

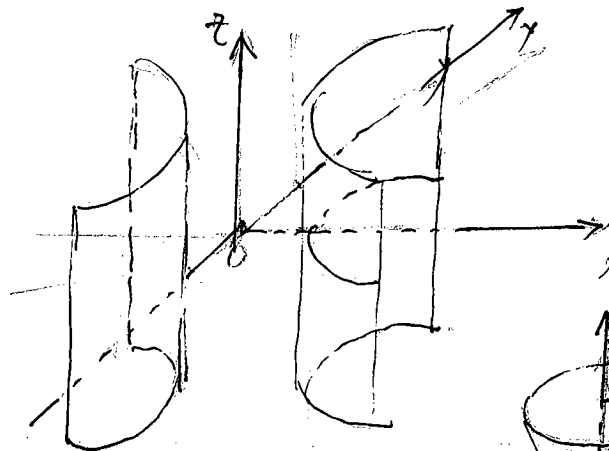
(4)

$$x^2 - y^2 = 2x$$

$$x^2 - 2x + 1 - y^2 = 1$$

$$(x-1)^2 - y^2 = 1$$

双曲面.

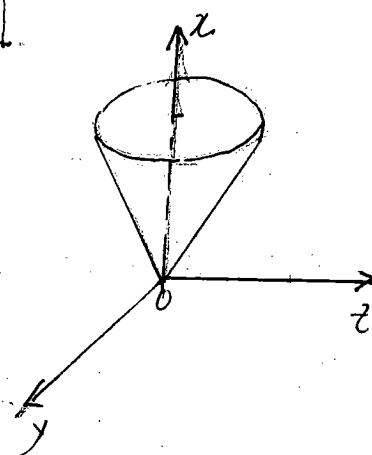


$$2 \cos \frac{\pi}{12} - 2$$

$$2 \cos \frac{2\pi}{3} - 12$$

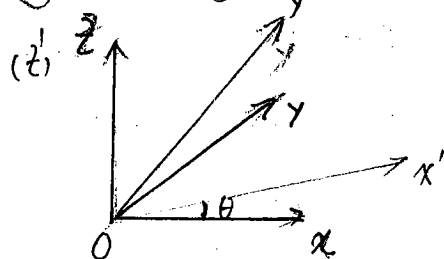
(5)

$$2y^2 + z^2 = x, \text{ 椭圆锥面.}$$



(6)

$$z = xy$$



作变换

$$x = x' \cos \theta - y' \sin \theta$$

$$y = x' \sin \theta + y' \cos \theta$$

$$z = z'$$

$$z = z' = (x' \cos \theta - y' \sin \theta) \cdot (x' \sin \theta + y' \cos \theta)$$

$$= x'^2 \sin \theta \cos \theta + x' \cdot y' \cos^2 \theta - x' \cdot y' \sin^2 \theta - y'^2 \sin \theta \cos \theta$$

$$= (x'^2 - y'^2) \cdot \sin \theta \cos \theta + x' y' (\cos^2 \theta - \sin^2 \theta)$$

$$\cos^2 \theta - \sin^2 \theta = \cos 2\theta \stackrel{\frac{1}{2}}{=} 0, \quad 2\theta = \frac{\pi}{2}, \quad \theta = \frac{\pi}{4}$$

$$z' = \frac{1}{2} (x'^2 - y'^2)$$

$$\sin \theta = \cos \theta = \frac{1}{\sqrt{2}}, \quad \sin \theta \cos \theta = \frac{1}{2}$$

$$x'^2 - y'^2 = 2z' \quad \text{双曲抛物面.}$$

