
}
if(res.F==1)res.F = p - res.F;
return res.F;
}
};

```

2 Strings

2.1 manacher

```

vector<vector<int>> d;
// d[0] contains half the length of max palindrome of
// odd length with centre at i
// d[1] contains half the length of max palindrome of
// even length with right centre at i

void manacher(string s){
    int n = s.size();
    d.resize(n,vector<int>(2));
    for (int t = 0; t < 2; t++) {
        int l = 0, r = -1, j;
        for (int i = 0; i < n; i++) {
            j = (i > r) ? 1 :
                min(d[l+r-i+t][t],r-i+t) + 1;

            while (
                i + j - t < n && i - j >= 0
                && s[i + j - t] == s[i - j]) j++;

            d[i][t] = --j;
            if (i + j + t > r) {
                l = i - j; r = i + j - t;
            }
        }
    }
}

```

2.2 suffix_array

```

// Time Complexity: O(nlogn)

void count_sort(vector<int> &p,vector<int> &c){ //
    Sorts values in p by keys in c i.e, if c[p[i]] <
    c[p[j]] then i appears before j in p.
    int n = p.size();
    vector<int> cnt(n);

```

```

for(auto x : c) cnt[x]++;
vector<int> p_new(n),pos(n);
pos[0] = 0;
for(int i=1;i<n;++i) pos[i] = pos[i-1] + cnt[i-1];
for(auto x : p){
    int i = c[x];
    p_new[pos[i]] = x;
    pos[i]++;
}
p = p_new;
}

// Returns sorted suffix_array of size (n+1) with first
// element = n (empty suffix).
vector<int> suffix_array(string s){
    s += '$';
    int n = s.size();
    vector<int> p(n),c(n); // p stores suffix array and
    // c stores its equivalence class
    {
        // k = 0 phase
        vector<pair<char,int>> a(n);
        for(int i=0;i<n;++i) a[i] = {s[i],i};
        sort(all(a));
        for(int i=0;i<n;++i) p[i] = a[i].S;
        c[p[0]] = 0;
        for(int i=1;i<n;++i){
            if(a[i].F == a[i-1].F) c[p[i]] = c[p[i-1]];
            else c[p[i]] = c[p[i-1]] + 1;
        }
    }
    int k=0;
    while((1<<k) < n ){ // k -> k + 1
        // We require to sort p by {c[i], c[i+(1<<k)]}
        // value. So we use radix sort: Sort the
        // second element of pair then count sort
        // first element in a stable fashion.
        // Sort by second element: p[i] -> (1<<k). As
        // p[i]'s are already sorted by c[i] values.
        for(int i = 0; i < n ; ++i) p[i] = (p[i] -
            (1<<k) + n )%n;
        count_sort(p,c);

        vector<int> c_new(n);
        c_new[p[0]] = 0;
        for(int i=1;i<n;++i){
            pii prev = {c[p[i-1]] , c[(p[i-1] +
                (1<<k))%n] } ;
            pii now = {c[p[i]] , c[(p[i] + (1<<k))%n] } ;
            if( now == prev) c_new[p[i]] = c_new[p[i-1]];
            else c_new[p[i]] = c_new[p[i-1]] + 1;
        }
        c = c_new;
        ++k;
    }
    return p;
}

```

```

vector<int> lcp_array(vector<int> &p,vector<int>
    &c,string s){
    int n = p.size();
    vector<int> lcp(n-1);
    int k=0;
    for(int i=0;i<n-1;++i){
        int pi = c[i];
        int j = p[pi-1];

```

```

        //lcp[i] = lcp[s[i...],s[j...]]
        while(s[i+k] == s[j+k]) ++k;
        lcp[pi-1] = k;
        k = max(k-1,0);
    }
    return lcp;
}
// Finds lcp using p and
// c array defined in suffix array

```

2.3 aho_corasick

```

const static int K = 26;
// Will change if input is not just lowercase alphabets
struct Vertex {
    int next[K];
    int leaf = 0;
    // It actually denotes number of leafs reachable
    // from current vertexes using links.
    int p = -1;
    char pch;
    int link = -1;
    int go[K];

    Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
        fill(begin(next), end(next), -1);
        fill(begin(go), end(go), -1);
    }
};
vector<Vertex> t;
// Automation is stored in form of vector.

// Add String s to the automaton.
void add_s(string const& s) {
    int v = 0;
    for (char ch : s) {
        int c = ch - 'a';
        if (t[v].next[c] == -1) {
            t[v].next[c] = t.size();
            t.emplace_back(v, ch);
        }
        v = t[v].next[c];
    }
    t[v].leaf += 1;
}

// Forward declaration of functions
int go(int v, char ch);

// gets the link from vertex v.
int get_link(int v) {
    if (t[v].link == -1) {
        if (v == 0 || t[v].p == 0)
            t[v].link = 0;
        else
            t[v].link = go(get_link(t[v].p), t[v].pch);
    }
    return t[v].link;
}

int go(int v, char ch) {
    int c = ch - 'a';
    // May change if not lowercase alphabet
    if (t[v].go[c] == -1) {
        if (t[v].next[c] != -1)

```

```

        t[v].go[c] = t[v].next[c];
    } else
        t[v].go[c] = v == 0 ? 0 :
            go(get_link(v), ch);
    }
    return t[v].go[c];
}

// To calculate links and leafs(exit link) for nodes.
void bfs() {
    queue<int> order;
    order.push(0);
    while(!order.empty()) {
        int cur = order.front(); order.pop();
        t[cur].link = get_link(cur);
        t[cur].leaf += t[t[cur].link].leaf;
        for(int i=0;i<K;++i) {
            if(t[cur].next[i] != -1) {
                order.push(t[cur].next[i]);
            }
        }
    }
}

```

3 Polynomials

3.1 poly_mono

```

const int P1 = 880803841, G1 = 26; //(105*2^23)+1
const int P2 = 897581057, G2 = 3; //(107*2^23)+1
const int P3 = 998244353, G3 = 3; //(119*2^23)+1
const int primitive = 3;

#define u32      __uint32_t
#define u64      __uint64_t
#define vi      vector<int>
#define v64      vector<u64>
#define all(x)   x.begin(),x.end()
template<int mod>
constexpr int powmod(int a,int p = mod -2){
    int res = 1;
    while(p){
        if(p&1)res = (res*1ll*a)%mod;
        p>>=1;
        a = (a*1ll*a)%mod;
    }
    return res;
}

template<int max_base,int mod,int primitive>
class Ntt{
private:
    constexpr static v64 fill(const int o){
        vector<u64> res(max_base);
        const int m = max_base>>1;
        res[m] = (1ll<<32)%mod;
        for(int i = m+1;i<max_base;++i)
            res[i] = reduce(res[i-1]*1ll*o);
        for(int i = m-1;i--i) res[i] = res[i<<1];
        res[0] = (1ll<<32)%mod;
        return res;
    }
    constexpr static v64 init_omegas(){
        const int omega =
            (powmod<mod>(primitive,(mod-1)/
                max_base)*(1ll<<32))%mod;

```

```

    return fill(omega);
}
constexpr static v64 init_iomegas(){
    const int omega =
        powmod<mod>(primitive, (mod-1)/max_base);
    const int iomega =
        (powmod<mod>(omega)*(1ll<<32))%mod;
    return fill(iomega);
}
static const v64 omegas, iomegas;
constexpr static u32 init_mod_inv(){
    u32 inv = mod;
    for(int i=0; i<4; ++i) inv*=(2-(mod*inv));
    return -inv;
}
static const u32 mod_inv = init_mod_inv(),
    mod32 = mod;
static const u64 mod64 = mod;
public:
    // use to combine if using fft explicitly
    // see mul for details
    static const inline u32 reduce(u64 x){
        u32 m = static_cast<u32>(x)*mod_inv;
        u32 t = (x+m*mod64)>>32;
        if(t>=mod)t-=mod;
        return t;
    }
    static void fft(vi &a){
        int n = a.size();
        for(int m=n>>1; m>=1){
            auto it_start = omegas.begin()+m;
            auto it_end = it_start+m;
            for(auto l = a.begin(); l!=a.end(); l+=m){
                for(auto it = it_start;
                    it!=it_end; ++it, ++l){
                    int e = *l-l[m];
                    if(e<0)e+=mod;
                    *l+=l[m];
                    if(*l>=mod)*l-=mod;
                    l[m] = reduce(e* *it);
                }
            }
        }
    }
    static void ifft(vi &a){
        int n = a.size();
        for(int m=1; m<n; m<=1){
            auto it_start = iomegas.begin()+m;
            auto it_end = it_start+m;
            for(auto l = a.begin(); l!=a.end(); l+=m){
                for(auto it = it_start;
                    it!=it_end; ++it, ++l){
                    l[m] = reduce(l[m]* *it);
                    int e = *l-l[m];
                    if(e<0)e+=mod;
                    *l+=l[m];
                    if(*l>=mod)*l-=mod;
                    l[m] = e;
                }
            }
        }
        u64 f = (((1ll<<32)*omegas[0])/a.size())%mod;
        for(int i=0; i<a.size(); ++i)
            a[i] = reduce(a[i]*f);
    }
    static vi mul(vi a, vi b){
        int need = a.size()+b.size()-1;

```

```

        int nbase = 1<<(32-__builtin_clz(need-1));
        a.resize(nbase); b.resize(nbase);
        fft(a); fft(b);
        for(int i=0; i<nbase; ++i)
            a[i]=reduce(a[i]*1ll*b[i]);
        ifft(a);
        a.resize(need);
        return a;
    }
    static vi inv(vi &a){
        int n = a.size(), k=1;
        vi res(1, powmod<mod>(a[0]));
        while(k<n){
            int l = k<<1;
            int need = l<<1;
            if(l>n)a.resize(l);
            res.resize(need);
            vi temp(a.begin(), a.begin()+l);
            temp.resize(need); fft(temp); fft(temp);
            for(int i=0; i<need; ++i)
                res[i] = reduce(temp[i]*1ll*
                    reduce(res[i]*1ll*res[i]));
            ifft(res);
            for(int i=k; i<l; ++i)
                if(res[i]) res[i]=mod-res[i];
            k = l;
        }
        a.resize(n); res.resize(n);
        return res;
    }
};

template<int max_base, int mod, int primitive> const v64
    Ntt<max_base, mod, primitive>::omegas =
        init_omegas();
template<int max_base, int mod, int primitive> const v64
    Ntt<max_base, mod, primitive>::iomegas =
        init_iomegas();

const int mod = 998244353;
const int base = 1<<20;
vi& operator *= (vi& a, const vi& b){
    if(a.empty() || b.empty()) a.clear();
    else a = Ntt<base, mod, primitive>::mul(a, b);
    return a;
}
vi operator * (const vi& a, const vi& b){
    vi c = a; return c*=b;
}
vi& operator /= (vi& a, const vi& b){
    if(a.size()<b.size()) a.clear();
    else{
        vi d = b;
        reverse(d.begin(), d.end());
        reverse(a.begin(), a.end());
        int deg = a.size()-b.size();
        a.resize(deg+1);
        d.resize(deg+1);
        d = Ntt<base, mod, primitive>::inv(d);
        a*=d; a.resize(deg+1);
        reverse(a.begin(), a.end());
    }
    return a;
}
vi operator / (vi& a, const vi& b){
    vi c = a; return c/=b;
}

```

```

vi& operator += (vi& a,const vi& b){
    if(a.size()<b.size())a.resize(b.size());
    for(int i=0;i<b.size();++i){
        a[i]+=b[i];
        if(a[i]>=mod)a[i]-=mod;
    }
    return a;
}
vi operator + (const vi& a,const vi& b){
    vi c = a;return c+=b;
}
vi& operator -= (vi& a,const vi& b){
    if(a.size()<b.size())a.resize(b.size());
    for(int i=0;i<b.size();++i){
        a[i]-=b[i];
        if(a[i]<0)a[i]+=mod;
    }
    return a;
}
vi operator - (const vi& a,const vi& b){
    vi c = a;
    return c-=b;
}
vi& operator /= (vi& a,const vi& b){
    if(a.size()<b.size())return a;
    vi c = (a/b)*b;
    a -= c;
    a.resize(b.size()-1);
    return a;
}
vi operator % (const vi& a,const vi& b){
    vi c = a;return c%=b;
}

```

3.2 poly_arbitrary

```

typedef long long i64;
typedef complex<double> im;

const int o = 20, len = 1 << o, mod = 1e9 + 7;
const double pi = acos(-1.0);

namespace poly {
int r[len], up, l;
im w[len], iw[len], I(0, 1);

void init() {
    w[1] = iw[1] = im(1, 0);
    for (int l = 2; l != len; l <= 1) {
        double x = cos(pi / l), y = sin(pi / l);
        im p(x, y), ip(x, -y);
        for (int i = 0; i != l; i += 2) {
            w[l + i] = w[(l + i) >> 1], iw[l + i] = iw[(l + i) >> 1];
            w[l + i + 1] = w[l + i] * p, iw[l + i + 1] = iw[l + i] * ip;
        }
    }
    for (int i = (len >> 1) - 1; i; i--)
        w[i] = w[i << 1], iw[i] = iw[i << 1];
    for (int i = 0; i != len; i++)
        r[i] = (r[i >> 1] >> 1) | ((i & 1) << (o - 1));
}

int pre(int n) {

```

```

    l = 32 - __builtin_clz(n), up = 1 << l;
    return up;
}

void fft(im *a, int n, bool op, im *w) {
    for (int i = 0; i != n; i++) {
        int t = r[i] >> (o - l);
        if (i < t)
            swap(a[i], a[t]);
    }
    for (int l = 1; l != n; l <= 1) {
        im *k = w + l;
        for (im *f = a; f != a + n; f += l)
            for (im *j = k; j != k + l; j++, f++) {
                im x = *f, y = f[l] * *j;
                f[l] = x - y, *f += y;
            }
    }
    if (op)
        for (int i = 0; i != n; i++)
            a[i] /= n;
}

vector<int> mul(vector<int> &f, vector<int> &g) {
    int n = f.size()-1, m = g.size()-1;
    static im a[len], b[len], c[len], d[len];
    pre(n + m);
    int mm = sqrt(mod);
    for (int i = 0; i <= n; i++)
        a[i] = im(f[i] % mm, f[i] / mm);
    for (int i = 0; i <= m; i++)
        b[i] = im(g[i] % mm, g[i] / mm);
    fft(a, up, 0, w), fft(b, up, 0, w);
    for (int i = 0; i != up; i++) {
        a[i] /= 2, b[i] /= 2;
        c[i] = im(a[i].real(), -a[i].imag()),
        d[i] = im(b[i].real(), -b[i].imag());
    }
    reverse(c + 1, c + up), reverse(d + 1, d + up);
    for (int i = 0; i != up; i++) {
        im a0 = a[i] + c[i], a1 = (c[i] - a[i]) * I;
        im b0 = b[i] + d[i], b1 = (d[i] - b[i]) * I;
        a[i] = a0 * b0 + I * a1 * b1,
        b[i] = a0 * b1 + I * a1 * b0;
    }
    fft(a, up, 1, iw), fft(b, up, 1, iw);
    auto num = [](double x) {
        return (i64)round(x) % mod;
    };
    vector<int> h(n+m+1);
    for (int i = 0; i <= n + m; i++){
        h[i] = (num(a[i].real())
                + num(a[i].imag()) * mm * mm
                + (num(b[i].real())
                + num(b[i].imag())) * mm) % mod;
    }
    for (int i = 0; i != up; i++)
        a[i] = b[i] = c[i] = d[i] = 0;
    return h;
}
}
// namespace poly please call poly::init()
// and set o,len,mod accordingly

```

3.3 poly_bitwise


```

void muland(vector<int> &a, int inv) {
    int n = a.size();
    for(int len = 1; 2*len <= n; len <= 1) {
        for(int i=0; i<n; i+=2*len) {
            for(int j=0; j<len; ++j) {
                int str = a[i+j];
                if(!inv) {
                    a[i+j] = a[i+j+len];
                    a[i+j+len] += str;
                } else {
                    a[i+j] = -str+a[i+j+len];
                    a[i+j+len] = str;
                }
            }
        }
    }
}

void mulor(vector<int> &a, int inv) {
    int n = a.size();
    for(int len = 2; len <= n; len <= 1) {
        for(int i=0; i<n; i+=len) {
            for(int j=0; j<len/2; ++j) {
                int str = a[i+j];
                if(!inv) {
                    a[i+j] += a[i+j+len/2];
                    a[i+j + len/2] = str;
                } else {
                    a[i+j] = a[i+j+len/2];
                    a[i+j + len/2] = str
                        - a[i+j+len/2];
                }
            }
        }
    }
}

void mulxor(vector<int> &a, int inv) {
    int n = a.size();
    for(int len = 2; len <= n; len <= 1) {
        for(int i=0; i<n; i+=len) {
            for(int j=0; j<len/2; ++j) {
                int str = a[i+j];
                a[i+j] = a[i+j] + a[i+j+len/2];
                a[i+j + len/2] = str - a[i+j+len/2];
            }
        }
    }
    if(inv) for(int i=0; i<n; ++i) a[i]/=n;
}

vector<int> Multiand(vector<int> &a, vector<int> &b) {
    int n = max(b.size(), a.size());
    int i=1;
    while(n > i) {
        i*=2;
    } n = i;
    while(a.size()!=n) a.pb(0);
    while(b.size()!=n) b.pb(0);

    muland(a,0); muland(b,0);
    vector<int> ans;
    for(int i=0; i<a.size(); ++i)
        ans.pb(a[i]*b[i]);
    muland(ans,1);
    return ans;
}

```

}

4 Trees

4.1 centroid_decomposition

```

const int N=200005; // Change based on constraint
set<int> G[N]; // adjacency list (note that this is
               // stored in set, not vector)
int sz[N], pa[N];

int dfs(int u, int p) {
    sz[u] = 1;
    for(auto v : G[u]) if(v != p) {
        sz[u] += dfs(v, u);
    }
    return sz[u];
}

int centroid(int u, int p, int n) {
    for(auto v : G[u]) if(v != p) {
        if(sz[v] > n / 2) return centroid(v, u, n);
    }
    return u;
}

void build(int u, int p) {
    int n = dfs(u, p);
    int c = centroid(u, p, n);
    if(p == -1) p = c;
    pa[c] = p;

    vector<int> tmp(G[c].begin(), G[c].end());
    for(auto v : tmp) {
        G[c].erase(v); G[v].erase(c);
        build(v, c);
    }
}

```

4.2 top_tree

```

// should have identity transform
struct Transform{
    long long val;
    Transform():val(0ll){}
    Transform(long long _val):val(_val){}
    Transform& operator +=(Transform &other){
        val+=other.val;
        return *this;
    }
    bool isLazy()const{return val;}
};

// transforming values and summing = summing and
// transforming
// sum is commutative and associative
// transforming identity = identity
struct Val{
    int n;
    long long val;
    Val(int _n, long long _val):n(_n),val(_val){}
    Val(long long _val):n(1),val(_val){}
    Val():n(0),val(0){}
    Val operator +(Val &other)const{
        return Val(n+other.n, val+other.val);};
}

```

```

Val& operator +=(Transform
    &T){val+=(n*T.val);return *this;}
bool isIdentity()const{return n==0;}
};

template<typename val, typename transform>
class TopTree{
public:
    struct Splay{
        struct node{
            int l,r,ar,p;
            bool flip;
            val self, path, sub, all;
            transform lazyPath, lazySub;
            node():
                l(0),r(0),ar(0),p(0),flip(false){}
            node(int _val):
                l(0),r(0),ar(0),p(0),flip(false),
                self(_val), path(_val), all(_val){}
        };
        int stx;
        vector<node> nodes;
        Splay(int n,int q){
            nodes.assign(n+q+1,node(0));
            nodes[0] = node();
            for(int i=n+1;i<nodes.size();++i)
                nodes[i] = nodes[0];
            stx = n;
        }
        inline void lazyApplyPath(int u, transform &T){
            if(!nodes[u].path.isIdentity()){
                nodes[u].self+=T,nodes[u].path+=T,
                nodes[u].lazyPath+=T;
                nodes[u].all =
                    nodes[u].path+nodes[u].sub;
            }
        }
        inline void lazyApplySub(int u, transform &T){
            if(!nodes[u].sub.isIdentity()){
                nodes[u].sub+=T,nodes[u].lazySub+=T;
                nodes[u].all =
                    nodes[u].path+nodes[u].sub;
            }
        }
        inline void flip(int u){
            swap(nodes[u].l,nodes[u].r);
            nodes[u].flip^=1;
        }
        inline void push(int u){
            if(nodes[u].lazyPath.isLazy()){
                lazyApplyPath(nodes[u].l,
                    nodes[u].lazyPath),
                lazyApplyPath(nodes[u].r,
                    nodes[u].lazyPath);
                nodes[u].lazyPath = transform();
            }
            if(nodes[u].lazySub.isLazy()){
                lazyApplySub(nodes[u].l,
                    nodes[u].lazySub),
                lazyApplySub(nodes[u].r,
                    nodes[u].lazySub),
                lazyApplySub(nodes[u].ar,
                    nodes[u].lazySub),
                lazyApplyPath(nodes[u].ar,
                    nodes[u].lazySub);
                nodes[u].lazySub = transform();
            }
        }
    };

```

```

        if(nodes[u].flip){
            nodes[u].flip = false;
            flip(nodes[u].l);
            flip(nodes[u].r);
        }
    }
    inline void pull(int u){
        if(!u)return;
        int lc = nodes[u].l, rc = nodes[u].r,
            ar = nodes[u].ar;
        nodes[u].path = nodes[lc].path
            +nodes[u].self
            +nodes[rc].path;
        nodes[u].sub = nodes[lc].sub
            +nodes[rc].sub
            +nodes[ar].all;
        nodes[u].all = nodes[u].path+nodes[u].sub;
    }
    inline void rotate(int u){
        int p = nodes[u].p;
        if(nodes[p].r==u){
            nodes[p].r = nodes[u].l;
            if(nodes[u].l)
                nodes[nodes[u].l].p = p;
            nodes[u].l = p;
        }
        else{
            nodes[p].l = nodes[u].r;
            if(nodes[u].r)
                nodes[nodes[u].r].p = p;
            nodes[u].r = p;
        }
        nodes[u].p = nodes[p].p;
        nodes[p].p = u;
        if(nodes[nodes[u].p].l == p)
            nodes[nodes[u].p].l = u;
        else if(nodes[nodes[u].p].r == p)
            nodes[nodes[u].p].r = u;
        else if(nodes[nodes[u].p].ar == p)
            nodes[nodes[u].p].ar = u;
    }
    inline void splay(int x){
        while((nodes[nodes[x].p].l==x)||
            (nodes[nodes[x].p].r==x)){
            int y = nodes[x].p;
            int z = nodes[y].p;
            if((nodes[z].l==y)|| (nodes[z].r==y)){
                push(z);push(y);push(x);
                if((nodes[z].l==y)&&(
                    nodes[y].l==x))||
                    ((nodes[z].r==y)&&(
                        nodes[y].r==x)))
                    rotate(y);
                else
                    rotate(x);
                rotate(x);
                pull(z);pull(y);pull(x);
            }
            else{
                push(y);push(x);
                rotate(x);
                pull(y);pull(x);
            }
        }
        push(x);
    }
    inline void detach(int u){

```

```

push(u);
if(nodes[u].r){
    if(nodes[nodes[u].ar].ar
        ||(!nodes[u].ar)){
        nodes[++stx].r = nodes[u].ar;
        nodes[stx].p = u;
        if(nodes[stx].r)
            nodes[nodes[stx].r].p = stx;
        nodes[u].ar = stx;
    }
    else
        push(nodes[u].ar);
    nodes[nodes[u].ar].ar = nodes[u].r;
    nodes[nodes[u].r].p = nodes[u].ar;
    nodes[u].r = 0;
    pull(nodes[u].ar);
    pull(u);
}
}
inline int access(int u){
    int x = u;
    int v = u;
    while(x){
        splay(x);
        if(u!=x){
            push(nodes[x].ar);
            swap(nodes[x].r,
                nodes[nodes[x].ar].ar);
            if(nodes[x].r)
                nodes[nodes[x].r].p = x;
            if(nodes[nodes[x].ar].ar)
                nodes[nodes[nodes[x].ar].ar].p =
                    nodes[x].ar;
            pull(nodes[x].ar);
            pull(x);
        }
        else
            detach(x);
        v = x;
        x = nodes[x].p;
    }
    if(x){
        splay(x);
        x = nodes[x].p;
    }
    splay(u);
    return v;
}
void root(int x){
    access(x);flip(x);push(x);
}
};
Splay S;
int root;
TopTree(int _n, int _q,int
    _root):S(_n,_q*2),root(_root){}
void updateSub(int x,transform T){
    S.root(root);S.access(x);
    int y = S.nodes[x].l;
    S.nodes[x].l = 0;
    S.pull(x);
    S.lazyApplyPath(x, T),S.lazyApplySub(x, T);
    S.push(x);S.nodes[x].l = y;S.pull(x);
}
void updatePath(int x,int y,transform T){
    S.root(x);S.access(y);S.lazyApplyPath(y, T);
}

```

```

void reroot(int r){root = r;}
val getPath(int x,int y){
    S.root(x);S.access(y);
    return S.nodes[y].path;
}
val getSub(int x){
    S.root(root);S.access(x);
    return S.nodes[x].self
        +S.nodes[S.nodes[x].r].path
        +S.nodes[S.nodes[x].ar].all;
}
void link(int x,int y){
    S.root(x);S.access(y);
    S.nodes[y].r = x,S.nodes[x].p = y;
    S.pull(y);
}
int lca(int x,int y){
    S.root(root);S.access(y);
    return S.access(x);
}
void changePar(int x,int y){
    if(lca(x,y)!=x){
        S.nodes[S.nodes[x].l].p = 0;
        S.nodes[x].l = 0;S.pull(x);
        link(x,y);
    }
}
void cut(int u){
    S.root(root);S.access(u);
    S.nodes[S.nodes[u].l].p = 0;
    S.nodes[u].l = 0;S.pull(u);
}
};

```

5 Graphs

5.1 max_flow

/*
Implementation of Dinic's blocking algorithm
for the maximum flow.
Complexity: $V^2 E$ (faster on real graphs).

please add edges not related to input first
to improve constants

This class accepts a graph
(costructed calling AddEdge) and then solves
the maximum flow problem for any source and sink.

Both directed and undirected graphs are supported.
In case of undirected graphs,
each edge must be added twice.

To compute the maximum flow just call
GetMaxFlowValue(source, sink).
*/

```

template <typename T>
struct Dinic {
    struct Edge {
        int u, v;
        T cap, flow;
        Edge() {}
    }

```

```

Edge(int u, int v, T cap): u(u), v(v),
    cap(cap), flow(0) {}
};

int N;
vector<Edge> edges; // The "inverse" edge of
    edges[i] is edges[i^1].
vector<vector<int>> aa; // Stores the index of the
    edge in the edges vector.
// dist is the distance in the bfs.
// pt is used internally to save time in the dfs.
vector<int> dist, pt;

Dinic(int N): N(N), edges(0), aa(N), dist(N), pt(N)
{}

void AddEdge(int u, int v, T cap) {
    assert(0 <= u and u < N);
    assert(0 <= v and v < N);
    // dbg(u, v, cap);
    if (u != v) {
        edges.push_back(Edge(u, v, cap));
        aa[u].push_back(edges.size() - 1);
        // The inverse edge has 0 capacity.
        edges.push_back(Edge(v, u, 0));
        aa[v].push_back(edges.size() - 1);
    }
}

// Computes all distances from source and stores
    them in dist.
// It returns true if sink is reachable from source.
bool BFS(int source, int sink) {
    queue<int> q({source});
    fill(dist.begin(), dist.end(), N + 1);
    dist[source] = 0;
    while(!q.empty()) {
        int u = q.front(); q.pop();
        if (u == sink) break;
        for (int k : aa[u]) {
            Edge &e = edges[k];
            if (e.flow < e.cap && dist[e.v] >
                dist[e.u] + 1) {
                dist[e.v] = dist[e.u] + 1;
                q.push(e.v);
            }
        }
    }
    return dist[sink] != N + 1;
}

T DFS(int u, int sink, T flow = -1) {
    if (u == sink || flow == 0) return flow;
    // ACHTUNG: Be careful of using references (&)
        where needed!
    for (int &i = pt[u]; i < (int)aa[u].size();
        i++) {
        Edge &e = edges[aa[u][i]];
        Edge &oe = edges[aa[u][i] ^ 1];
        if (dist[e.v] == dist[e.u] + 1) {
            T amt = e.cap - e.flow;
            if (flow != -1 && amt > flow) amt = flow;
            if (T pushed = DFS(e.v, sink, amt)) {
                e.flow += pushed;
                oe.flow -= pushed;
                return pushed;
            }
        }
    }
}

```

```

    }
}
return 0;
}

T GetMaxFlowValue(int source, int sink) {
    for (Edge& e : edges) e.flow = 0;
    T res = 0;
    while (BFS(source, sink)) {
        fill(pt.begin(), pt.end(), 0);
        while (T flow = DFS(source, sink)) res +=
            flow;
    }
    return res;
}
};

```

5.2 edmond_blossom_unweighted

```

struct edmond {
    int n, m, nE, n_matches, q_n, book_mark;
    vector<int> adj, nxt, go, mate, q, book, type, fa, bel;

    edmond(int n, int m): n(n), m(m) {
        nE = 0;
        n_matches = 0;
        adj.resize(n+1);
        mate.resize(n+1);
        q.resize(n+1);
        book.resize(n+1);
        type.resize(n+1);
        fa.resize(n+1);
        bel.resize(n+1);
        go.resize((m<<1)|1);
        nxt.resize((m<<1)|1);
    }

    void addEdge(const int &u, const int &v) {
        nxt[++nE] = adj[u], go[adj[u] = nE] = v;
        nxt[++nE] = adj[v], go[adj[v] = nE] = u;
    }

    void augment(int u) {
        while (u) {
            int nu = mate[fa[u]];
            mate[mate[u] = fa[u]] = u;
            u = nu;
        }
    }

    int get_lca(int u, int v) {
        ++book_mark;
        while (true) {
            if (u) {
                if (book[u] == book_mark) return u;
                book[u] = book_mark;
                u = bel[fa[mate[u]]];
            }
            swap(u, v);
        }
    }

    void go_up(int u, int v, const int &mv) {
        while (bel[u] != mv) {
            fa[u] = v;

```

```

        v = mate[u];
        if (type[v] == 1) type[q[++q_n] = v] = 0;
        bel[u] = bel[v] = mv;
        u = fa[v];
    }
}

void after_go_up() {
    for (int u = 1; u <= n; ++u) bel[u] =
        bel[bel[u]];
}

bool match(const int &sv) {
    for (int u = 1; u <= n; ++u) bel[u] = u,
        type[u] = -1;
    type[q[q_n = 1] = sv] = 0;
    for (int i = 1; i <= q_n; ++i) {
        int u = q[i];
        for (int e = adj[u]; e; e = nxt[e]) {
            int v = go[e];
            if (!~type[v]) {
                fa[v] = u, type[v] = 1;
                int nu = mate[v];
                if (!nu) {
                    augment(v);
                    return true;
                }
                type[q[++q_n] = nu] = 0;
            } else if (!type[v] && bel[u] != bel[v]) {
                int lca = get_lca(u, v);
                go_up(u, v, lca);
                go_up(v, u, lca);
                after_go_up();
            }
        }
    }
    return false;
}

void calc_max_match() {
    n_matches = 0;
    for (int u = 1; u <= n; ++u)
        if (!mate[u] && match(u)) ++n_matches;
}

/*
int main() {
    int n,m;
    cin >> n >> m;
    edmond er(n, m);
    while(m--) {
        int x,y; cin >> x >> y;
        er.addEdge(x+1, y+1); // Input should be
            strictly 1-based indexed node.
    }
    er.calc_max_match();
    cout << er.n_matches << endl;
    for(int u = 1; u <= er.n; ++u)
        if(er.mate[u] > u) cout << er.mate[u]-1 << ' ',
            << u-1 << '\n';
    return 0;
}
*/

```

5.3 edmond_blossom_weighted

```

struct Blossom {
    const long long inf = 1e18;
    static const int N = 105; // > Max number of
        vertices.
    struct edge {
        int u, v;
        long long w;
    } g[N * 2][N * 2];
    int n, n_x, match[N * 2], slack[N * 2], st[N * 2],
        pa[N * 2], flower_from[N * 2][N * 2], S[N * 2],
        vis[N * 2];
    long long lab[N * 2];
    long long dist(edge const& e) { return lab[e.u] +
        lab[e.v] - g[e.u][e.v].w * 2; }
    vector<int> flower[N * 2];
    deque<int> q;
    Blossom(int _n) {
        n = _n;
        q = deque<int>();
        for (int u = 1; u <= n * 2; ++u) {
            match[u] = slack[u] = st[u] = pa[u] = S[u] =
                vis[u] = lab[u] = 0;
            for (int v = 1; v <= n * 2; ++v) {
                g[u][v] = edge{u, v, 0};
                flower_from[u][v] = 0;
            }
            flower[u].clear();
        }
    }
    void add_edge(int u, int v, long long w) {
        ++u; ++v;
        g[u][v].w = max(g[u][v].w, w);
        g[v][u].w = max(g[v][u].w, w);
    }
    inline void update_slack(int u, int x) {
        if (!slack[x] || dist(g[u][x]) <
            dist(g[slack[x]][x])) slack[x] = u;
    }
    inline void set_slack(int x) {
        slack[x] = 0;
        for (int u = 1; u <= n; ++u) {
            if (g[u][x].w > 0 && st[u] != x && S[st[u]]
                == 0) update_slack(u, x);
        }
    }
    inline void q_push(int x) {
        if (x <= n) return q.push_back(x);
        for (int i = 0; i < (int)flower[x].size(); ++i)
            q_push(flower[x][i]);
    }
    inline void set_st(int x, int b) {
        st[x] = b;
        if (x <= n) return;
        for (int i = 0; i < (int)flower[x].size(); ++i)
            set_st(flower[x][i], b);
    }
    inline int get_pr(int b, int xr) {
        int pr = find(flower[b].begin(),
            flower[b].end(), xr) - flower[b].begin();
        if (pr % 2 == 1) {
            reverse(flower[b].begin() + 1,
                flower[b].end());
            return (int)flower[b].size() - pr;
        } else return pr;
    }
}

```

```

inline void set_match(int u, int v) {
    match[u] = g[u][v].v;
    if (u <= n) return;
    edge e = g[u][v];
    int xr = flower_from[u][e.u], pr = get_pr(u,
        xr);
    for (int i = 0; i < pr; ++i)
        set_match(flower[u][i], flower[u][i ^ 1]);
    set_match(xr, v);
    rotate(flower[u].begin(), flower[u].begin() +
        pr, flower[u].end());
}

inline void augment(int u, int v) {
    int xnv = st[match[u]];
    set_match(u, v);
    if (!xnv) return;
    set_match(xnv, st[pa[xnv]]);
    augment(st[pa[xnv]], xnv);
}

inline int get_lca(int u, int v) {
    static int t = 0;
    for (++t; u || v; swap(u, v)) {
        if (u == 0) continue;
        if (vis[u] == t) return u;
        vis[u] = t;
        u = st[match[u]];
        if (u) u = st[pa[u]];
    }
    return 0;
}

inline void add_blossom(int u, int lca, int v) {
    int b = n + 1;
    while(b <= n_x && st[b]) ++b;
    if (b > n_x) ++n_x;
    lab[b] = 0, S[b] = 0;
    match[b] = match[lca];
    flower[b].clear();
    flower[b].push_back(lca);
    for (int x = u, y; x != lca; x = st[pa[y]]) {
        flower[b].push_back(x),
        flower[b].push_back(y = st[match[x]]),
        q_push(y);
    }
    reverse(flower[b].begin() + 1, flower[b].end());
    for (int x = v, y; x != lca; x = st[pa[y]]) {
        flower[b].push_back(x),
        flower[b].push_back(y = st[match[x]]),
        q_push(y);
    }
    set_st(b, b);
    for (int x = 1; x <= n_x; ++x) g[b][x].w =
        g[x][b].w = 0;
    for (int x = 1; x <= n; ++x) flower_from[b][x]
        = 0;
    for (int i = 0; i < (int)flower[b].size(); ++i) {
        int xs = flower[b][i];
        for (int x = 1; x <= n_x; ++x) {
            if (g[b][x].w == 0 || dist(g[xs][x]) <
                dist(g[b][x]))
                g[b][x] = g[xs][x], g[x][b] =
                    g[x][xs];
        }
        for (int x = 1; x <= n; ++x) {
            if (flower_from[xs][x])
                flower_from[b][x] = xs;
        }
    }
    set_slack(b);
}

inline void expand_blossom(int b) { // S[b] == 1
    for (int i = 0; i < (int)flower[b].size(); ++i)
        set_st(flower[b][i], flower[b][i]);
    int xr = flower_from[b][g[b][pa[b]].u], pr =
        get_pr(b, xr);
    for (int i = 0; i < pr; i += 2) {
        int xs = flower[b][i], xns = flower[b][i +
            1];
        pa[xs] = g[xns][xs].u;
        S[xs] = 1, S[xns] = 0;
        slack[xs] = 0, set_slack(xns);
        q_push(xns);
    }
    S[xr] = 1, pa[xr] = pa[b];
    for (int i = pr + 1; i < (int)flower[b].size();
        ++i) {
        int xs = flower[b][i];
        S[xs] = -1, set_slack(xs);
    }
    st[b] = 0;
}

inline bool on_found_edge(const edge &e) {
    int u = st[e.u], v = st[e.v];
    if (S[v] == -1) {
        pa[v] = e.u, S[v] = 1;
        int nu = st[match[v]];
        slack[v] = slack[nu] = 0;
        S[nu] = 0, q_push(nu);
    } else if (S[v] == 0) {
        int lca = get_lca(u, v);
        if (!lca) return augment(u, v), augment(v,
            u), 1;
        else add_blossom(u, lca, v);
    }
    return 0;
}

inline bool matching() {
    fill(S, S + n_x + 1, -1), fill(slack, slack +
        n_x + 1, 0);
    q.clear();
    for (int x = 1; x <= n_x; ++x) {
        if (st[x] == x && !match[x]) pa[x] = 0, S[x]
            = 0, q_push(x);
    }
    if (q.empty()) return 0;
    for (;;) {
        while ((int)q.size()) {
            int u = q.front();
            q.pop_front();
            if (S[st[u]] == 1) continue;
            for (int v = 1; v <= n; ++v) {
                if (g[u][v].w > 0 && st[u] != st[v]) {
                    if (dist(g[u][v]) == 0) {
                        if (on_found_edge(g[u][v]))
                            return 1;
                    } else update_slack(u, st[v]);
                }
            }
        }
        long long d = inf;
        for (int b = n + 1; b <= n_x; ++b) {
            if (st[b] == b && S[b] == 1) d = min(d,
                lab[b] / 2);
        }
    }
}

```

```

    for (int x = 1; x <= n_x; ++x) {
        if (st[x] == x && slack[x]) {
            if (S[x] == -1) d = min(d,
                dist(g[slack[x]][x]));
            else if (S[x] == 0) d = min(d,
                dist(g[slack[x]][x]) / 2);
        }
    }
    for (int u = 1; u <= n; ++u) {
        if (S[st[u]] == 0) {
            if (lab[u] <= d) return 0;
            lab[u] -= d;
        } else if (S[st[u]] == 1) lab[u] += d;
    }
    for (int b = n + 1; b <= n_x; ++b) {
        if (st[b] == b) {
            if (S[st[b]] == 0) lab[b] += d * 2;
            else if (S[st[b]] == 1) lab[b] -= d *
                2;
        }
    }
    q.clear();
    for (int x = 1; x <= n_x; ++x) {
        if (st[x] == x && slack[x] &&
            st[slack[x]] != x &&
            dist(g[slack[x]][x]) == 0)
            if (on_found_edge(g[slack[x]][x]))
                return 1;
    }
    for (int b = n + 1; b <= n_x; ++b) {
        if (st[b] == b && S[b] == 1 && lab[b] ==
            0) expand_blossom(b);
    }
}
return 0;
}
pair<long long, int> solve() {
    fill(match, match + n + 1, 0);
    n_x = n;
    int cnt = 0;
    long long ans = 0;
    for (int u = 0; u <= n; ++u) st[u] = u,
        flower[u].clear();
    long long w_max = 0;
    for (int u = 1; u <= n; ++u) {
        for (int v = 1; v <= n; ++v) {
            flower_from[u][v] = (u == v ? u : 0);
            w_max = max(w_max, g[u][v].w);
        }
    }
    for (int u = 1; u <= n; ++u) lab[u] = w_max;
    while (matching()) ++cnt;
    for (int u = 1; u <= n; ++u) {
        if (match[u] && match[u] < u) ans +=
            g[u][match[u]].w;
    }
    for (int i = 0; i < n; ++i)
        match[i] = match[i + 1] - 1;
    return make_pair(ans, cnt);
}
}
/*
int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
    int n, m;

```

```

    cin >> n >> m;
    Blossom g(n);
    for (int i = 0; i < m; ++i) {
        int u, v, w;
        cin >> u >> v >> w;
        g.add_edge(u-1, v-1, w);
        // pass 0-based index here.
    }
    auto ans = g.solve();
    // {max_weight, matching size}
    cout << ans.second << ' ' << ans.first << '\n';
    for (int i = 0; i < n; ++i) {
        if (g.match[i] > i) cout << i+1 << ' ' <<
            g.match[i]+1 << '\n'; // print 1-based
            index.
    }
}
*/

```

6 Geometry

6.1 convex_hull

```

#include<bits/stdc++.h>
using namespace std;

struct pt {
    double x, y;
    pt(double x=0, double y=0): x(x),y(y) {}
    bool operator == (const pt &rhs) const {
        return (x == rhs.x && y == rhs.y);
    }
    bool operator < (const pt &rhs) const {
        return y < rhs.y || (y==rhs.y && x < rhs.x);
    }
    bool operator > (const pt &rhs) const {
        return y > rhs.y || (y==rhs.y && x > rhs.x);
    }
};

double area(const vector<pt> &poly) {
    int n = static_cast<int>(poly.size());
    double area = 0;
    for(int i=0;i<n;++i) {
        pt p = i ? poly[i-1] :poly.back();
        pt q = poly[i];

        area += (p.x - q.x) * (p.y - q.y) ;
    }
    area = fabs(area)/2;
    return area ;
}

int orientation(pt a, pt b, pt c) {
    double v = a.x*(b.y-c.y)+
        b.x*(c.y-a.y)+c.x*(a.y-b.y);
    if (v < 0) return -1; // clockwise
    if (v > 0) return +1; // counter-clockwise
    return 0;
}

bool cw(
    pt a, pt b, pt c, bool include_collinear=false) {
    int o = orientation(a, b, c);

```



```

    return o < 0 || (include_collinear && o == 0);
}
bool collinear(pt a, pt b, pt c) {
    return orientation(a, b, c) == 0;
}

// Returns square of distance between point a and b
long double square_dist(pt a, pt b) {
    return (a.x-b.x)*1ll*(a.x-b.x)
        + (a.y-b.y)*1ll*(a.y-b.y);
}

// Returns points in clockwise order with a[0] as
// left lowermost point (Minimum point)
void convex_hull(
    vector<pt>& a, bool include_collinear = false) {
    pt p0 = *min_element(a.begin(), a.end(),
        [](pt a, pt b) {
            return make_pair(a.y, a.x)
                < make_pair(b.y, b.x);
        });
    auto square_dist_from_p0 = [&p0](pt& a){
        return square_dist(p0, a);
    };
    sort(a.begin(), a.end(), [&p0](
        const pt& a, const pt& b) {
        int o = orientation(p0, a, b);
        if (o == 0)
            return square_dist_from_p0(a)
                < square_dist_from_p0(b);
        return o < 0;
    });
    if (include_collinear) {
        int i = (int)a.size()-1;
        while (i >= 0 &&
            collinear(p0, a[i], a.back())) i--;
        reverse(a.begin()+i+1, a.end());
    }

    vector<pt> st;
    for (int i = 0; i < (int)a.size(); i++) {
        while (st.size() > 1 && !cw(st[st.size()-2],
            st.back(), a[i], include_collinear))
            st.pop_back();
        st.push_back(a[i]);
    }

    a = st;
}

// poly: Contains points of polygon in counter
// clockwise order, with poly[0] as lower
// leftmost point (minimum point) and top is the index
// of top rightmost point (maximum point).
// Min/Max are defined by comparator operator
// defined for points.
// It returns 1: Point outside, 0: Point in boundary,
// -1: Point inside.
int pointVsConvexPolygon(
    pt &point, vector<pt> &poly, int top) {
    if (point < poly[0] || point > poly[top]) return 1;
    int o = orientation(point, poly[top], poly[0]);
    if (o == 0) {
        if (point == poly[0] || point == poly[top])
            return 0;
        return (top == 1 || top+1==poly.size())
            ? 0 : -1;
    }
}

```

```

} else if (o < 0) {
    auto itLeft = upper_bound(
        poly.rbegin(), poly.rend() - top-1, point);
    return orientation((itLeft == poly.rbegin() ?
        poly[0]:itLeft[-1]), itLeft[0], point);
} else {
    auto itRight = lower_bound(poly.begin()+1,
        poly.begin()+top, point);
    return orientation(point,
        itRight[0], itRight[-1]);
}
}

// a and b represent direction:
// Returns 1 if direction is ccw, 0 is collinear
// and -1 is direction is cw (clockwise).
int ccw(const pt &a, const pt&b) {
    long double ans = (long double)a.x*b.y
        - (long double)a.y*b.x;
    if (ans < 0) return -1;
    return (ans > 0);
}

// Maximum distance (squared) between
// given sets of points
// in O(N) or O(N*log(N))
// (first make them a convex polygon)
long double maxSquareDist(vector<pt> &poly) {
    int n = static_cast<int>(poly.size());
    long double res = 0;
    for (int i = 0, j = n < 2 ? 0 : 1; i < j; ++i)
        for (; j = (j+1)%n) {
            res = max(res, square_dist(
                poly[i], poly[j]));
            pt dir1 = pt(poly[i+1].x-poly[i].x,
                poly[i+1].y-poly[i].y);
            pt dir2 = pt(poly[(j+1)%n].x-poly[j].x,
                poly[(j+1)%n].y-poly[j].y);
            if (ccw(dir1, dir2) <= 0) break;
        }
    return res;
}

```

7 STL

7.1 pbds

```

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

#define ordered_set tree<int, null_type, less<int>, \
    rb_tree_tag, tree_order_statistics_node_update>

// strict less than is recommended to avoid problems
// with equality
// order_of_key(T key): number of elements less than key
// find_by_order(int): gives the 0 based index elem

```

7.2 pragmas

```
#pragma GCC optimize("O3,unroll-loops")  
#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")
```

7.3 random

```
mt19937_64 rng(chrono::steady_clock::now().  
               time_since_epoch().count());  
  
// cal rng() for random number
```
