

Optimization via simulation

CASE STUDY: A STOCHASTIC INSPECTION SYSTEM

Preparation:

Slide 2

- Hold Module
- How to create a “signal” module?

A Stochastic Inspection System

Slide 3

- In a nuclear plant, some parts that need inspection (or some special treatment) arrive according to a Poisson process with rate λ . Every T time units the system is inspected and at each inspection time all messages present (if any) are cleared from the system (this process takes almost no time). A fixed cost of $K > 0$ is incurred for each inspection. Also, for each item there is a holding cost of $h > 0$ per unit time the item has to wait before it is cleared from the system. We wish to determine the optimal value of T for which the long-run average cost per unit time is minimal.
- Let $K=50$, $h=1$, $\lambda=1$. What's the T^* ?
- How about $K=500$, $h=0.01$, $\lambda=1$?

Build the model

Slide 4



Discussions

Slide 5

- How to find out the optimal T^* ?
 - ▣ Trial & error
 - ▣ Optimization techniques/DOE

OptQuest

Slide 6

□ Steps

- Build a base model
- Identify control/decision variables
- Create an “optimization” model – OptQuest
- Change the decision variables from “fix” to “design”
- Configure parameters, constraints, replications etc.
- Optimize!

OptQuest

Slide 7

Experiment
Select an experiment type, specify a name and choose a top-level agent.

Name:

Top-level agent:

Experiment Type:

- ☒ Simulation
- ☒ **Optimization**
- ☒ Parameter Variation
- ☒ Compare Runs
- ☒ Monte Carlo
- ☒ Sensitivity Analysis
- ☒ Calibration
- ☒ Custom

Searches for a parameter set corresponding to the best value of the provided objective function. A number of constraints on parameters or model variables can be specified. Optimization under uncertainty is supported by using replications. Optimization progress chart is displayed.

☒ Copy model time settings from:

< Back Next > Cancel Finish

OPT1 - Optimization Experiment

Name: ☐ Ignore

Top-level agent:

Objective: ☒ minimize ☐ maximize

☒ Number of iterations:

☐ Automatic stop

Maximum available memory: Mb

Create default UI

Parameters

Parameters:

Parameter	Type	Value			
		Min	Max	Step	Suggest
pLumbda	fixed	1			
pH	fixed	1			
pK	fixed	50			
pT	discrete	1	200	1	

OptQuest_Case1 : OPT1

Run

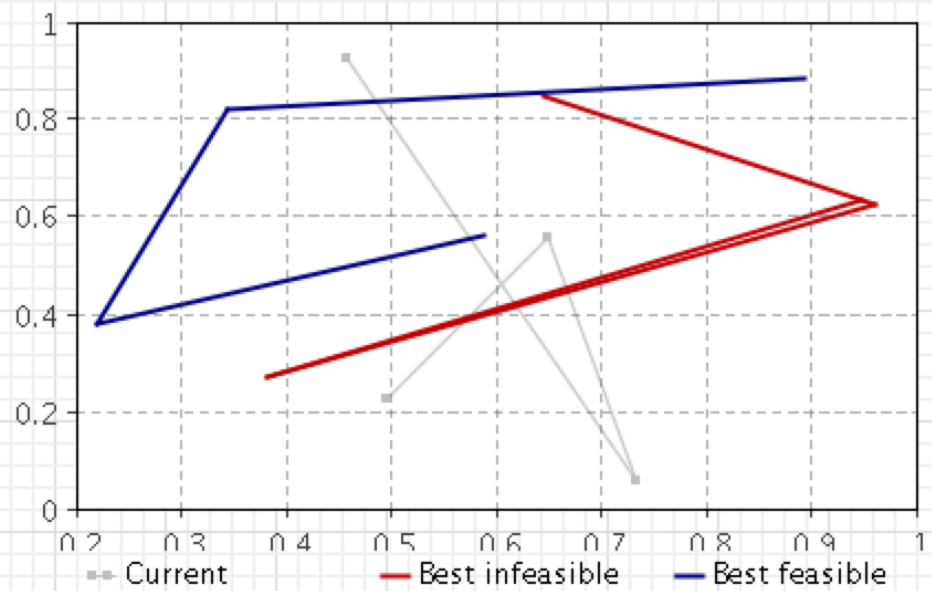
	Current	Best
Iteration:	infeasible?	infeasible?
Objective: ↓	?	?

Parameters

pLumbda	?	?
pH	?	?
pK	?	?
pT	?	?

Copy the best solution to the clipboard

copy



OptQuest_Case1 : OPT1

Run

	Current	Best
Iteration:	197	51
Objective:	183,566.77326	609.979

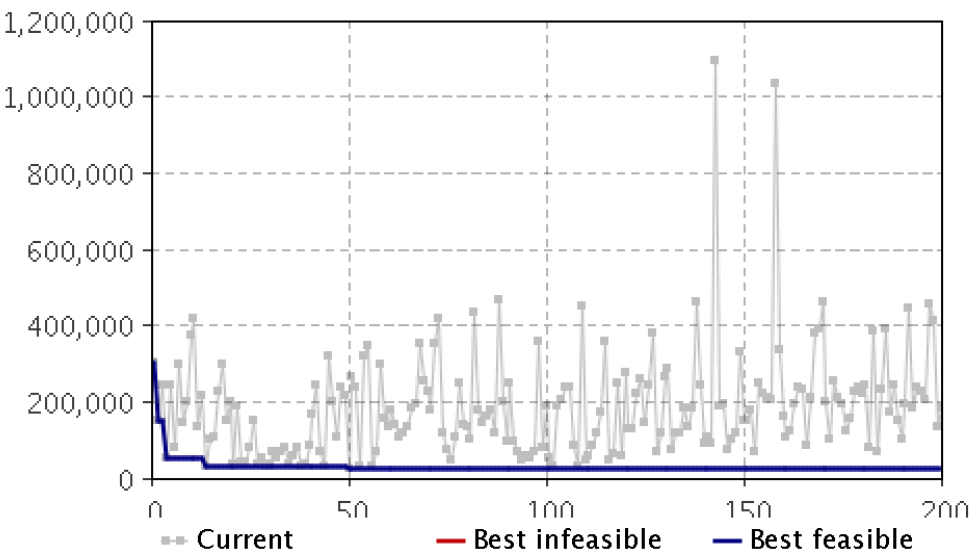
Parameters

pLumbda	1	1
pH	1	1
pK	50	50
pT	195	8

Copy the best solution to the clipboard

▶

copy



Closed form

Slide 10

$$\square T^* = \text{Sqrt}(2K / (h * \text{Lambda}))$$

Extension?

Slide 11

- What if the holding cost is $f(n_t)$ per time unit, in which n_t is the number of items and f is a function, e.g., $f(x) = x \log(x+5)$?