

东校区 2010 学年度第一学期 10 级《高等数学一》期末考试题 **答案** C-1

一. 完成下列各题 (每小题 7 分, 共 70 分)

1. 求 $\lim_{n \rightarrow \infty} \left(1 + \frac{1}{2n}\right)^n = \lim_{n \rightarrow \infty} \left[\left(1 + \frac{1}{2n}\right)^{2n}\right]^{\frac{1}{2}} = e^{\frac{1}{2}}.$

2. 求 $\lim_{(x,y) \rightarrow (0,0)} \frac{\ln(1+xy)}{\sin 2xy}$

令 $u = xy$, 则 $\lim_{(x,y) \rightarrow (0,0)} u = 0.$

$$\lim_{(x,y) \rightarrow (0,0)} \frac{\ln(1+xy)}{\sin(2xy)} = \lim_{u \rightarrow 0} \frac{\ln(1+u)}{\sin 2u} = \lim_{u \rightarrow 0} \frac{1}{2 \cos 2u} = \frac{1}{2}.$$

3. $y = x \arccos x^2$, 求 y' $y' = \arccos(x^2) - \frac{2x^2}{\sqrt{1-x^4}}.$

4. 设 $z + \cos(xy) = e^z$, 求 $\frac{\partial z}{\partial x}.$

$$z_x - y \sin(xy) = e^z \cdot z_x$$

$$z_x = \frac{y \sin(xy)}{1 - e^z}.$$

5. 设 $f(x, y, z) = z \sqrt{\frac{x}{y}}$, 求 $df(1, 1, 1).$

$$f_x(x, 1, 1) = (x)' = 1, f_x(1, 1, 1) = 1$$

$$f_y(1, y, 1) = \left(\frac{1}{y}\right)' = -\frac{1}{y^2}, f_y(1, 1, 1) = -1$$

$$f_z(1, 1, z) = (z)' = 0, f_z(1, 1, 1) = 0$$

$$df(1, 1, 1) = f_x(1, 1, 1)dx + f_y(1, 1, 1)dy + f_z(1, 1, 1)dz = dx - dy.$$